

# Realistic Image Synthesis

## - HDR Capture & Tone Mapping -

Philipp Slusallek

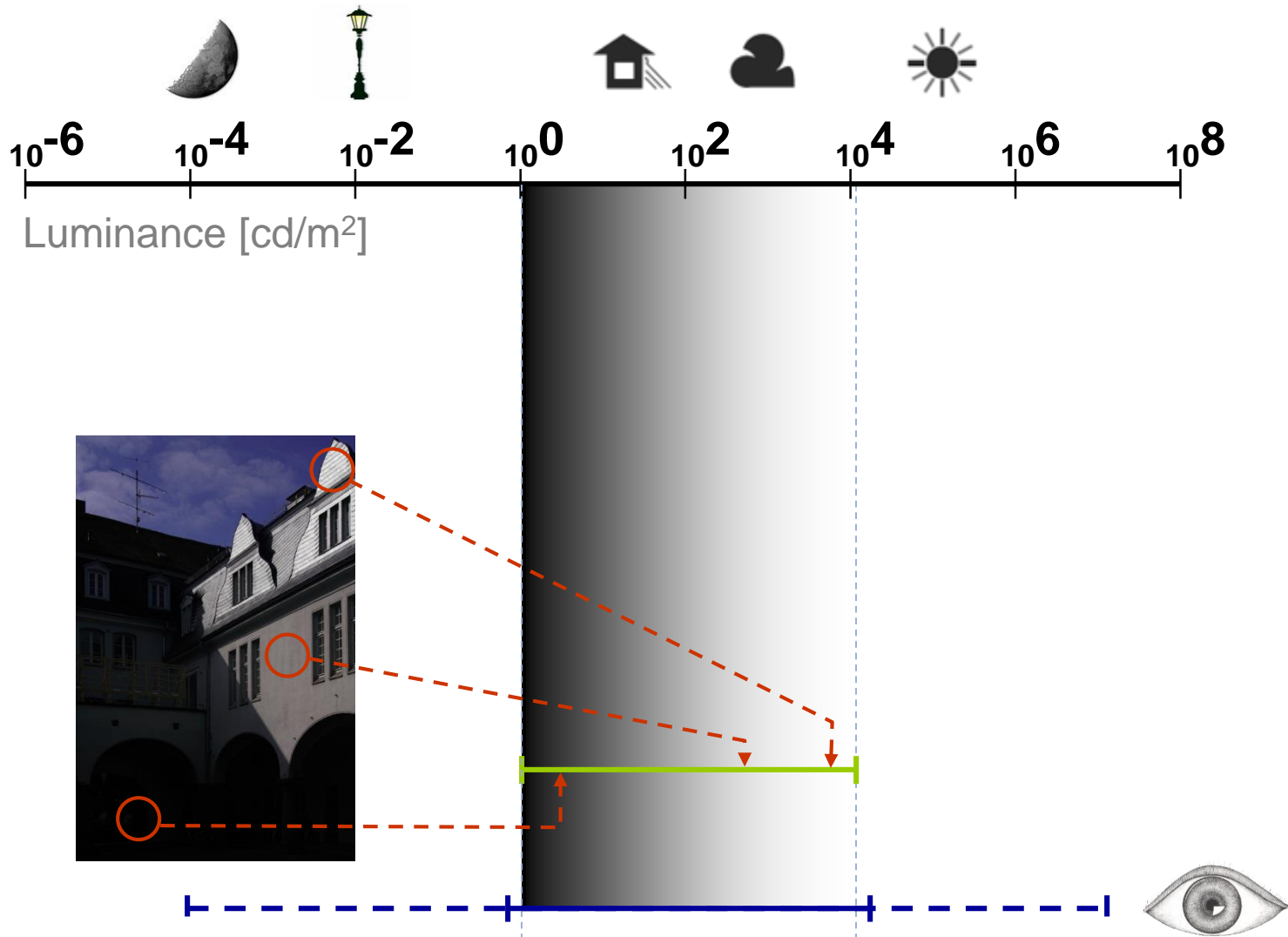
Karol Myszkowski

Gurprit Singh

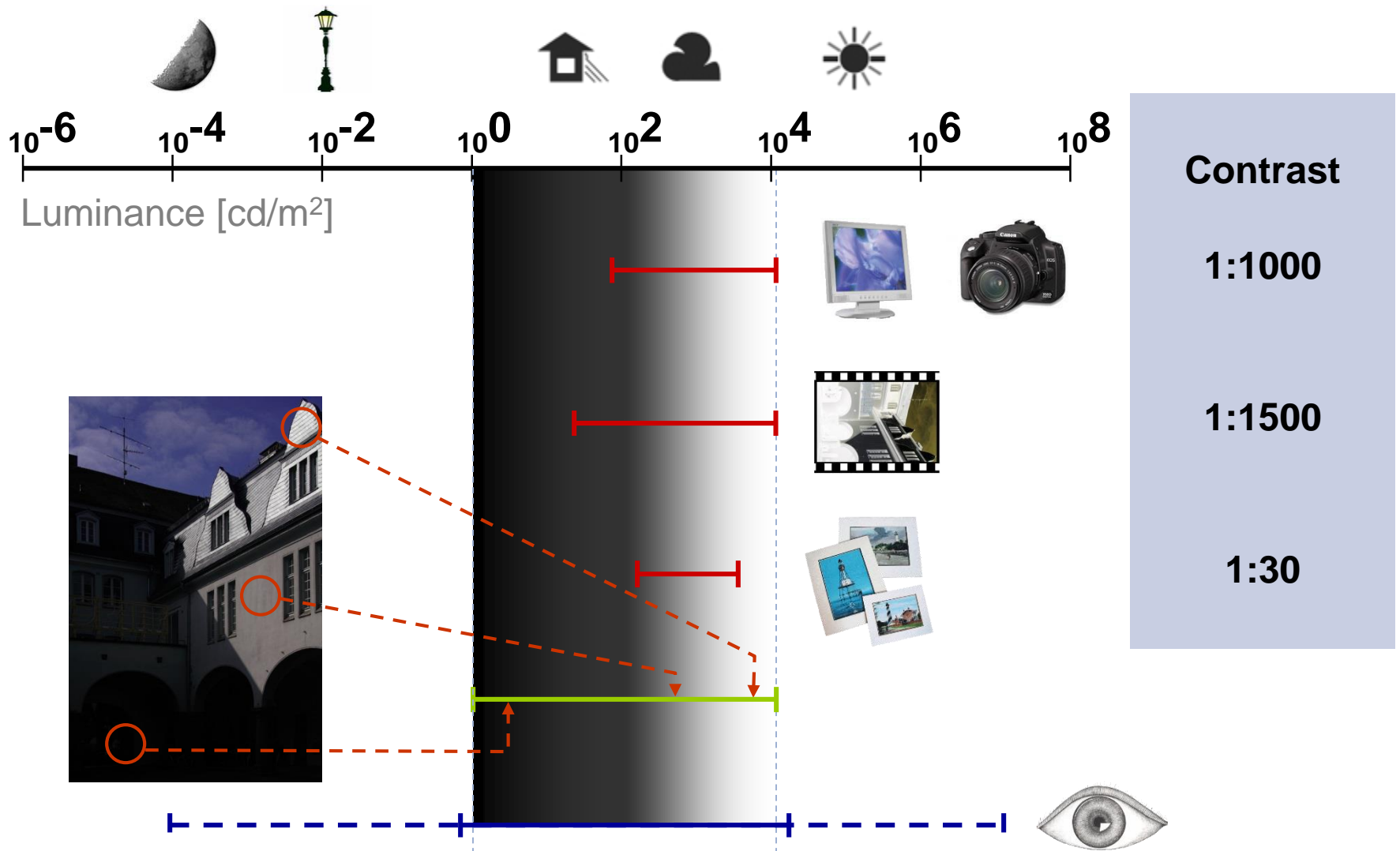
# LDR vs HDR – Comparison

Standard Dynamic Range		High Dynamic Range
	<p><b>QUALITY OF CONTRAST &amp; COLOR</b></p>	
<b>50 dB</b>	<b>Camera Dynamic Range</b>	<b>120 dB</b>
<b>1:200</b>	<b>Display Contrast</b>	<b>1:15.000</b>
<b>limited</b>	<b>Color Gamut</b>	<b>vivid and saturated colors</b>
<b>display-referred</b>	<b>Image Representation</b>	<b>scene-referred</b>
<b>display limited</b>	<b>Fidelity</b>	<b>as good as the eye can see</b>

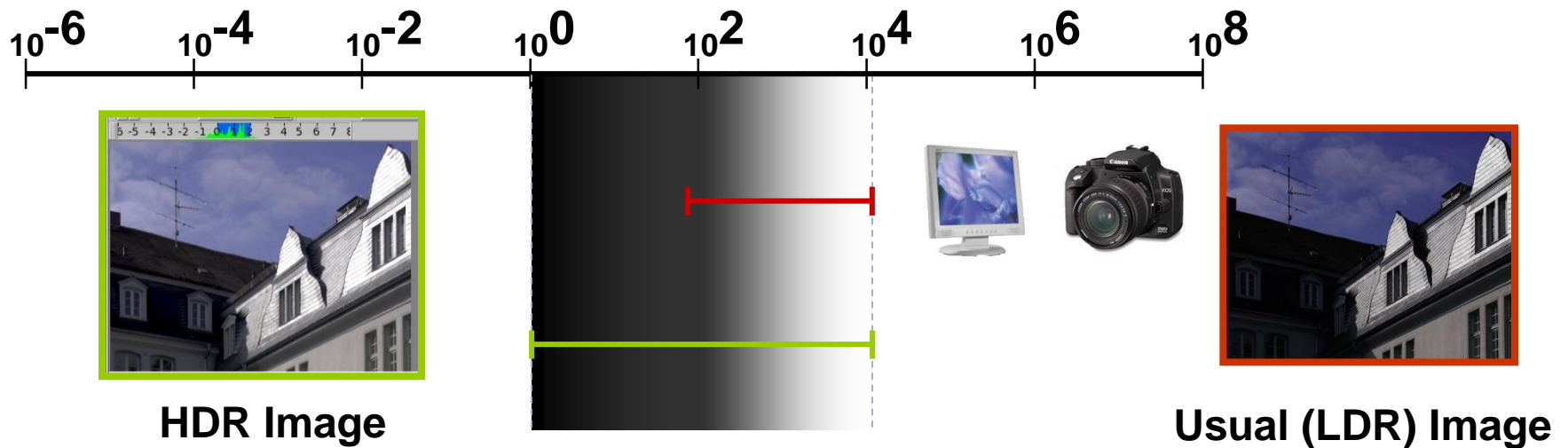
# Various Dynamic Ranges (1)



