

# Denoising Algorithms: Path to Neural Networks III



Image courtesy Vogel et al. [2018], Gharbi et al. [2019]

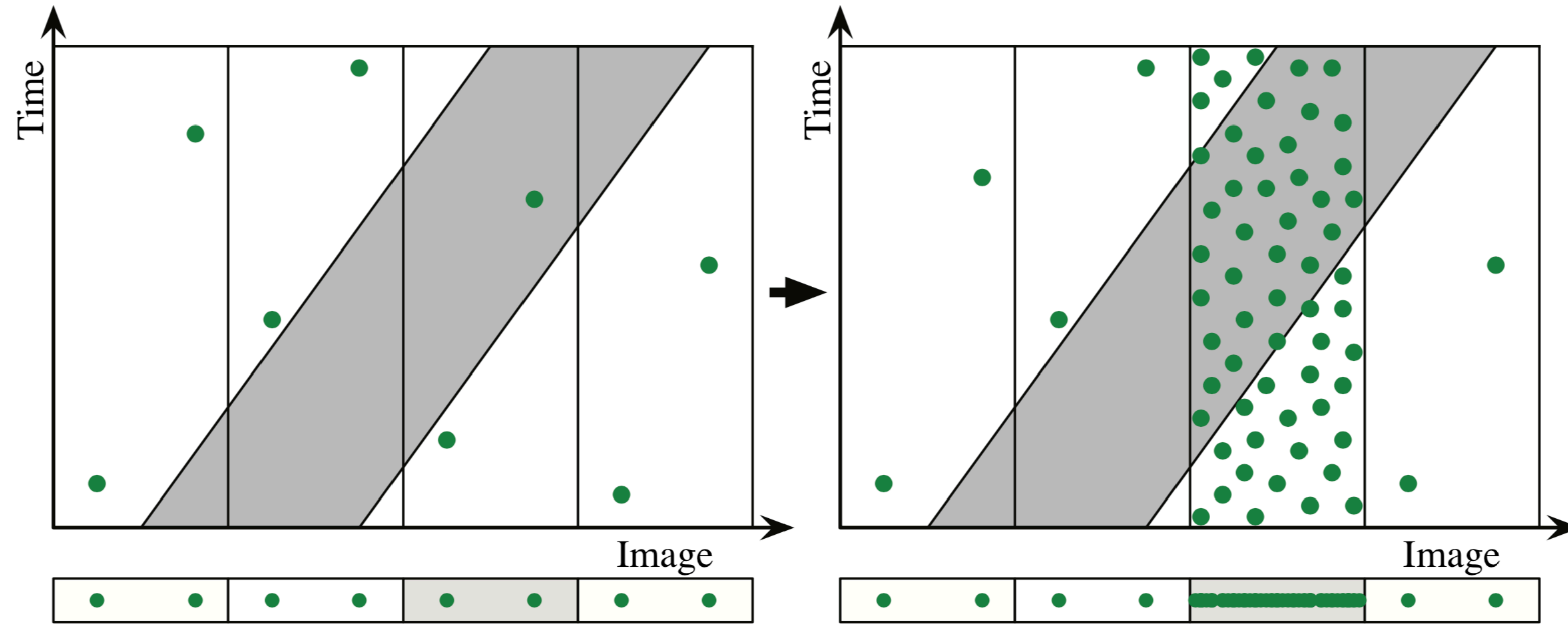
*Philipp Slusallek*   *Karol Myszkowski*   ***Gurprit Singh***