# Various Dynamic Ranges (2)



# High Dynamic Range



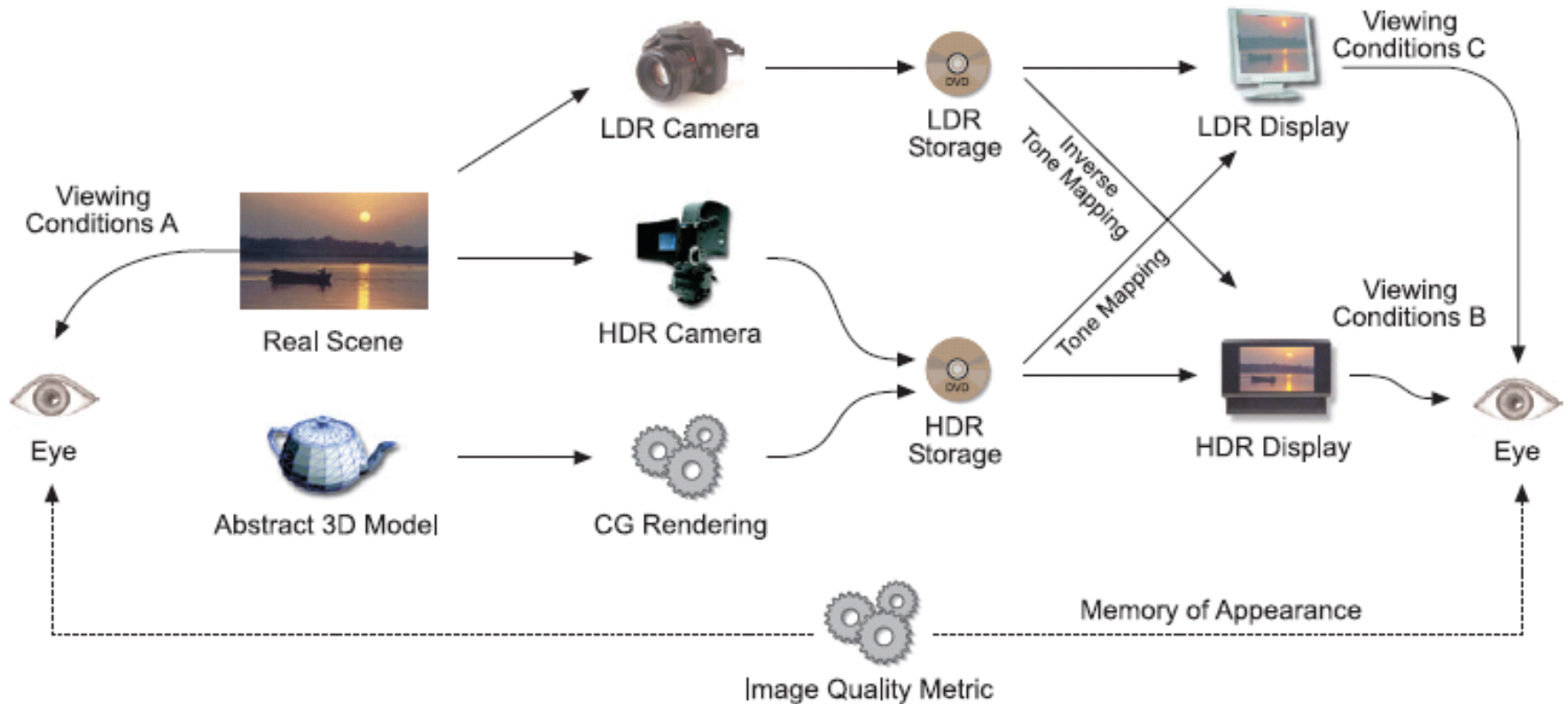
# Measures of Dynamic Range

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Contrast ratio	<b><math>CR = 1 : (Y_{\text{peak}}/Y_{\text{noise}})</math></b>	displays (1:500)
Orders of magnitude	<b><math>M = \log_{10}(Y_{\text{peak}}) - \log_{10}(Y_{\text{noise}})</math></b>	HDR imaging (2.7 orders)
Exposure latitude (f-stops)	<b><math>L = \log_2(Y_{\text{peak}}) - \log_2(Y_{\text{noise}})</math></b>	photography (9 f-stops)
Signal to noise ratio (SNR)	<b><math>SNR = 20 * \log_{10}(A_{\text{peak}}/A_{\text{noise}})</math></b>	digital cameras (53 [dB])

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# HDR Pipeline

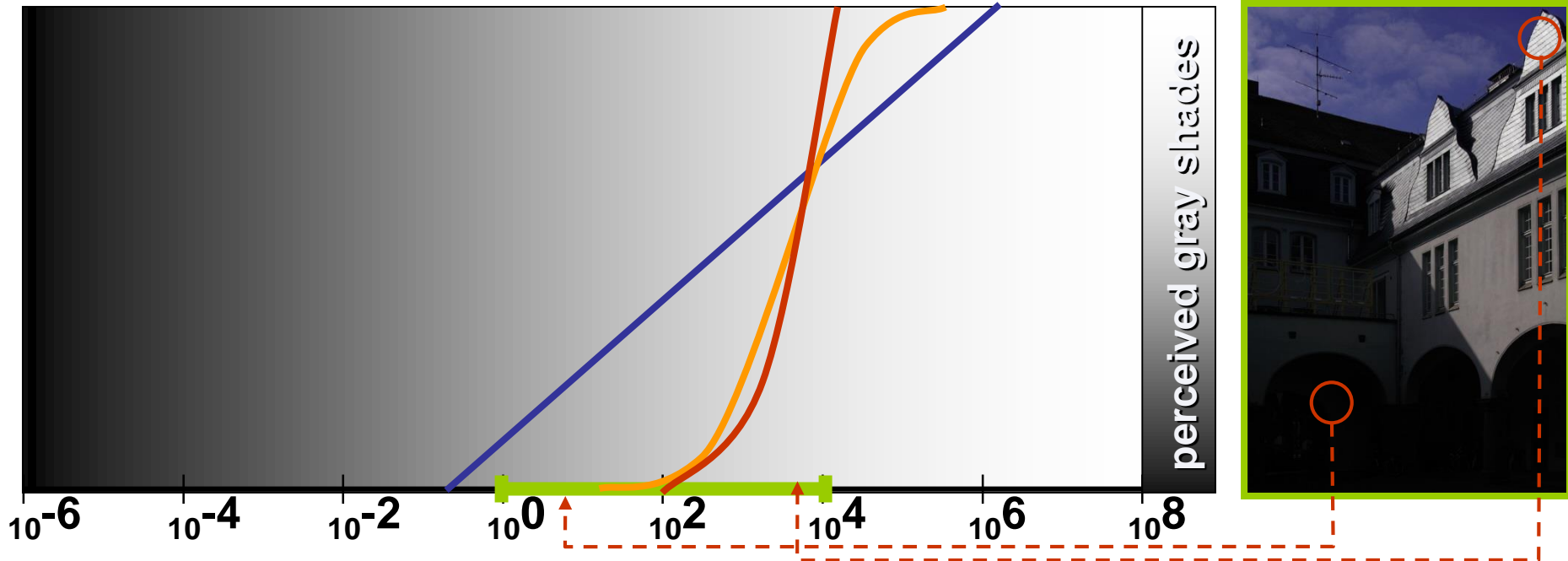
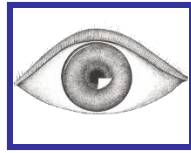


# Lecture Overview

- Capture of HDR images and video
  - HDR sensors
  - Multi-exposure techniques
  - Photometric calibration
- Tone Mapping of HDR images and video
  - Early ideas for reducing contrast range
  - Image processing – fixing problems
  - Alternative approaches
  - Perceptual effects in tone mapping
- Summary

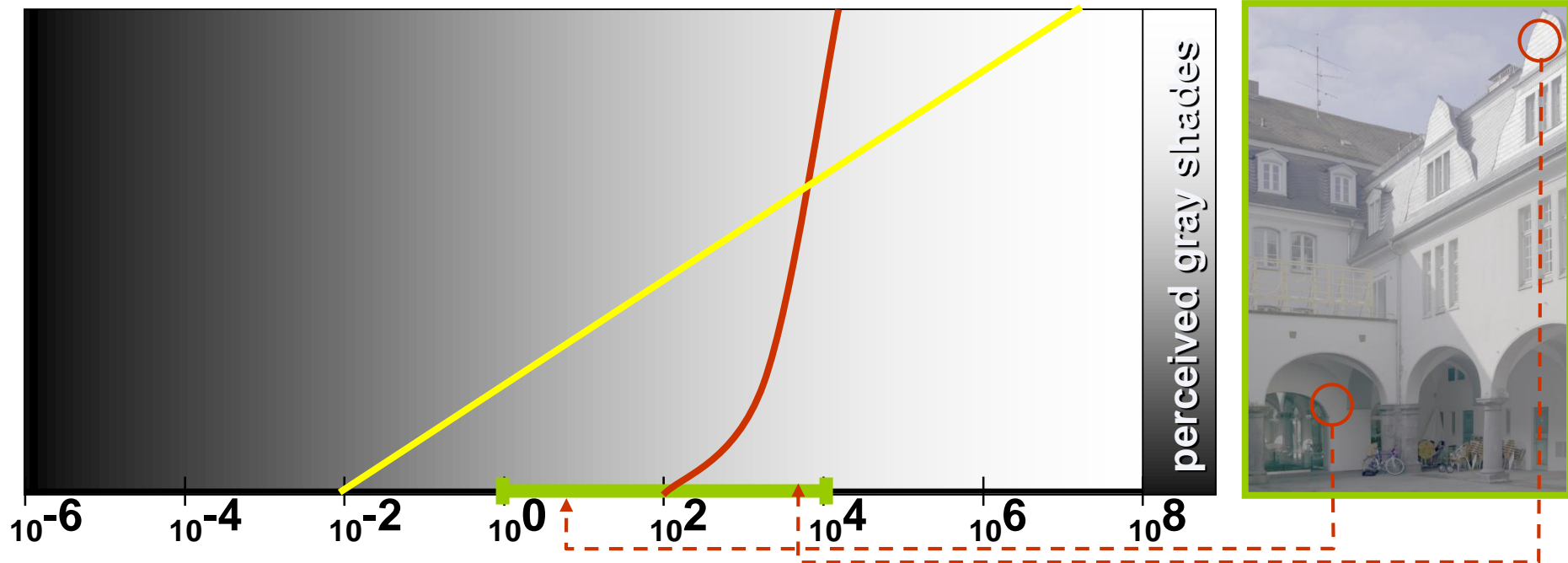


# HDR: a normal camera can't...



- linearity of the CCD sensor
- bound to 8-14bit processors
- saved in an 8bit gamma corrected image

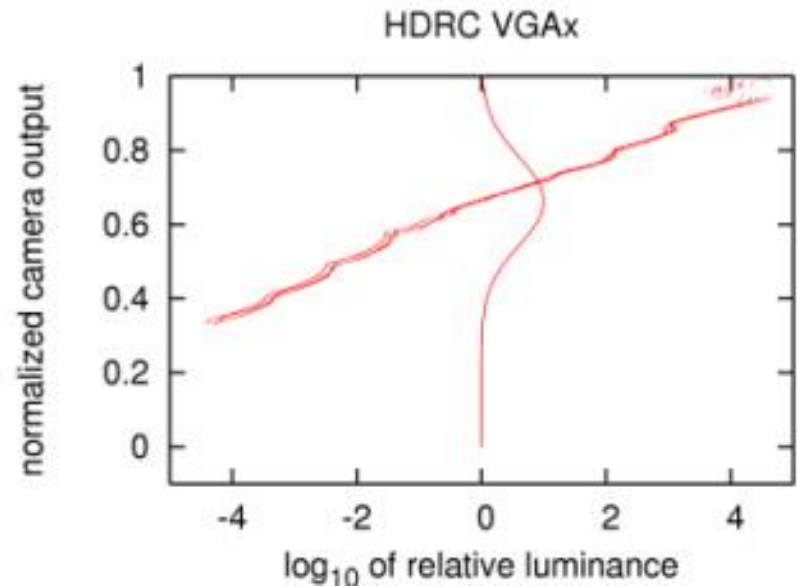
# HDR Sensors



- logarithmic response
- locally auto-adaptive
- hybrid sensors (linear-logarithmic)

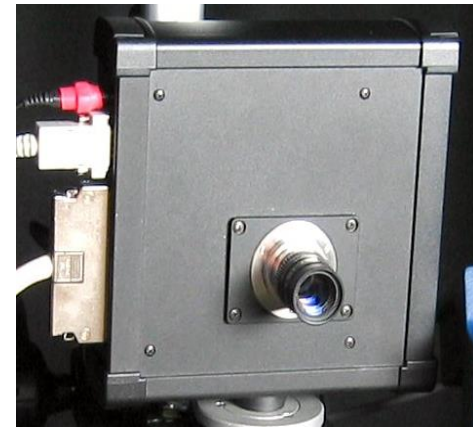
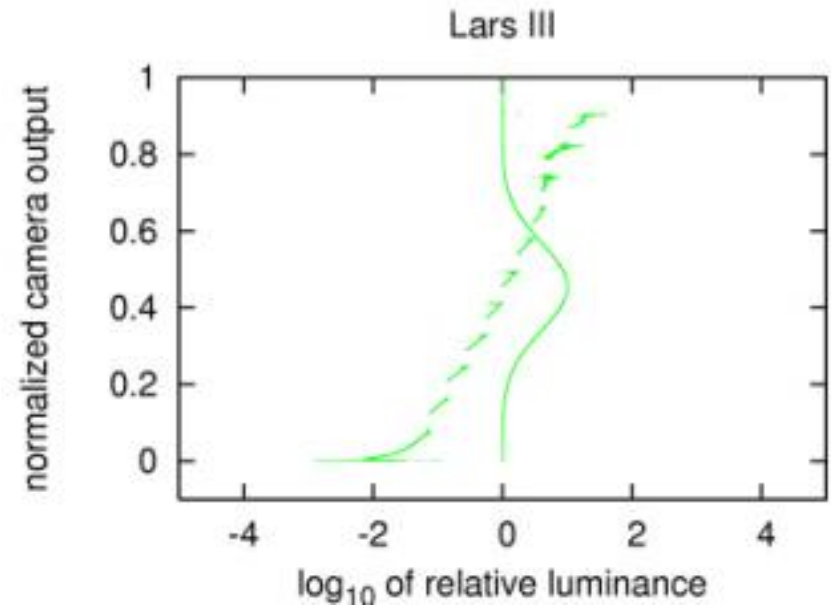
# Logarithmic HDR Sensor

- CMOS sensor (10bit)
- Transforms collected charge to logarithmic voltage (analog circuit)
- Dynamic range at the cost of quantization
- Very high saturation level
- High noise floor
- Non-linear noise
- Slow response at low luminance levels
- **Lin-log variants of sensor**
  - better quantization
  - lower noise floor



# Locally Auto-adaptive Sensor

- Individual integration time for each pixel
- 16bit sensor
  - collected charge (8bit)
  - integration time (8bit)
- Irradiance from time and charge
- Complicated noise model
- Fine quantization over a wide range
- Non-continuous output!



# HDR with a normal camera

Dynamic range of a typical CCD **1:1000**

Exposure variation ( $1/60$  :  $1/6000$ ) 1:100

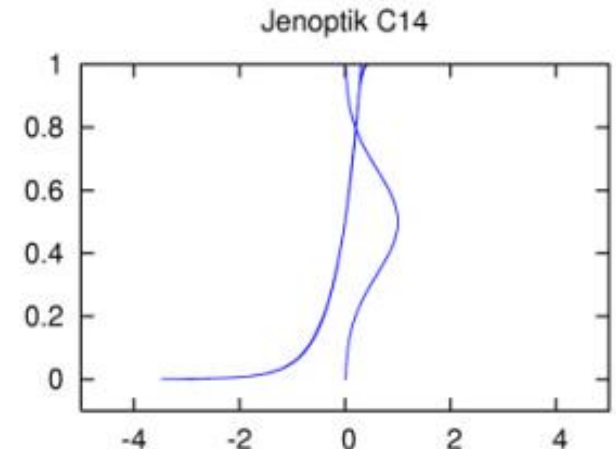
Aperture variation (f/2.0 : f/22.0)  $\sim$ 1:100

Sensitivity variation (ISO 50 : 800)  $\sim$ 1:10

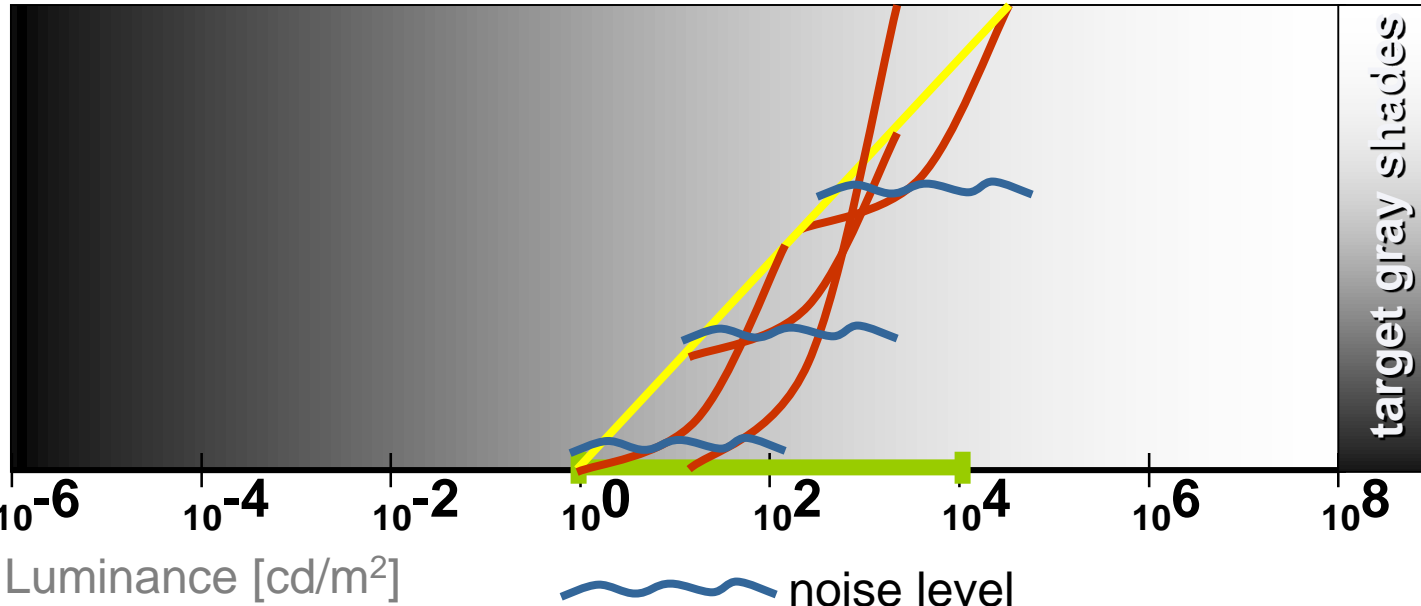
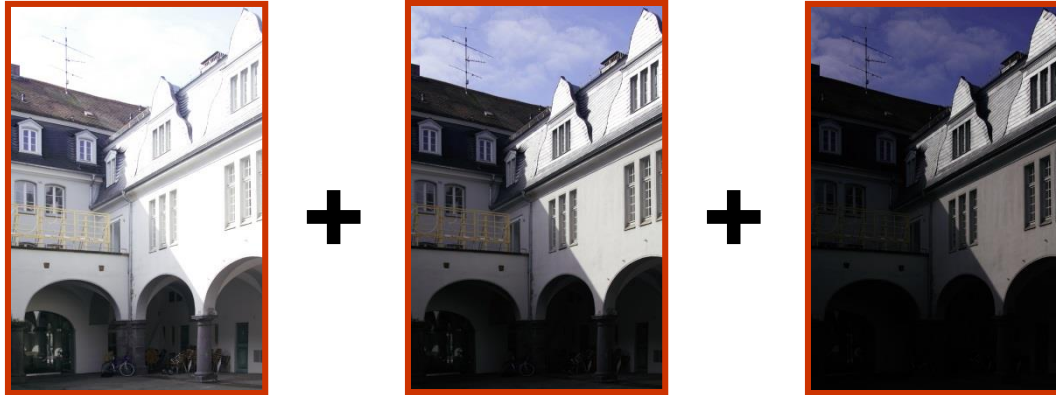
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**Total operational range 1:100,000,000 High Dynamic Range!**

Dynamic range of a single capture only **1:1000.**



# Multi-exposure Technique (1)



HDR Image

# Multi-exposure Technique (2)

- **Input**

- images captured with varying exposure
  - change exposure time, sensitivity (ISO), ND filters
  - same aperture!
  - exactly the same scene!

- **Unknowns**

- camera response curve (can be given as input)
- HDR image

- **Process**

- recovery of camera response curve (if not given as input)
- linearization of input images (to account for camera response)
- normalization by exposure level
- suppression of noise
- estimation of HDR image (linear combination of input images)

# Algorithm (1/3)

## Camera Response

$$y_{ij} = I(x_{ij} \cdot t_i)$$

## Merge to HDR

- Linearize input images and normalize by exposure time

$$x_{ij} = \frac{I^{-1}(y_{ij})}{t_i}$$

assume  $I$  is correct (initial guess)

- Weighted average of images (weights from certainty model)

$$x_j = \frac{\sum_i w_{ij} x_{ij}}{\sum_i w_{ij}}$$

## Optimize Camera Response

- Camera response

$$I^{-1}(y_{ij}) = t_i x_j$$

assume  $x_j$  is correct

- Refine initial guess on response
  - linear eq. (Gauss-Seidel method)

$$E_m = \{(i, j) : y_{ij} = m\}$$

$$I^{-1}(m) = \frac{1}{\text{Card}(E_m)} \sum_{i, j \in E_m} t_i x_j$$

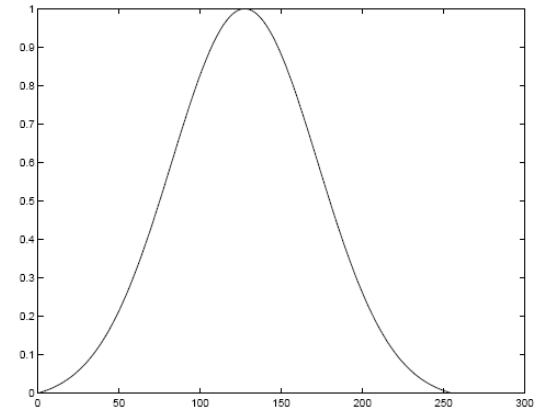
<p><math>t_i</math> exposure time of image <math>i</math> <math>y_{ij}</math> pixel of input image <math>i</math> at position <math>j</math> <math>I</math> camera response <math>x_j</math> HDR image at position <math>j</math> <math>w</math> weight from certainty model <math>m</math> camera output value</p>
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# Algorithm (2/3)

- Certainty model (for 8bit image)
  - High confidence in middle output range
  - Dequantization uncertainty term
  - Noise level

$$w(y_{ij}) = \exp\left(-4 \frac{(y_{ij} - 127.5)^2}{127.5^2}\right)$$



- Longer exposures are favored  $t_i^2$ 
  - Less random noise
- Weights

$$w_{ij} = w(y_{ij})t_i^2$$

# Algorithm (3/3)

1. Assume initial camera response  $I$  (linear)
2. Merge input images to HDR

$$x_j = \frac{\sum_i w(y_{ij}) t_i^2 \frac{I^{-1}(y_{ij})}{t_i}}{\sum_i w(y_{ij}) t_i^2}$$

3. Refine camera response

$$E_m = \{(i, j) : y_{ij} = m\}$$

$$I^{-1}(m) = \frac{1}{\text{Card}(E_m)} \sum_{i, j \in E_m} t_i x_j$$

4. Normalize camera response by middle value:  $I^{-1}(m)/I^{-1}(m_{med})$
5. Repeat 2,3,4 until objective function is acceptable

$$O = \sum_{i, j} w(y_{ij}) (I^{-1}(y_{ij}) - t_i x_j)^2$$

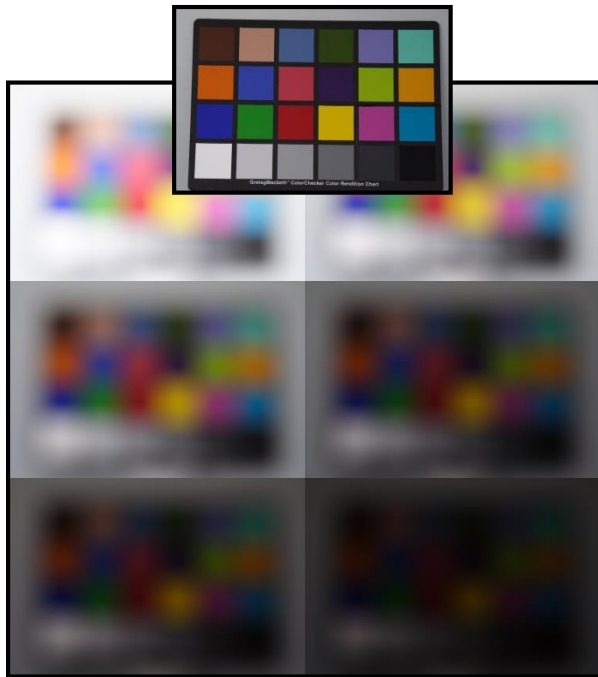
# Other Algorithms

- [Debevec & Malik 1997]
  - in log space
  - assumptions on the camera response
    - monotonic
    - continuous
  - a lot to compute for >8bit
- [Mitsunaga & Nayar 1999]
  - camera response approximated with a polynomial
  - very fast
- Both are more robust but less general
  - not possible to calibrate non-standard sensors