# Final Exam

20.08.19 from 10:00 to 13:00 in HS 002

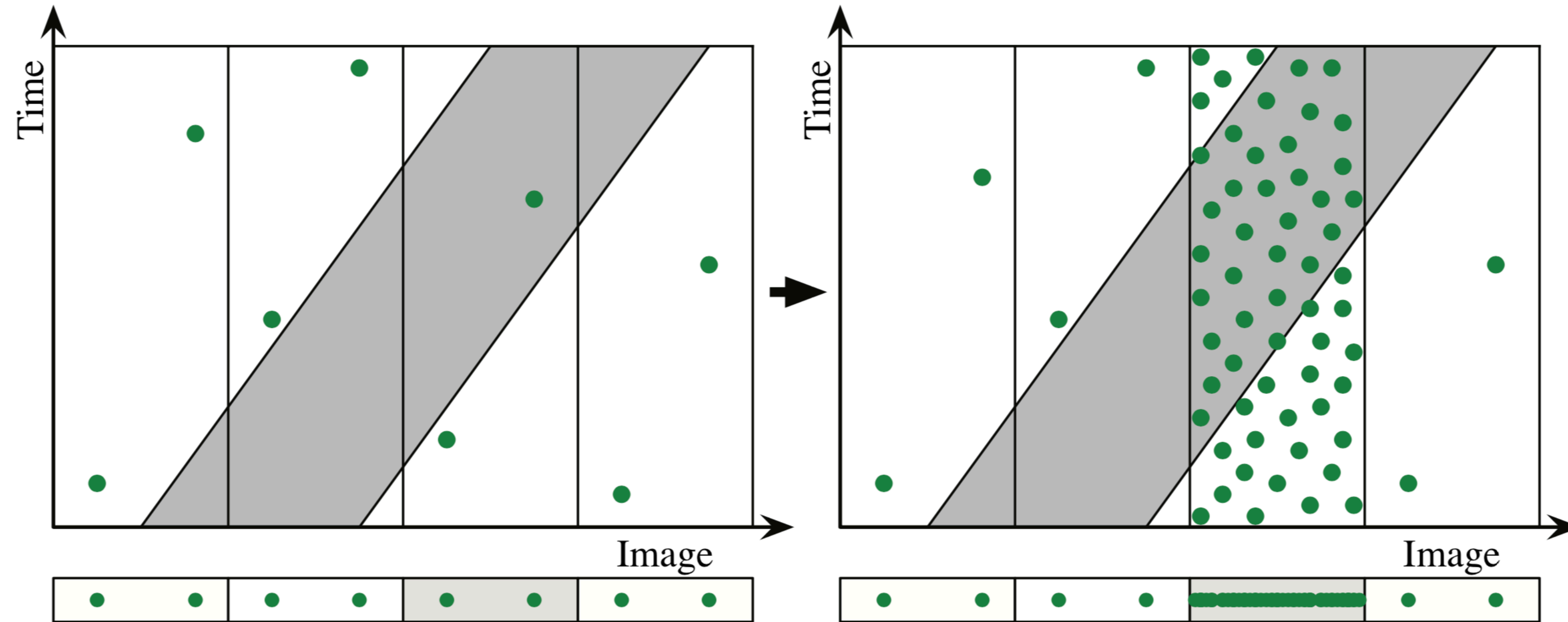
# Recap

# Image-space Adaptive Sampling



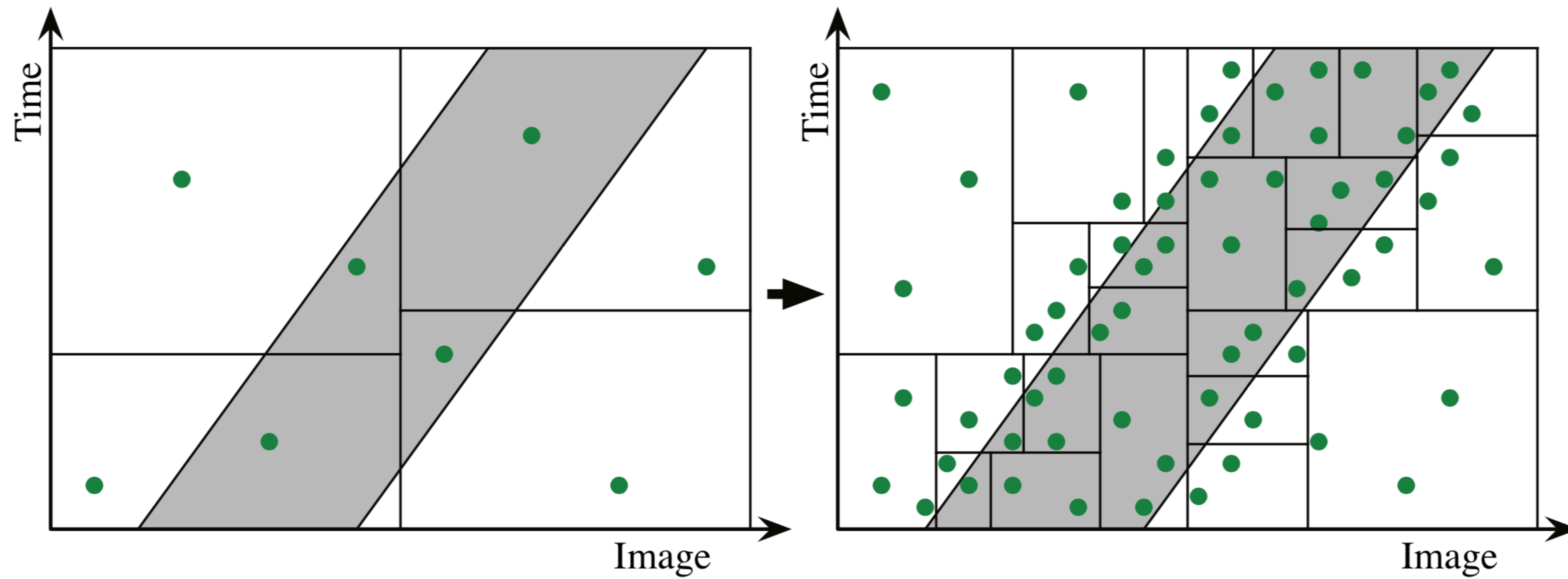
Hachisuka et al. [2008]