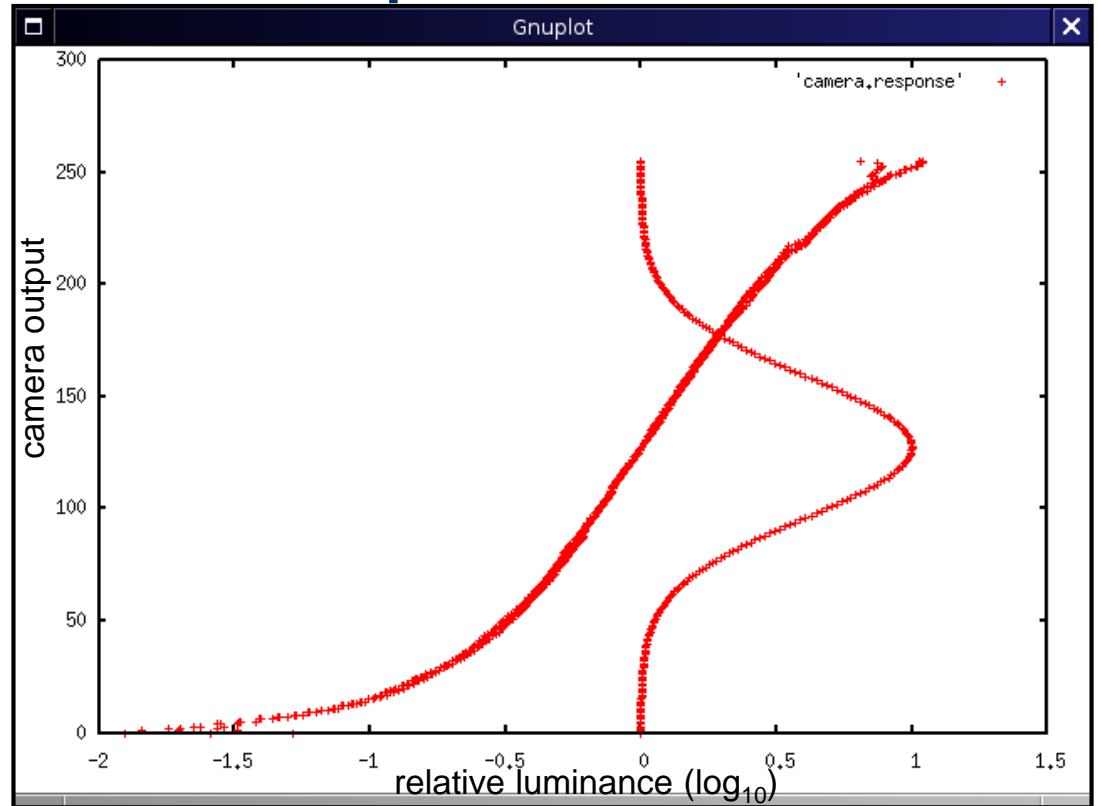
# Calibration (Response Recovery)

- Camera response can be reused
  - for the same camera
  - for the same picture style settings (eg. contrast)
- Good calibration target
  - Neutral target (e.g. Gray Card)
    - Minimize impact of color processing in camera
  - Smooth illumination
    - Uniform histogram of input values
  - Out-of-focus
    - No interference with edge aliasing and sharpening

# Recovered Camera Response



multiple exposures  
of out-of-focus  
color chart



recovered camera response  
(for each RGB channel separately)

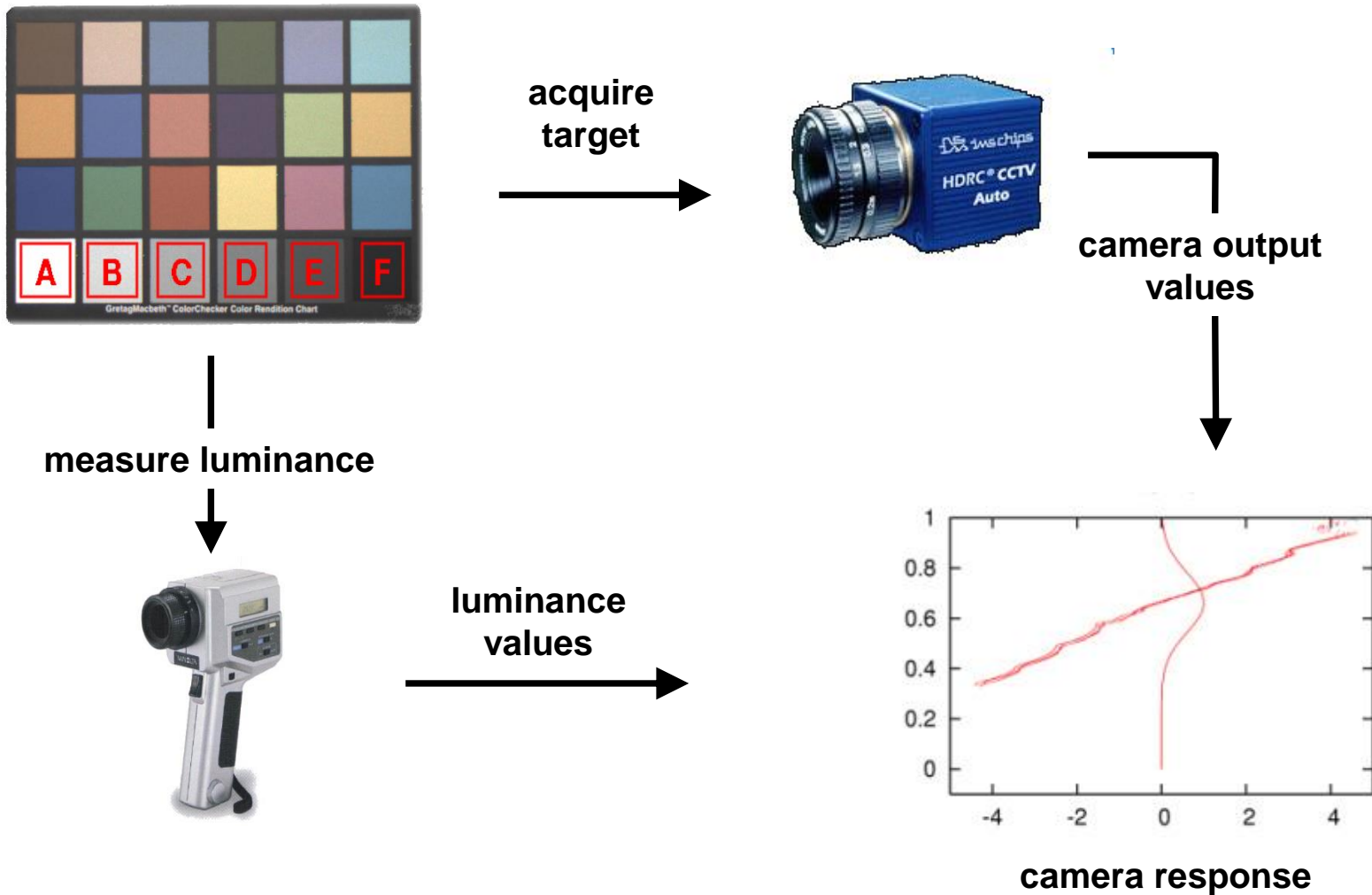
# Issues with Multi-exposures

- How many source images?
  - First expose for shadows: all output values above 128 (for 8bit imager)
  - 2 f-stops spacing (factor of 4) between images
  - one or two images with 1/3 f-stop increase will improve quantization in HDR image
  - Last exposure: no pixel in image with maximum value
- Alignment
  - Shoot from tripod
  - Otherwise use panorama stitching techniques to align images
- Ghosting
  - Moving objects between exposures leave “ghosts”
  - Statistical method to prevent such artifacts
- Practical only for images!
  - Multi-exposure video projects exist, but require care with subsequent frame registration by means of optical flow

# Photometric Calibration

- Converts camera output to luminance
  - requires camera response,
  - and a reference measurement for known exposure settings
- Applications
  - predictive rendering
  - simulation of human vision response to light
  - common output in systems combining different cameras

# Photometric Calibration (cntd.)





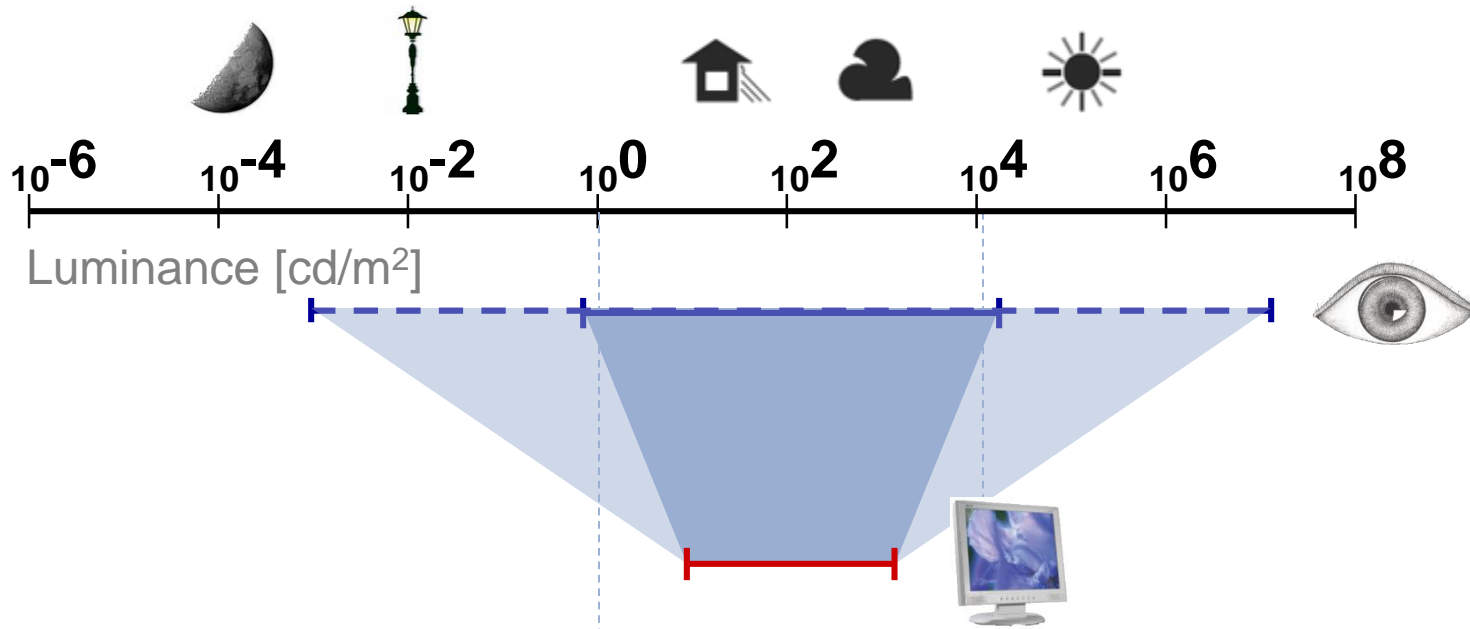
# HDR Sensor vs. Multi-exposure

- HDR camera
  - Fast acquisition of dynamic scenes at 25fps without motion artifacts
  - Currently lower resolution
- LDR camera + multi-exposure technique
  - Slow acquisition (impossible in some conditions)
  - Higher quality and resolution
  - High accuracy of measurements

# Lecture Overview

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- **Tone Mapping of HDR images and video**
  - Early ideas for reducing contrast range
  - Image processing – fixing problems
  - Alternative approaches
  - Perceptual effects in tone mapping
- **Summary**

# HDR Tone Mapping



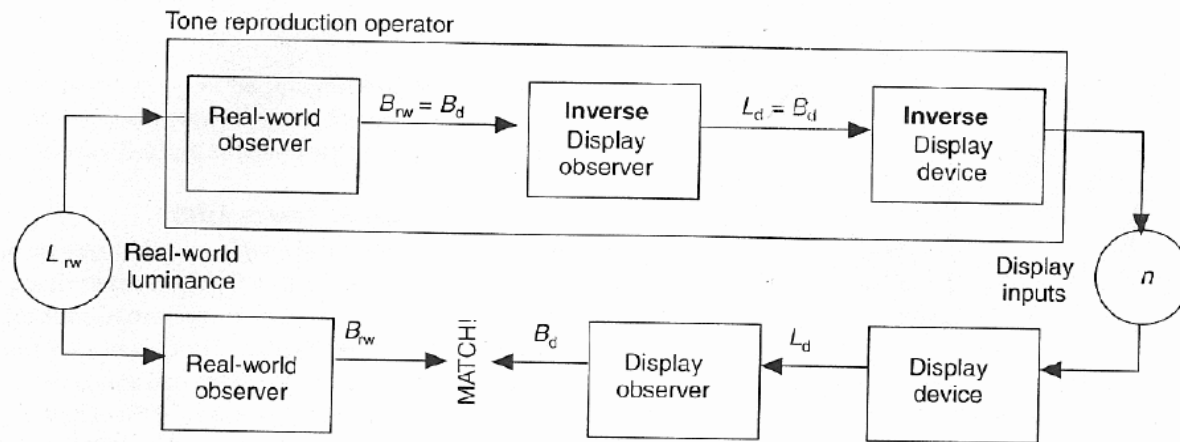
- Objectives of tone mapping
  - nice looking images
  - perceptual brightness match
  - good detail visibility
  - equivalent object detection performance
  - really application dependent...

# Previous lectures...

## General Principle

- **Approach**

- Create model of the observer
- Requirement:
  - Observer should perceive same image from real and virtual display
- Compute Tone-Mapping using concatenation and inversion of operators
- Model usually operates only on luminance (no color)



# General Idea

- Luminance as an input
  - absolute luminance
  - relative luminance (luminance factor)
- Transfer function
  - maps luminance to a certain pixel intensity
  - may be the same for all pixels (**global operators**)
  - may depend on spatially local neighbors (**local operators**)
  - dynamic range is reduced to a specified range
- Pixel intensity as output
  - often requires gamma correction
- Colors
  - most algorithms work on luminance
    - use RGB to Yxy color space transform
    - inverse transform using tone mapped luminance
  - otherwise each RGB channel processed independently

# General Problems

- Constraints in observation conditions
  - limited contrast
  - quantization
  - different ambient illumination
  - different luminance levels
  - adaptation level often incorrect for the scene
  - narrow field of view
- Appearance may not always be matched

# Transfer Functions

- Linear mapping (naïve approach)
  - like taking a usual photo
- Brightness function
- Sigmoid responses
  - simulate our photoreceptors
  - simulate response of photographic film
- Histogram equalization
  - standard image processing
  - requires detection threshold limit to prevent contouring

# Adapting Luminance

- Maps luminance on a scale of gray shades
- Task is to match gray levels
  - average luminance in the scene is perceived as a gray shade of medium brightness
  - such luminance is mapped on medium brightness of a display
  - the rest is mapped proportionally
- Practically adjusts brightness
  - sort of like using gray card or auto-exposure in photography
  - goal of adaptation processes in human vision
- Adapting luminance exists in many TM algorithms

$$Y_A = \exp\left(\frac{\sum \log(Y + \varepsilon)}{N} - \varepsilon\right)$$



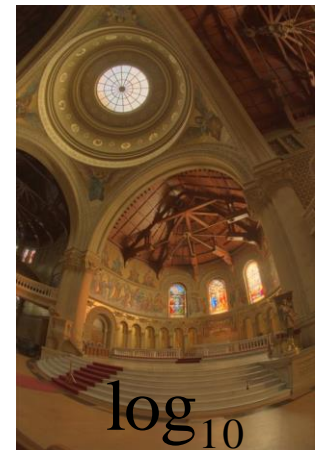
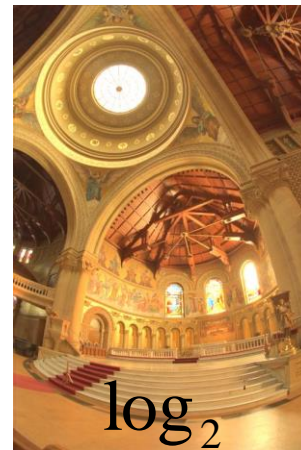
# Logarithmic Tone Mapping

- Logarithm is a crude approximation of brightness
- Change of base for varied contrast mapping in bright and dark areas
  - $\log_{10}$  maps better for bright areas
  - $\log_2$  maps better for dark areas
- Mapping parameter *bias* in range 0.1:1

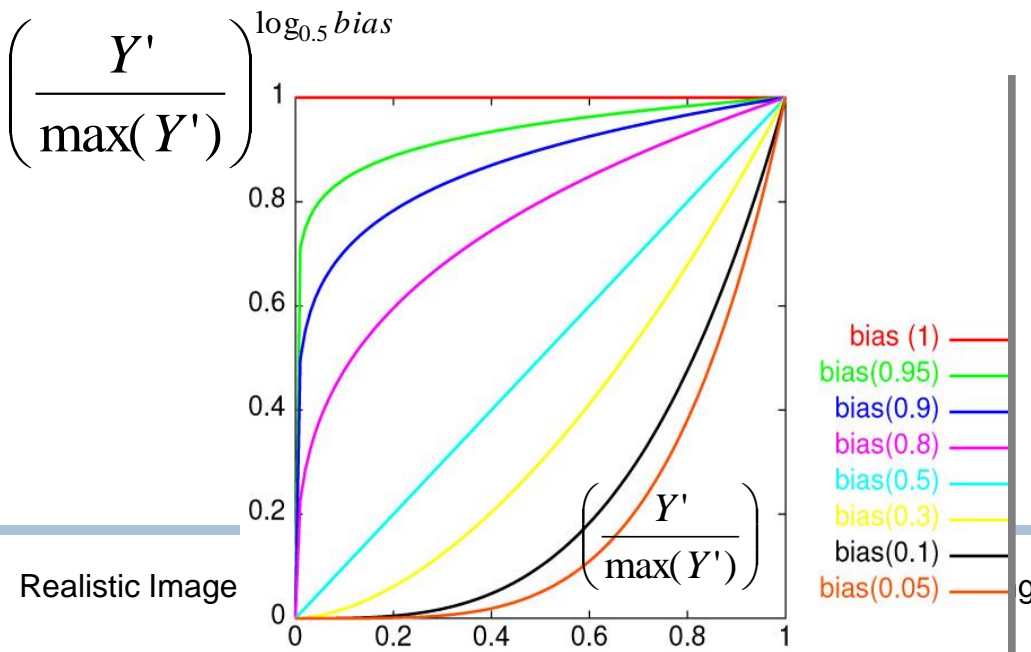
$$Y' = \frac{Y}{Y_A}$$

$$L = L_{\max} \cdot \frac{\log_{base(Y)}(Y'+1)}{\log_{10}(\max(Y') + 1)}$$

$$base(Y') = 2 + 8 \cdot \left( \frac{Y'}{\max(Y')} \right)^{\log_{0.5} bias}$$



# Logarithmic Tone Mapping



- These images illustrate how high luminance values are clamped to the maximum displayable values using different bias parameter values.
- The scene dynamic range is 1:11,751,307.

# Sigmoid Response

- Model of photoreceptor

$$L = \frac{Y}{Y + (f \cdot Y_A)^m} L_{\max}$$

- Brightness parameter  $f$
- Contrast parameter  $m$
- Adapting luminance  $Y_A$ 
  - average in an image
  - measured pixel (equal to  $Y$ )



logarithmic mapping



sigmoid mapping

# Histogram Equalization (1)

- Adapts transfer function to distribution of luminance in the image
- Algorithm:
  - compute histogram
  - compute transfer function (cumulative distribution)
  - limit slope of transfer function to prevent contouring
    - contouring – visible difference between 1 quantization step
    - use threshold versus intensity function (TVI)
      - TVI gives visible luminance difference for adapting luminance
- Most optimal transfer function
- Not efficient when large uniform areas are present in the image

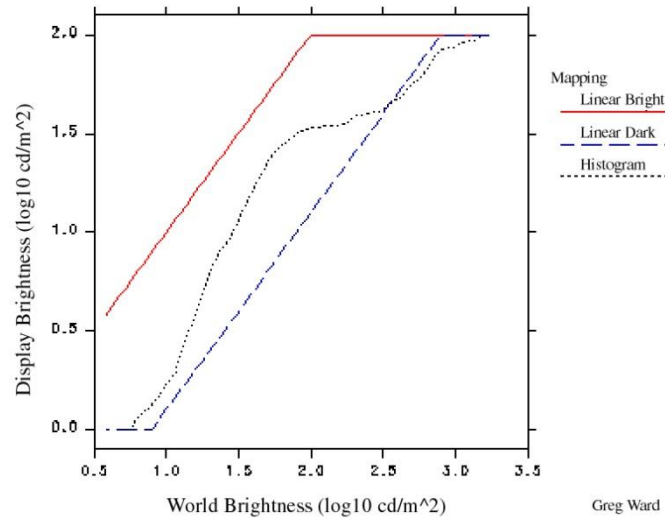
# Histogram Equalization (2)

## World to Display Luminance Mapping



A linear mapping of the luminances that overexposes the view through the window.

Greg Ward



A linear mapping of the luminances that underexposes the view of the interior.

Greg Ward



The luminances mapped to preserve the visibility of both indoor and outdoor features.

# Transfer Functions Compared



linear —



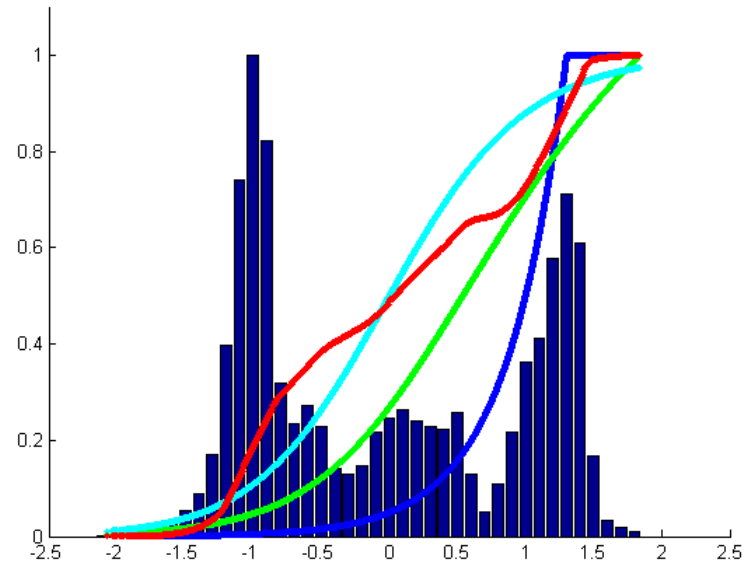
logarithmic —



photoreceptor —



histogram eq. —



- Interpretation
  - steepness of slope is contrast
  - luminance for which output is  $\sim 0$  and  $\sim 1$  is not transferred
- Usually low contrast for dark and bright areas!

# Problem with Details



- Strong compression of contrast puts micro-contrasts (details) below quantization level

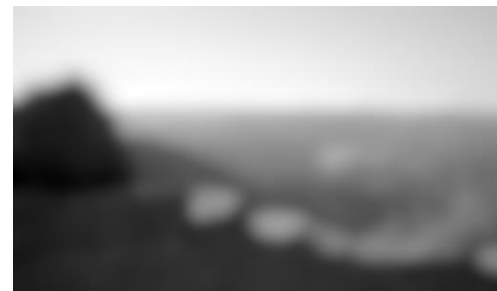
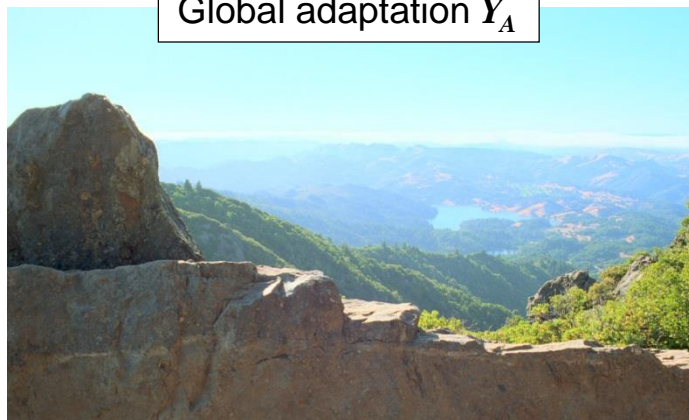
# Introducing Local Adaptation

- Eye adapts locally to observed area

$$L = \frac{Y'}{Y'+1} \leftarrow Y' = \frac{Y}{Y_A} \rightarrow L = \frac{Y'}{Y_L'+1}$$

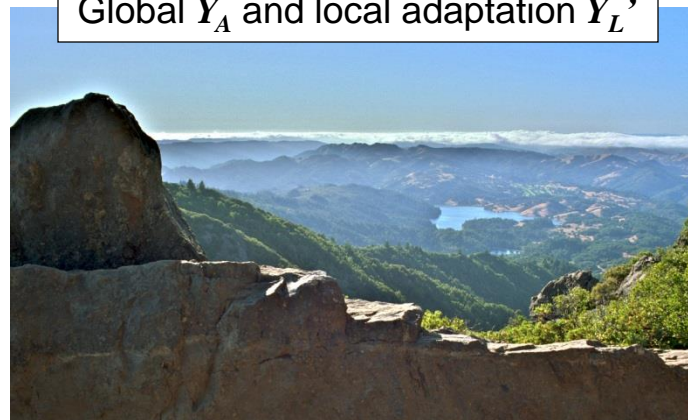


Global adaptation  $Y_A$



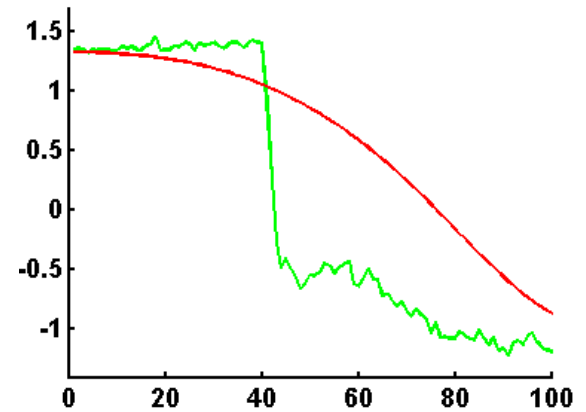
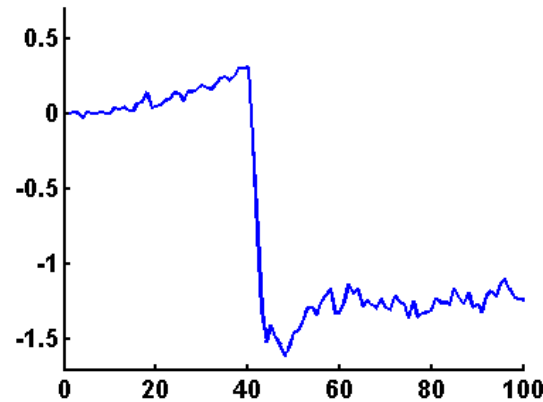
Gaussian blur of HDR image,  $\sigma \sim 1$ deg of visual angle.