# Image-space Adaptive Sampling

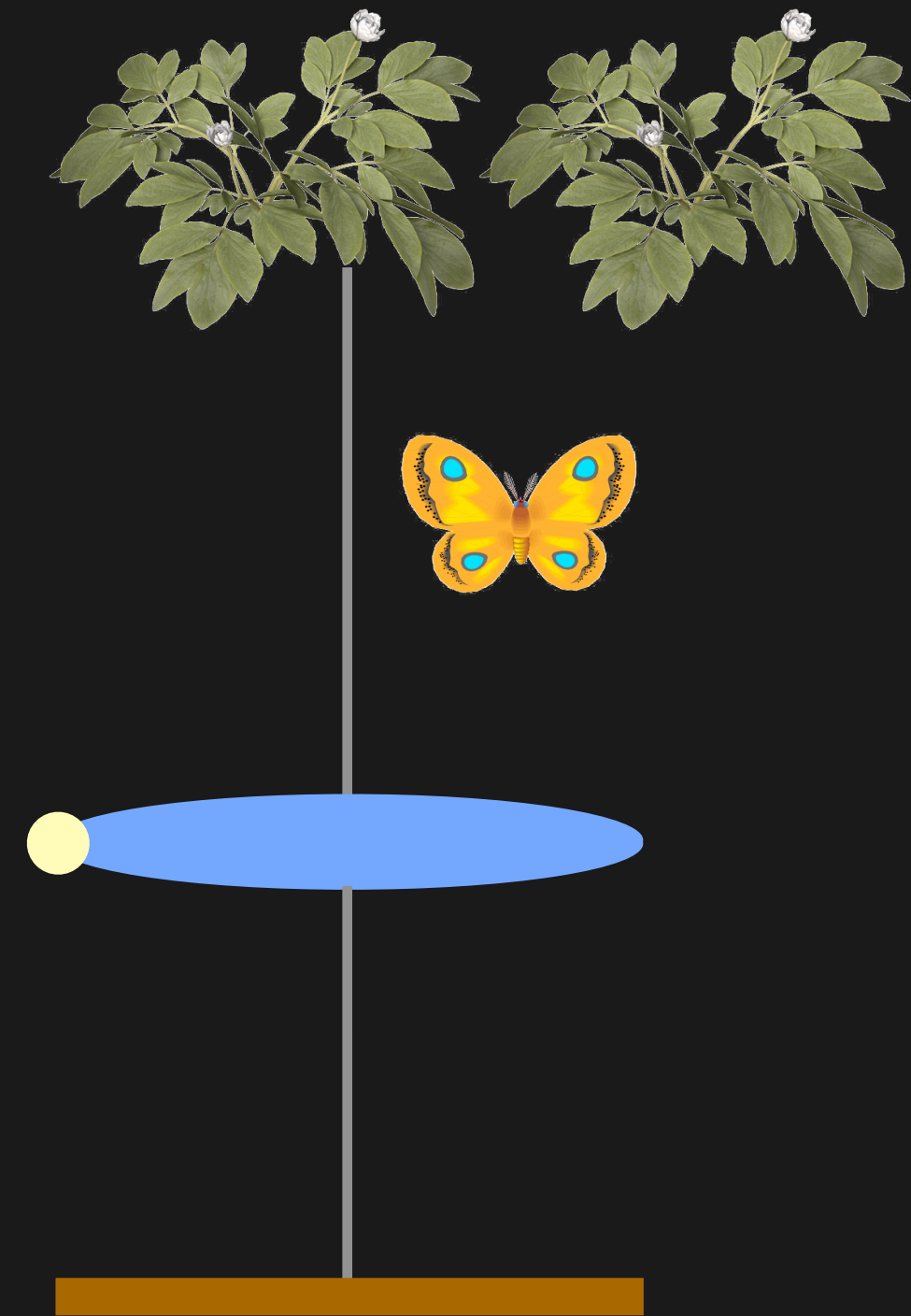


Hachisuka et al. [2008]