Global  $Y_A$  and local adaptation  $Y_L'$





# The Halo Artifact

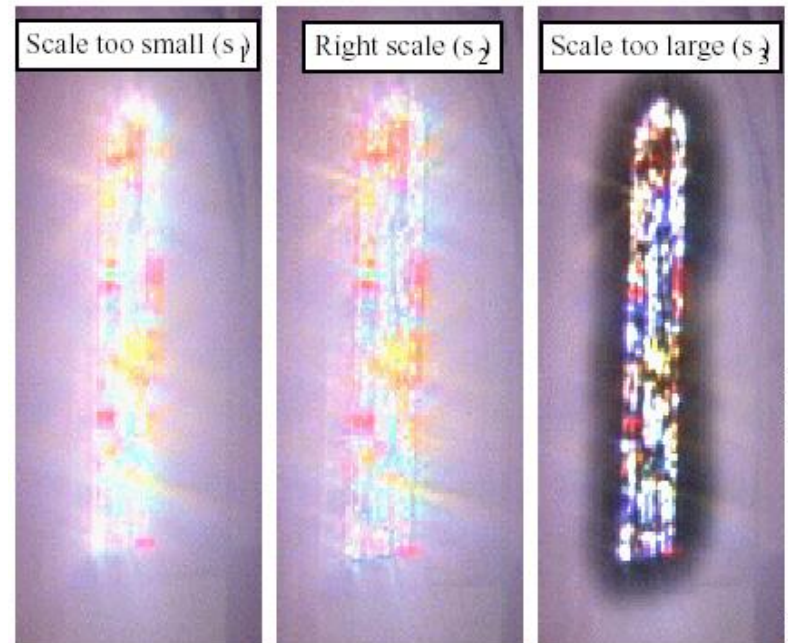
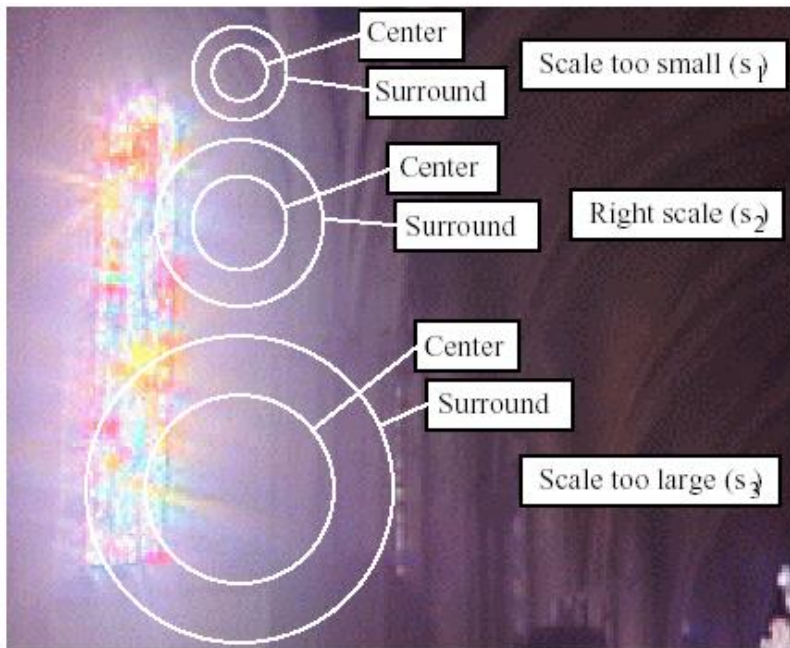


- Scan line example:
  - Gaussian blur under- (over-) estimates **local adaptation** near a **high contrast edge**
  - **tone mapped image** gets too bright (too dark) closer to such an edge
- Smaller blur kernel reduces the artifact (but then no details)
- Larger blur kernel spreads the artifact on larger area

# Adjusting Gaussian Blur

- So called: Automatic Dodging and Burning
  - for each pixel, test increasing blur size  $\sigma_i$
  - choose the largest blur which does not show halo artifact

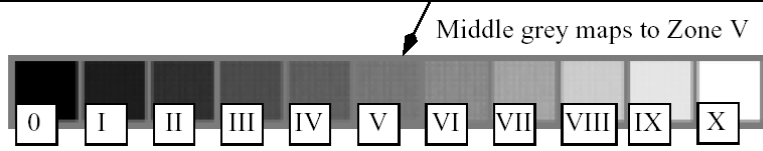
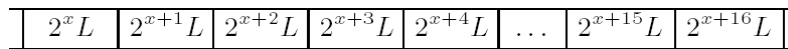
$$\left| Y_L(x, y, \sigma_i) - Y_L(x, y, \sigma_{i+1}) \right| < \varepsilon$$



Radiance map courtesy of Paul Debevec

# Photographic Tone Reproduction

- Map luminance using Zone System



Print zones: Zone V 18% reflectance

$$Y' = \frac{Y}{Y_A}, \quad Y_A = \exp\left(\frac{\sum \log(Y)}{N}\right)$$

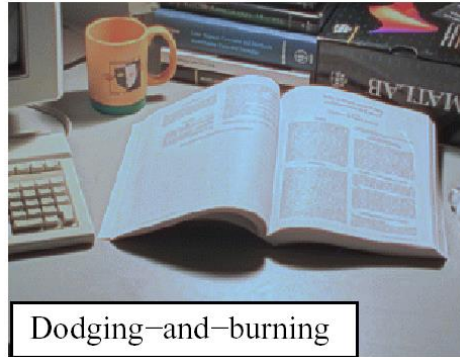
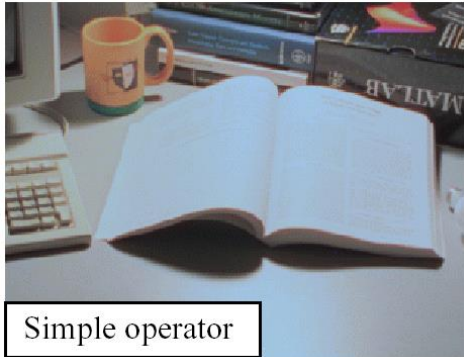
- Find local adaptation for each pixel
  - appropriate size of Gaussian (automatic dodging & burning)

$$\left| Y_L'(x, y, \sigma_i) - Y_L'(x, y, \sigma_{i+1}) \right| < \varepsilon$$

- Tone map using sigmoid function
  - different blur levels from Gaussian pyramid

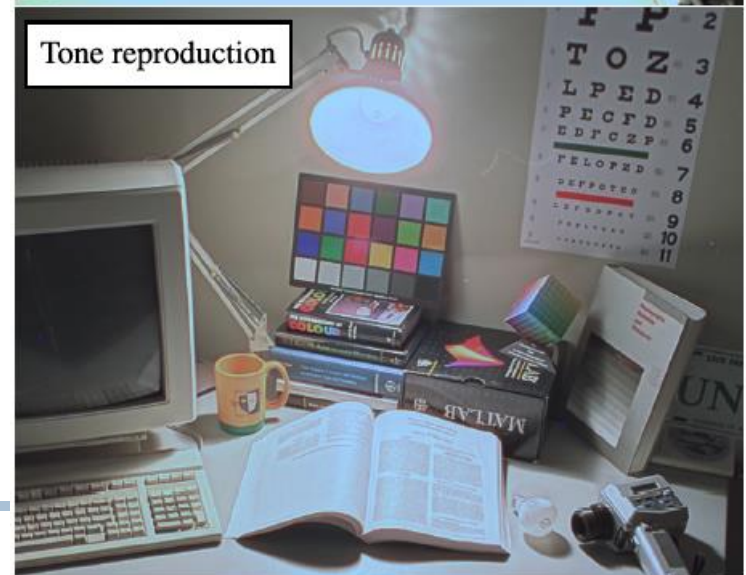
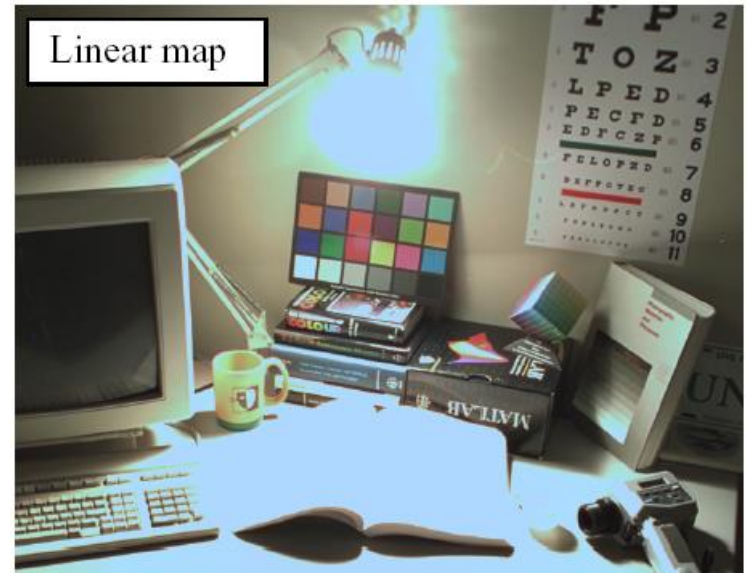
$$L(x, y) = \frac{Y'(x, y)}{Y_L'(x, y, \sigma_{x,y}) + 1}$$

# Photographic Tone Reproduction



- dodge** luminance of pixels in bright regions is significantly decreased
- burn** pixels in dark regions are compressed less, so their relative intensity increases

Automatic dodging-and-burning technique is more effective in preserving local details (notice the print in the book).

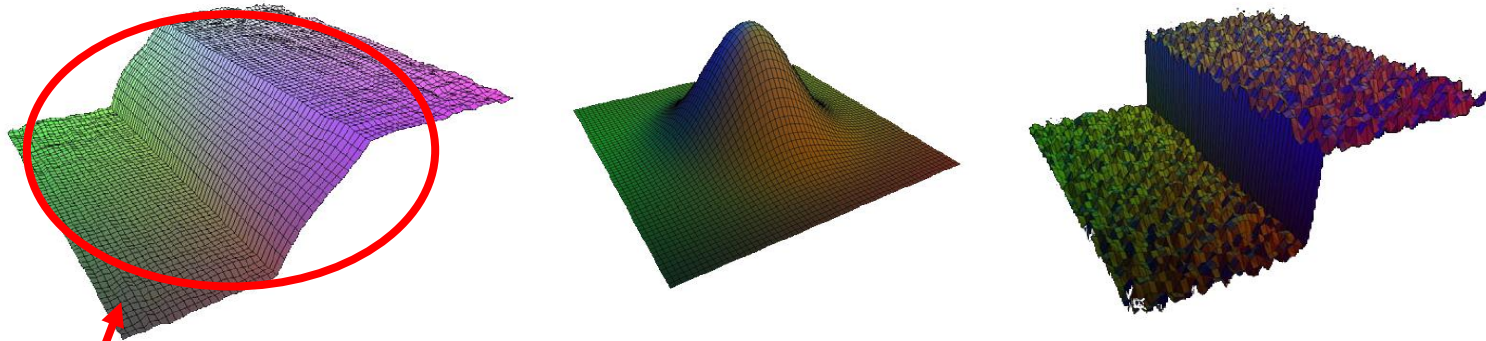


# Bilateral Filtering

- Edge preserving Gaussian filter to prevent halo
- Conceptually based on intrinsic image models:
  - decoupling of illumination and reflectance layers
    - very simple task in CG
    - complicated for real-world scenes
  - compress range of illumination layer
  - preserve reflectance layer (details)
- Bilateral filter separates:
  - texture details (high frequencies, low amplitudes)
  - illumination (low frequencies, high contrast edges)