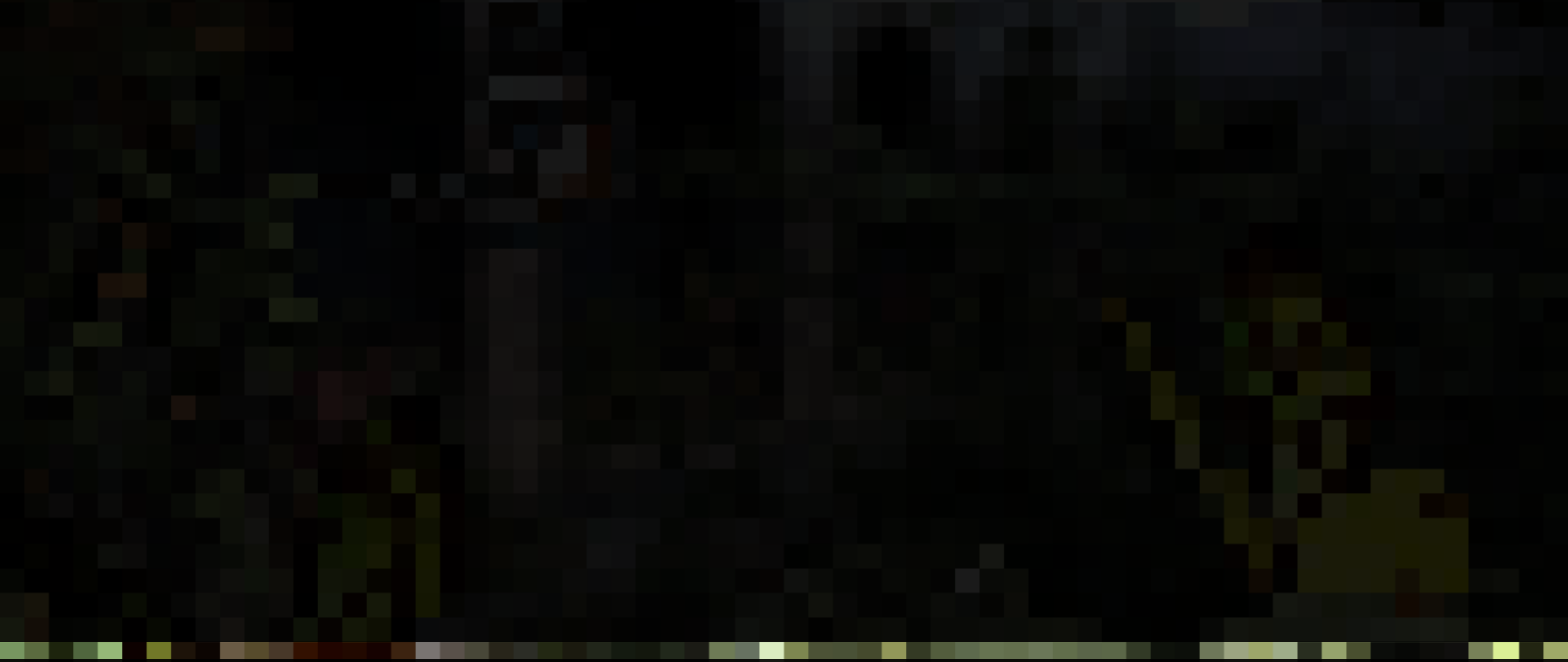
# Multidimensional Adaptive Sampling



# Depth of field

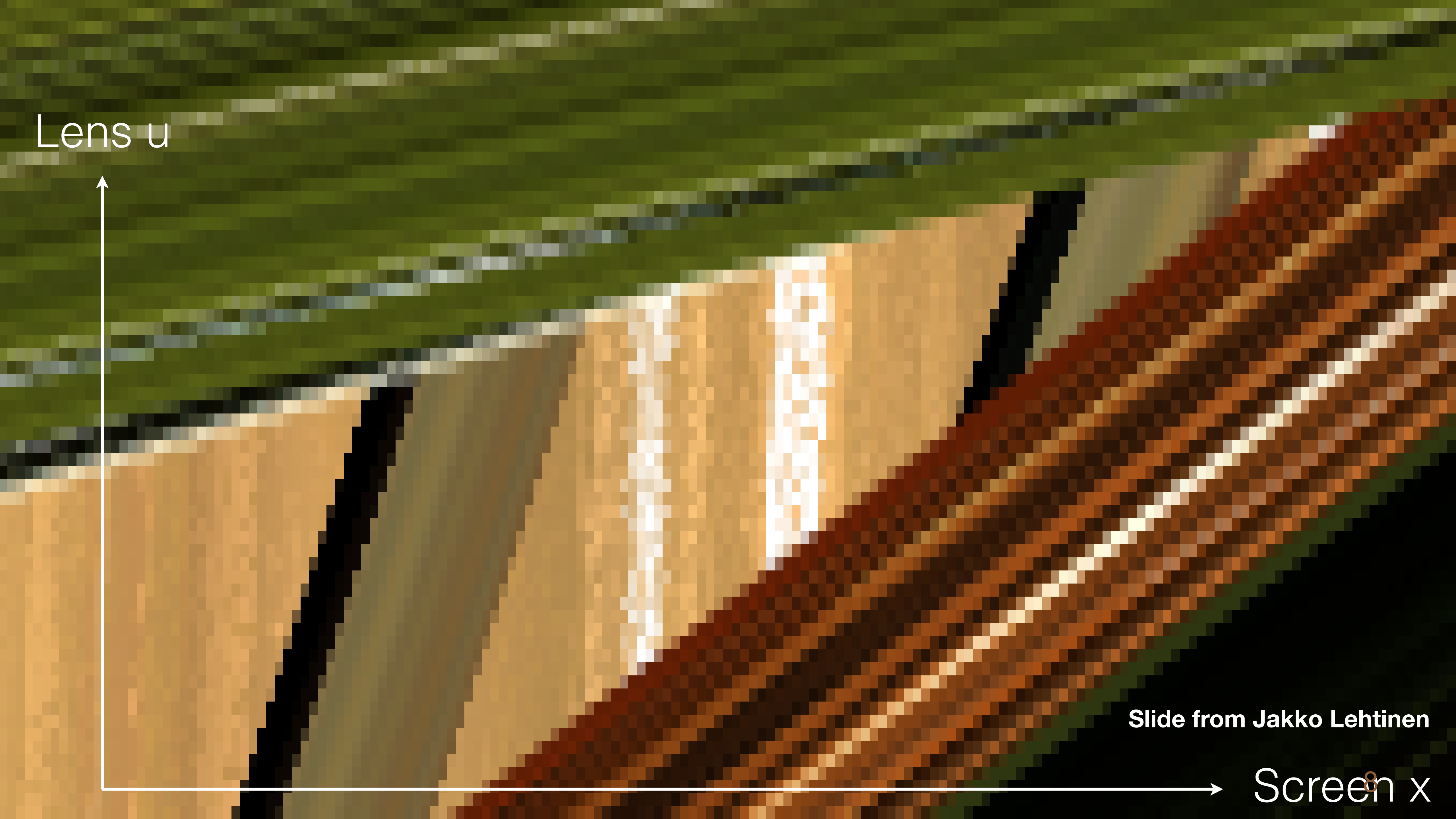


Slide from Jakko Lehtinen



1 scanline

Slide from Jakko Lehtinen