# Illumination Layer (1)

- Identify low frequencies in the scene
  - Gaussian filtering leads to halo artifacts



$$J_p = \frac{1}{W_p} \sum_{q \in N(p)} f_{\sigma_s}(\|p - q\|) \cdot I_q$$

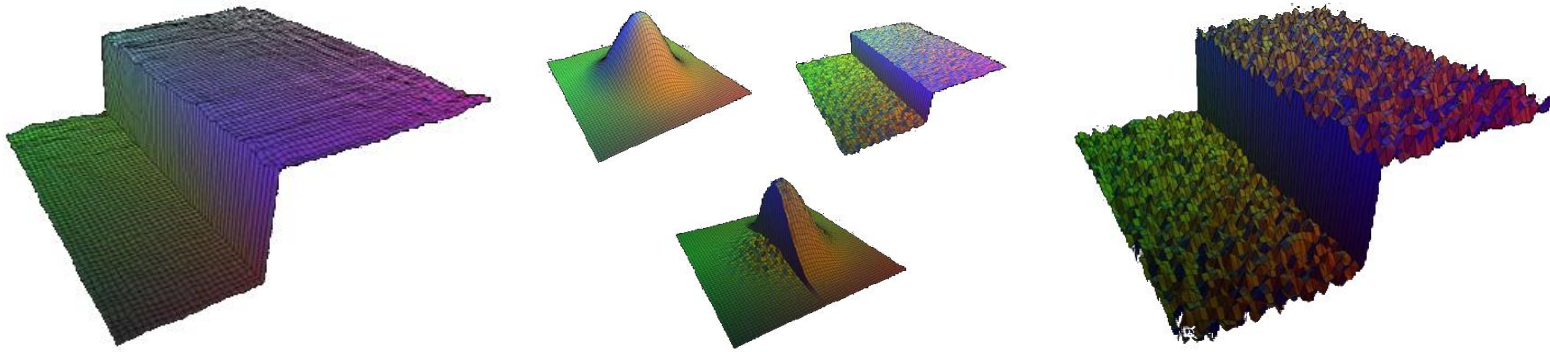
$f$  spatial kernel with large  $\sigma_s$

lost sharp edge



# Illumination Layer (2)

- Edge preserving filter – no halo artifacts



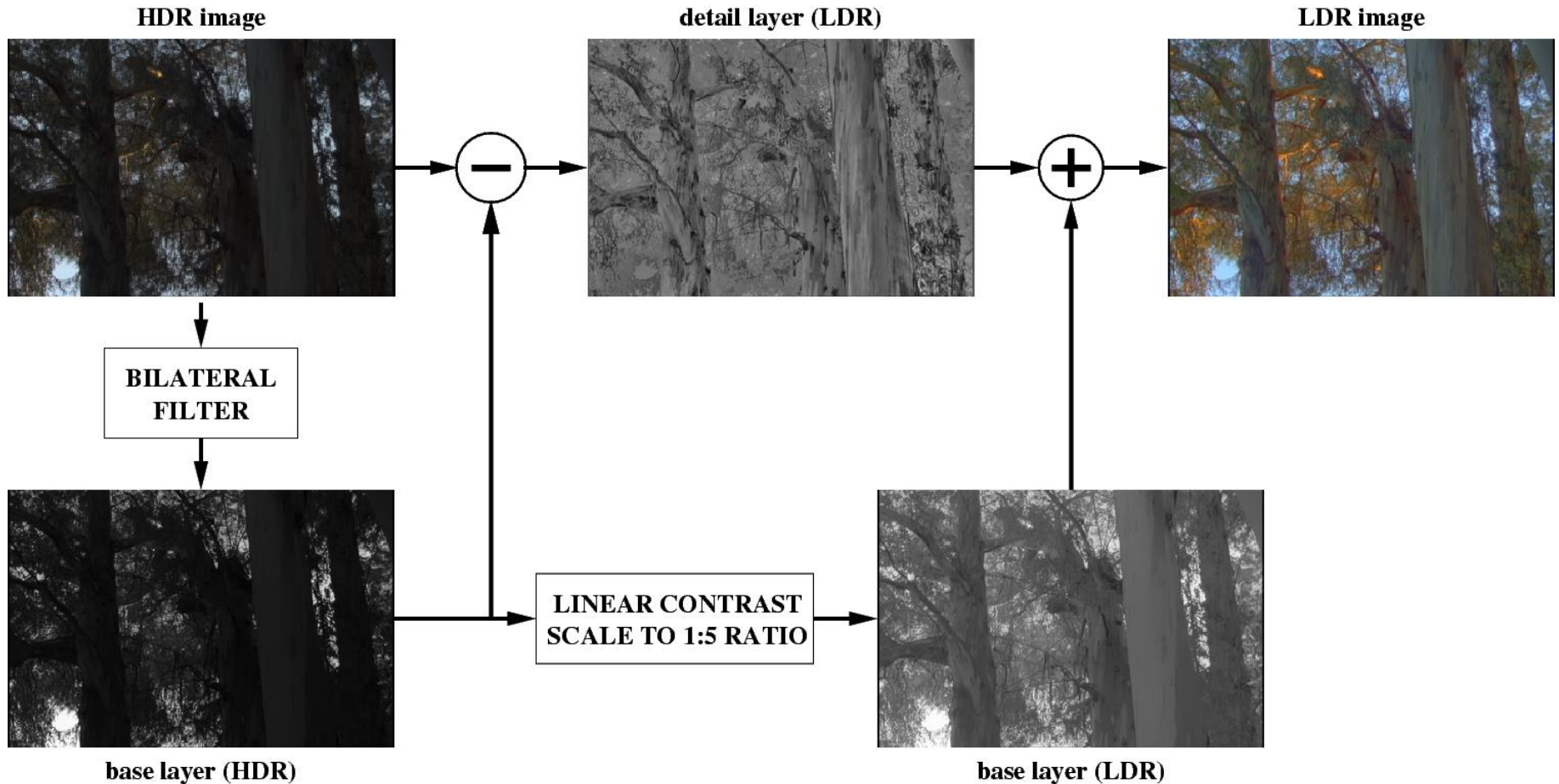
$$J_p = \frac{1}{W_p} \sum_{q \in N(p)} f_{\sigma_s}(\|p - q\|) \cdot g_{\sigma_r}(|I_p - I_q|) \cdot I_q$$

$f$  spatial kernel with large  $\sigma_s$

$g$  range kernel with very small  $\sigma_r$



# Tone Mapping Algorithm



Luminance in logarithmic domain.

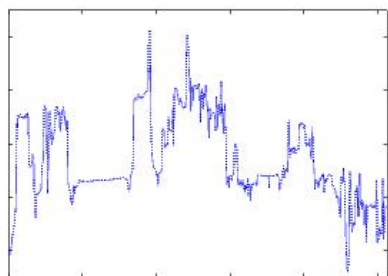


# Illumination & Reflectance

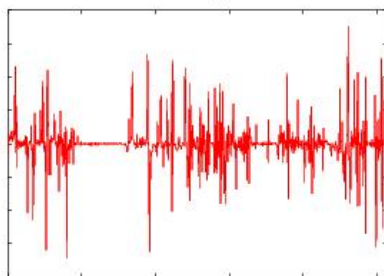


# Gradient Compression Algorithm

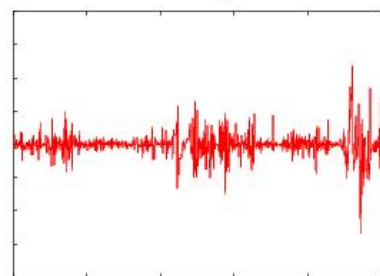
HDR scanline



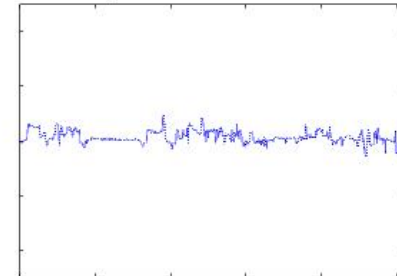
luminance gradients



attenuated gradients



compressed scanline



$$H = \log L$$

$\downarrow$   
 $H(x, y)$



$$\nabla H(x, y)$$

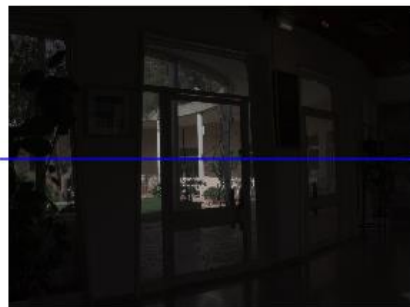


$$G(x, y) = \nabla H(x, y) * \Phi(x, y)$$



$$\nabla^2 I = \text{div } G$$

$$\downarrow L_d = \exp I$$



HDR scene

luminance gradients' map

attenuation map

compressed image

1. Calculate gradients map of image
2. Calculate attenuation map

3. Attenuate gradients
4. Solve Poisson equation to recover image

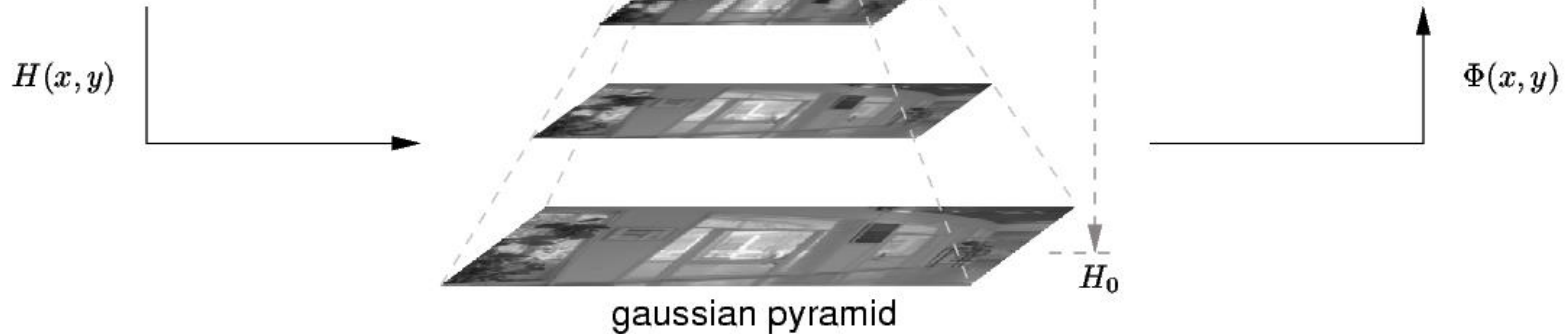
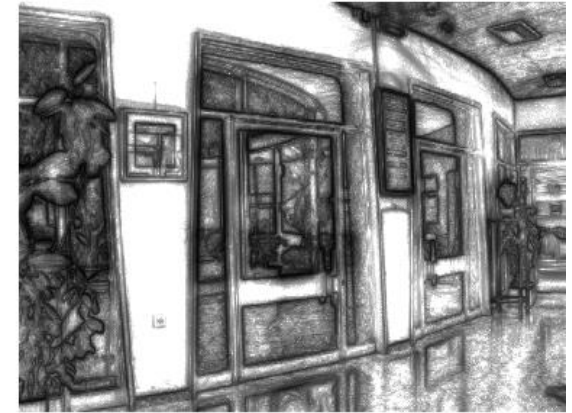
# Attenuation Map

HDR scene



$$\varphi_k(\mathbf{x}, \mathbf{y}) = \frac{\alpha}{\|\nabla \mathbf{H}_k(\mathbf{x}, \mathbf{y})\|} * \left( \frac{\|\nabla \mathbf{H}_k(\mathbf{x}, \mathbf{y})\|}{\alpha} \right)^\beta$$

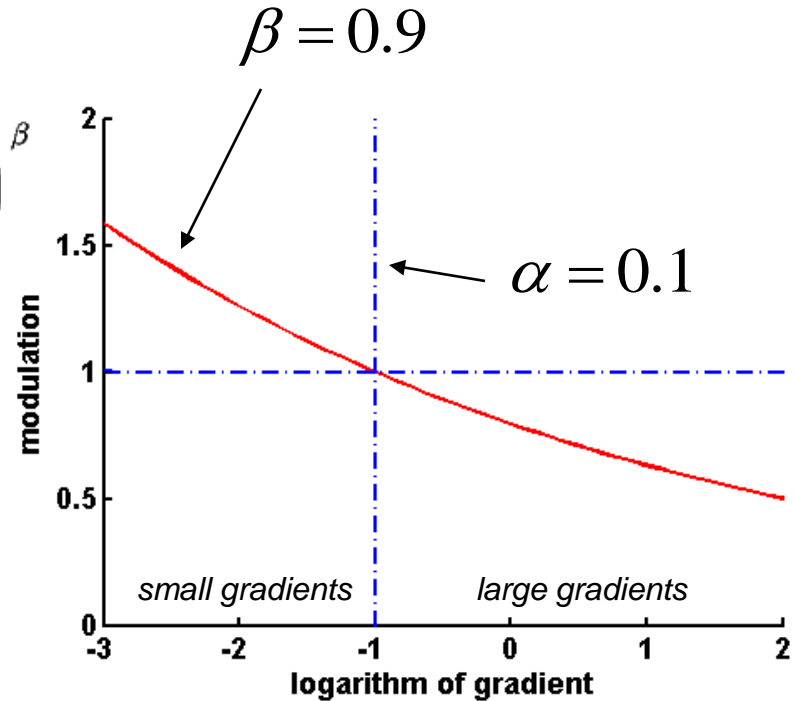
attenuation map



1. Create Gaussian pyramid
2. Calculate gradients on levels
3. Calculate attenuation on levels -  $\varphi_k$
4. Propagate levels to full resolution

# Transfer Function for Contrasts

$$\varphi_{\mathbf{k}}(\mathbf{x}, \mathbf{y}) = \frac{\alpha}{\|\nabla \mathbf{H}_{\mathbf{k}}(\mathbf{x}, \mathbf{y})\|} * \left( \frac{\|\nabla \mathbf{H}_{\mathbf{k}}(\mathbf{x}, \mathbf{y})\|}{\alpha} \right)^{\beta}$$



- Attenuate large gradients
  - presumably illumination
- Amplify small gradients
  - hopefully texture details
  - but also noise
- Equation has a division by zero!

# Global vs. Local Compression

Adaptive Logarithmic Mapping



- Loss of overall contrast
- Loss of texture details
- Real-time even on CPU
- Simple GPU implementation

Gradient Domain Compression



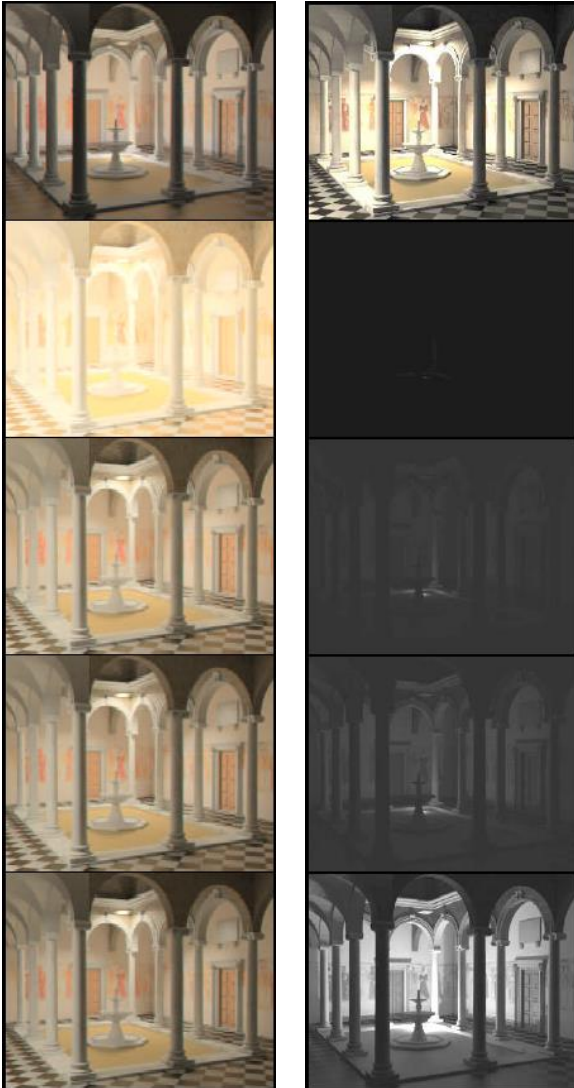
- Impression of high contrast
- Good preservation of fine details
- Solving Poisson equation takes time
- On GPU ~10fps still possible

# Perceptual Effects in TM

- Simulate effects that do not appear on a screen but are typically observed in real-world scenes
  - veiling glare
  - night vision
  - temporal adaptation to light
- Increase believability of results, because we associate such effects with luminance conditions



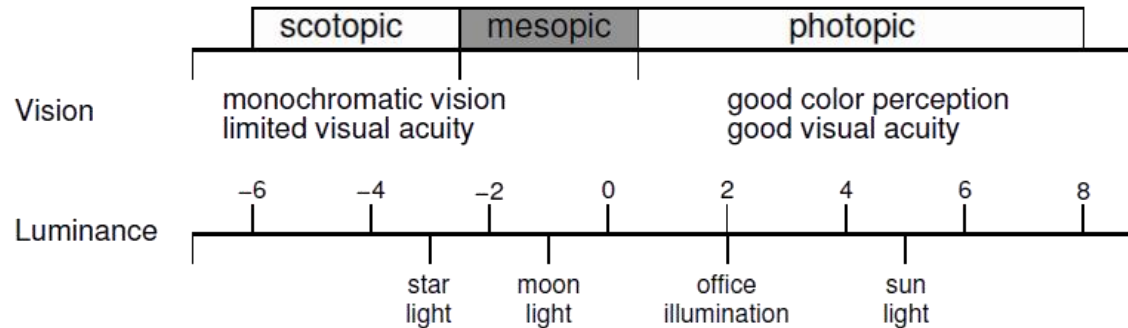
# Temporal Luminance Adaptation



- Compensates changes in illumination
- Simulated by smoothing adapting luminance in tone mapping equation
- Different speed of adaptation to light and to darkness

# Night Vision

- Human Vision operates in three distinct adaptation conditions:





# Visual Acuity

- Perception of spatial details is limited with decreasing illumination level
- Details can be removed using convolution with a Gaussian kernel
- Highest resolvable spatial frequency:

$$RF(Y) = 17.25 \cdot \arctan(1.4 \log_{10} Y + 0.35) + 25.72$$

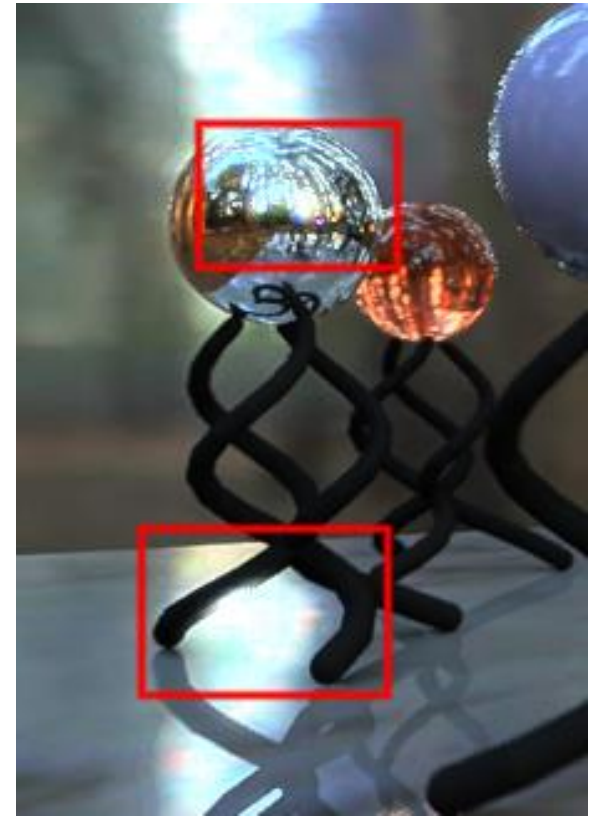
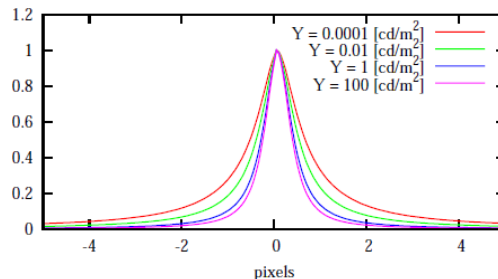


# Veiling Luminance (Glare)

- Decrease of contrast and visibility due to light scattering in the optical system of the eye
- Described by the optical transfer function:

$$OTF(\rho, d(\bar{Y})) = \exp\left(-\frac{\rho}{20.9 - 2.1 \cdot d}^{1.3 - 0.07 \cdot d}\right)$$

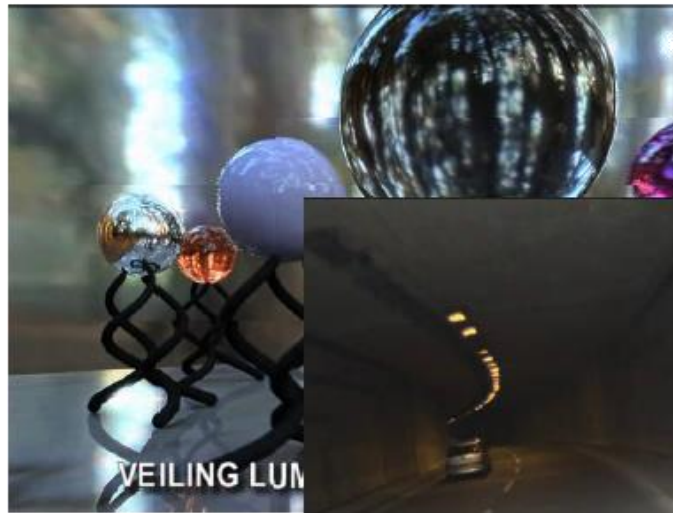
$\rho$  spatial frequency,  $d$  pupil aperture



# Fast TM on GPU

- Simple transfer function is very fast
- What about those advanced algorithms
  - bilateral: fast approximate algorithms available
  - gradient domain: GPU needs ~1s per 1MPx
- Real-time?
  - automatic dodging & burning
  - Gaussian pyramid can be built fast on GPU
  - the pyramid can be used to add perceptual effects at no additional cost!

# HDR Video Player with Perceptual Effects



# Papers about Calibration

- Estimation-Theoretic Approach to Dynamic Range Improvement Using Multiple Exposures
  - M. Robertson, S. Borman, and R. Stevenson
  - In: Journal of Electronic Imaging, vol. 12(2), April 2003.
- Recovering High Dynamic Range Radiance Maps from Photographs
  - Paul E. Debevec and Jitendra Malik
  - In: SIGGRAPH 97
- Radiometric Self Calibration
  - T. Mitsunaga and S.K. Nayar
  - In: Computer Vision and Pattern Recognition (CVPR), 1999.
- High Dynamic Range from Multiple Images: Which Exposures to Combine?
  - M.D. Grossberg and S.K. Nayar
  - In: ICCV Workshop on Color and Photometric Methods in Computer Vision (CPMCV), 2003.

# Papers about Tone Mapping

- Adaptive Logarithmic Mapping for Displaying High Contrast Scenes
  - F. Drago, K. Myszkowski, T. Annen, and N. Chiba
  - In: Eurographics 2003
- Photographic Tone Reproduction for Digital Images
  - E. Reinhard, M. Stark, P. Shirley, and J. Ferwerda
  - In: SIGGRAPH 2002 (ACM Transactions on Graphics)
- Fast Bilateral Filtering for the Display of High-Dynamic-Range Images
  - F. Durand and J. Dorsey
  - In: SIGGRAPH 2002 (ACM Transactions on Graphics)
- Gradient Domain High Dynamic Range Compression
  - R. Fattal, D. Lischinski, and M. Werman
  - In: SIGGRAPH 2002 (ACM Transactions on Graphics)
- Dynamic Range Reduction Inspired by Photoreceptor Physiology
  - E. Reinhard and K. Devlin
  - In IEEE Transactions on Visualization and Computer Graphics, 2005
- Time-Dependent Visual Adaptation for Realistic Image Display
  - S.N. Pattanaik, J. Tumblin, H. Yee, and D.P. Greenberg
  - In: Proceedings of ACM SIGGRAPH 2000
- Lightness Perception in Tone Reproduction for High Dynamic Range Images
  - G. Krawczyk, K. Myszkowski, H.-P. Seidel
  - In: Eurographics 2005
- Perceptual Effects in Real-time Tone Mapping
  - G. Krawczyk, K. Myszkowski, H.-P. Seidel
  - In: Spring Conference on Computer Graphics, 2005

# Acknowledgements

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