Lens  $u$

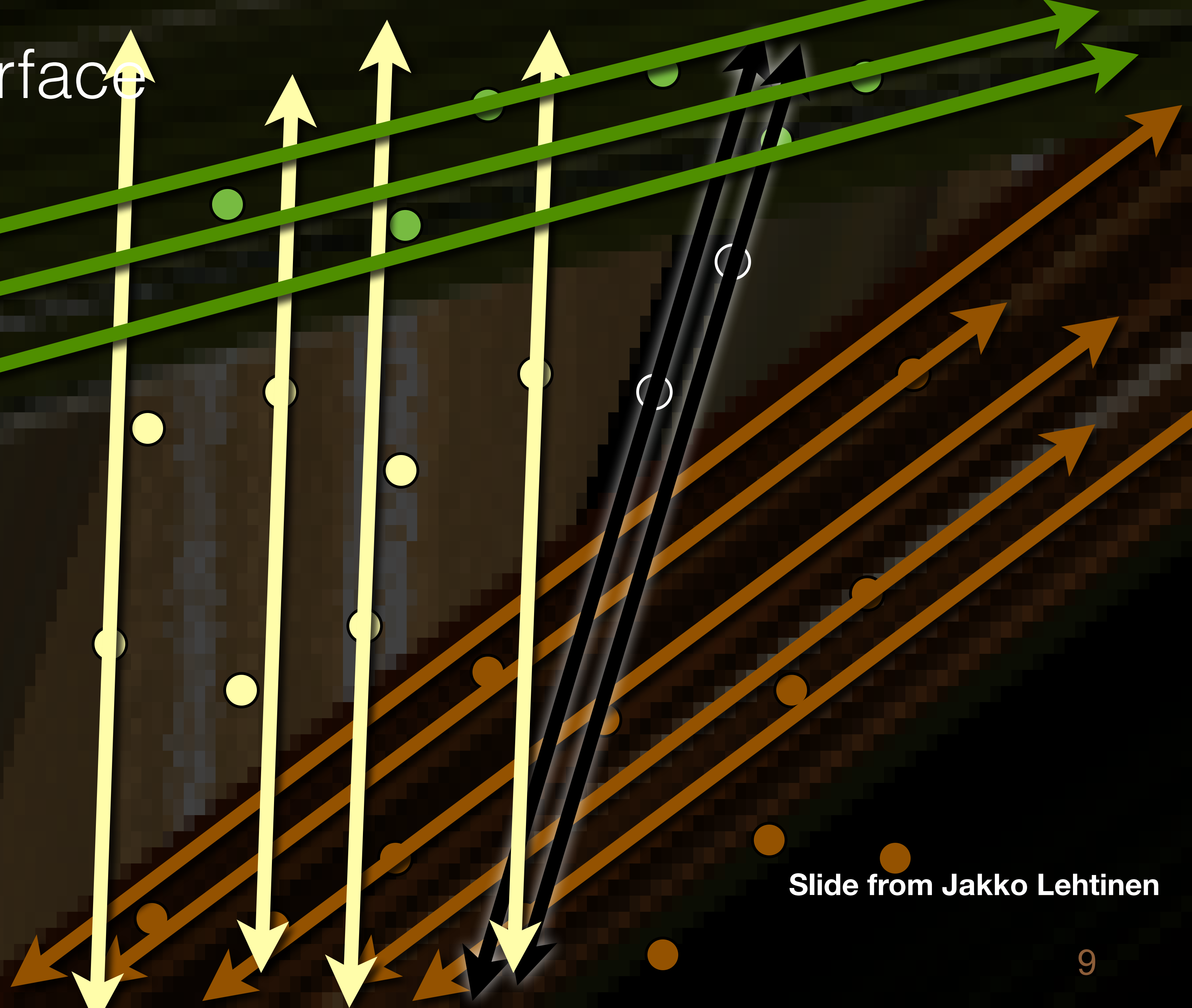
Slide from Jakko Lehtinen

Screen  $x$



# Visibility: SameSurface

The trajectories of samples originating from a single **apparent surface** never intersect.



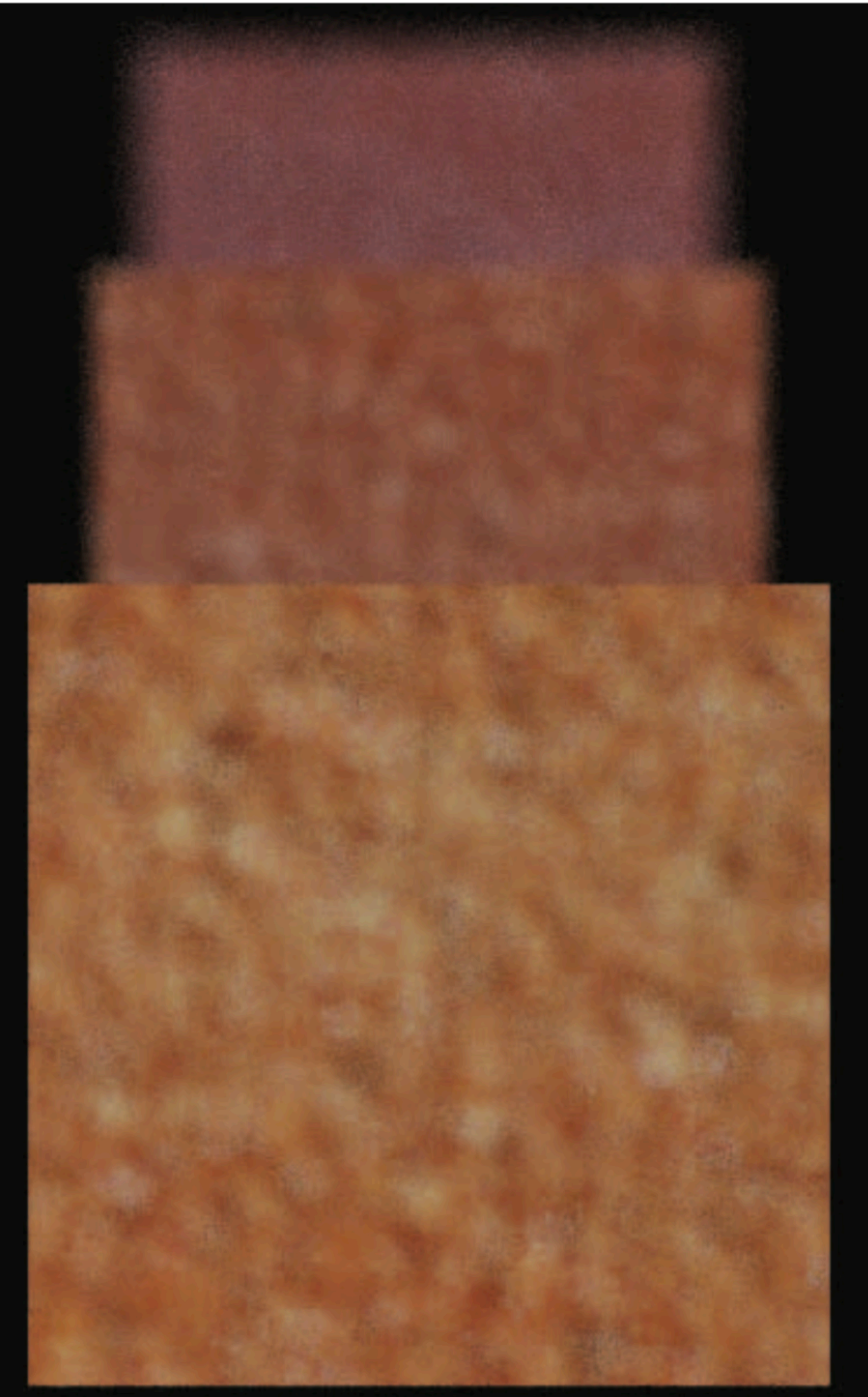
Slide from Jakko Lehtinen



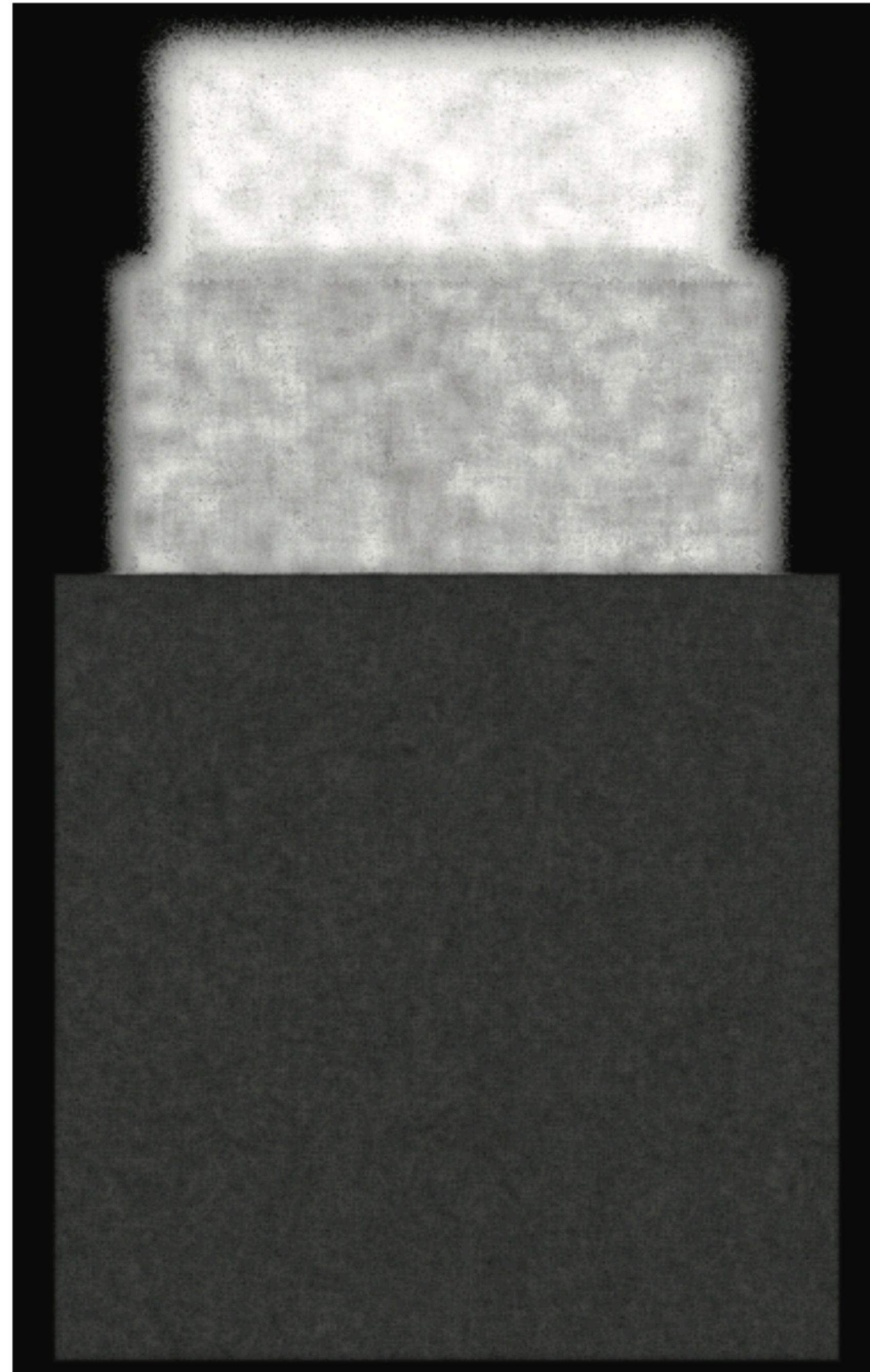
input Monte Carlo (8 samples/pixel)



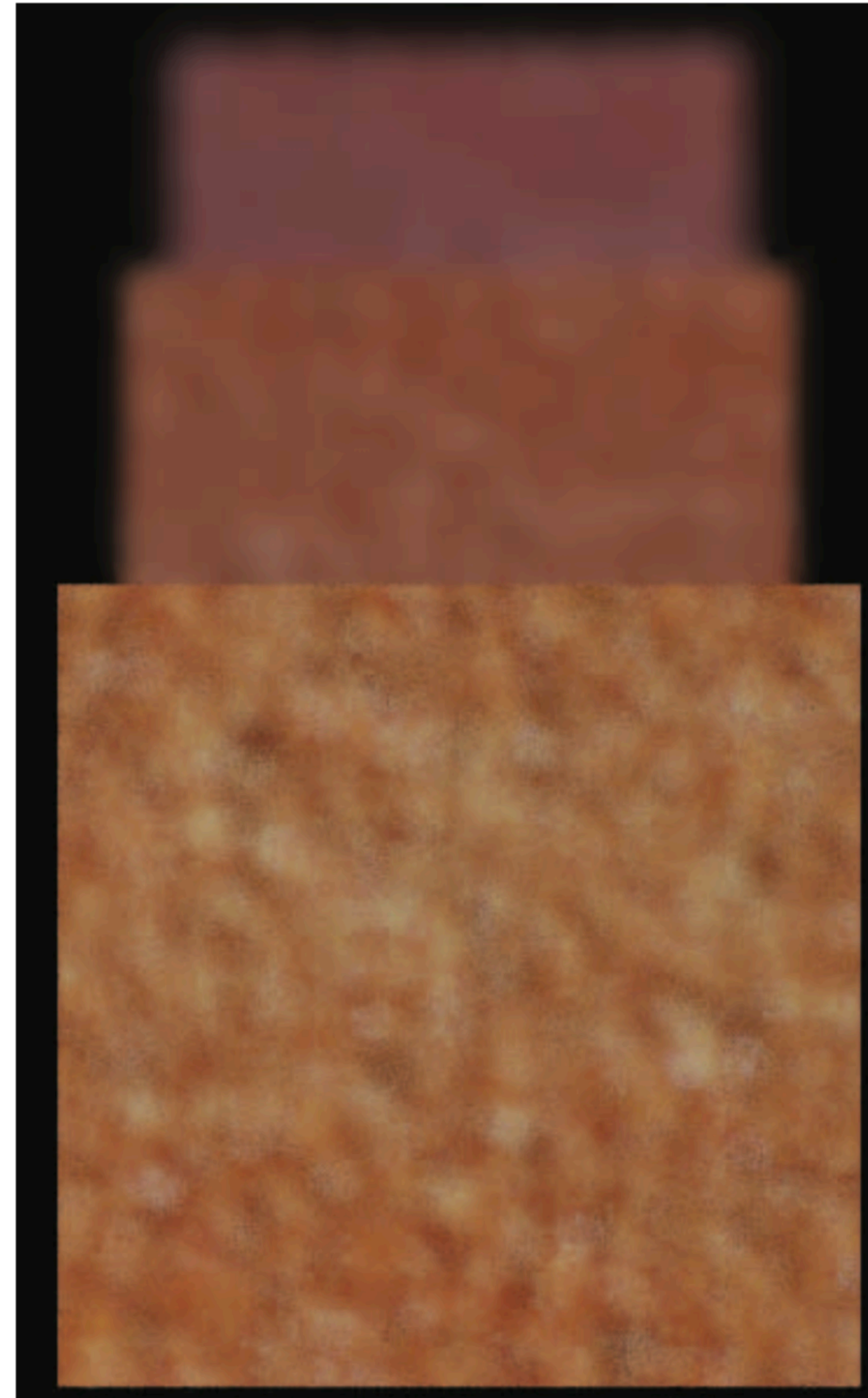
after RPF (8 samples/pixel)



**(a)** Input MC (8 spp)

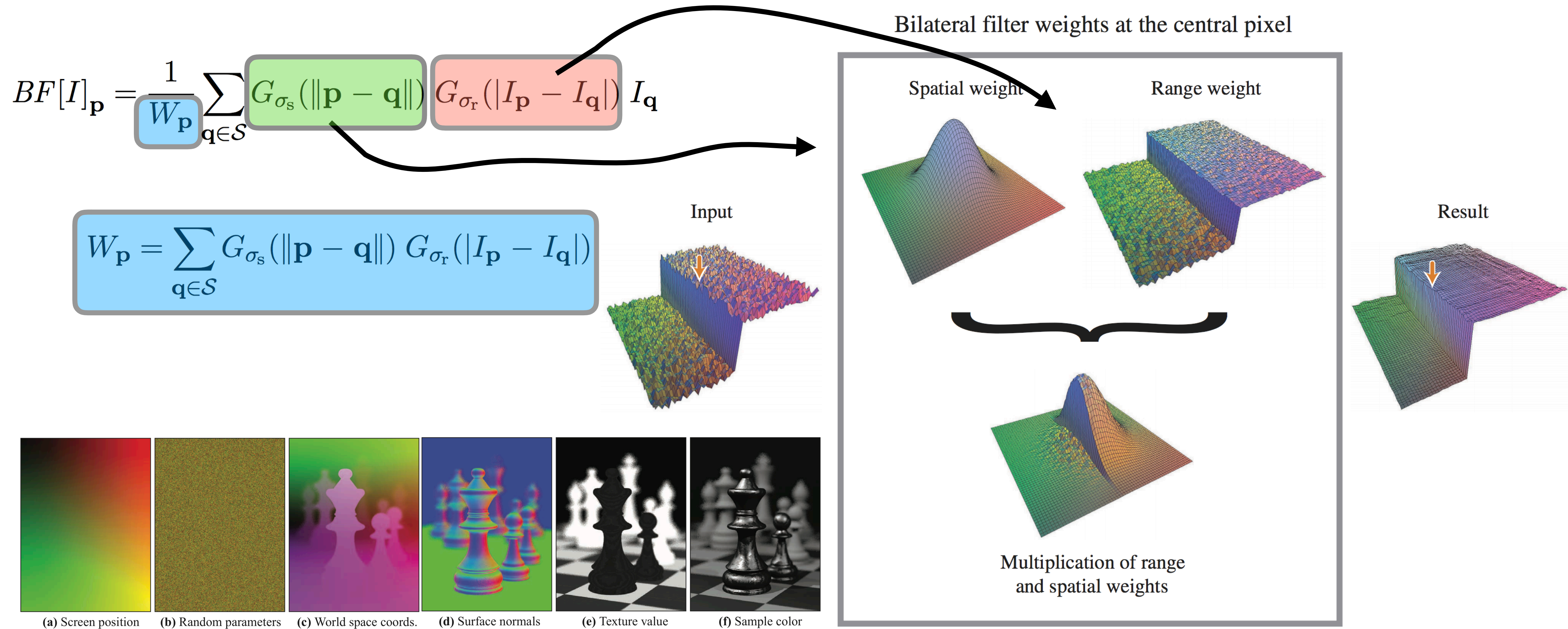


**(b)** Dependency on  $(u, v)$



**(c)** Our approach (RPF)

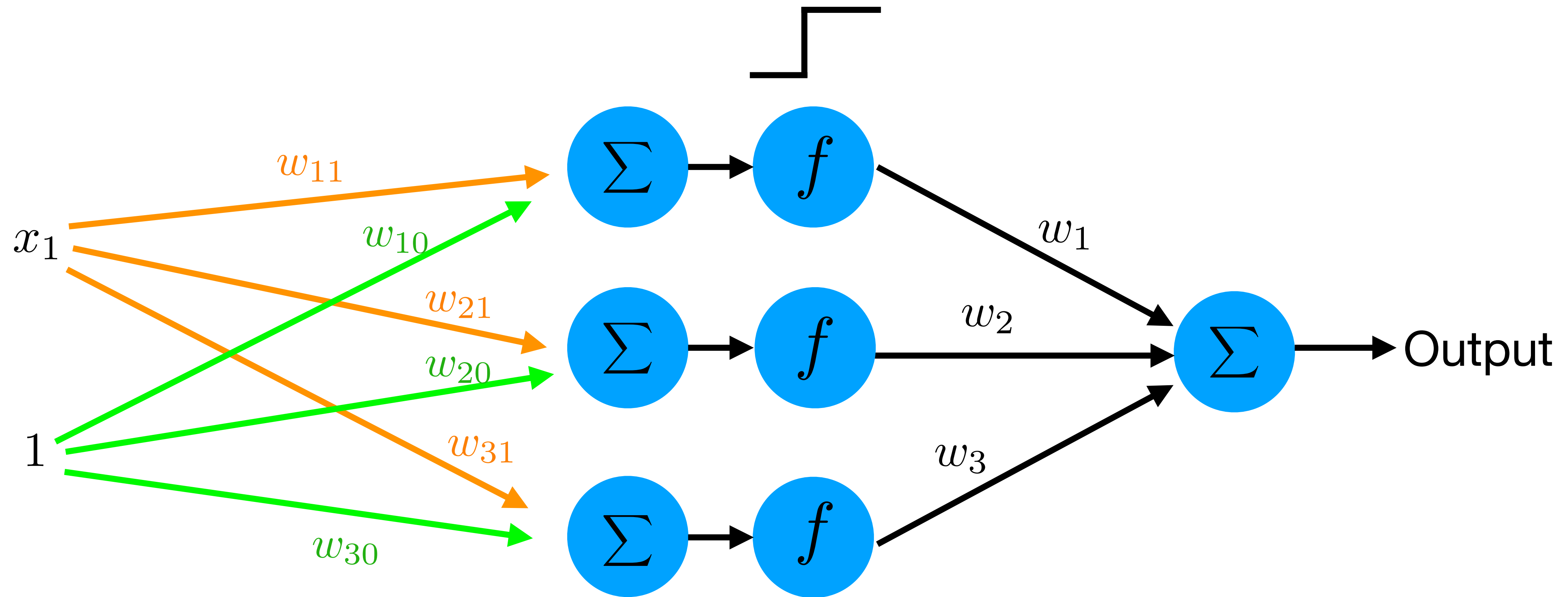
# Bilateral Filtering



# Bilateral Filtering of Features

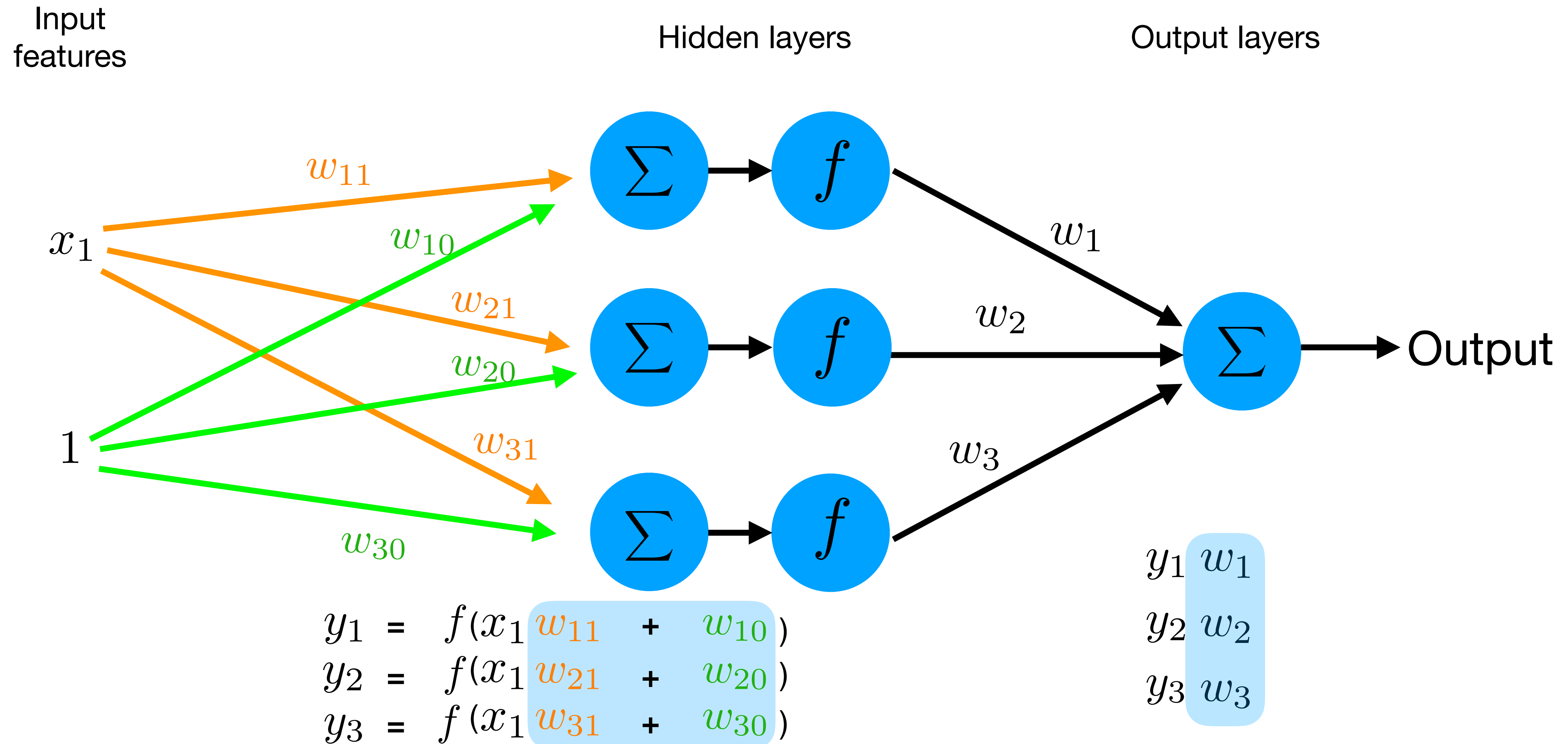
$$w_{ij} = \exp\left[-\frac{1}{2\sigma_p^2} \sum_{1 \leq k \leq 2} (\bar{\mathbf{p}}_{i,k} - \bar{\mathbf{p}}_{j,k})^2\right] \times$$
$$\exp\left[-\frac{1}{2\sigma_c^2} \sum_{1 \leq k \leq 3} \alpha_k (\bar{\mathbf{c}}_{i,k} - \bar{\mathbf{c}}_{j,k})^2\right] \times$$
$$\exp\left[-\frac{1}{2\sigma_f^2} \sum_{1 \leq k \leq m} \beta_k (\bar{\mathbf{f}}_{i,k} - \bar{\mathbf{f}}_{j,k})^2\right],$$

# Multi-layer Perceptron



$$\begin{aligned} y_1 &= f(x_1 w_{11} + w_{10}) \\ y_2 &= f(x_1 w_{21} + w_{20}) \\ y_3 &= f(x_1 w_{31} + w_{30}) \end{aligned}$$

# Multi-layer Perceptron



# Filter weights

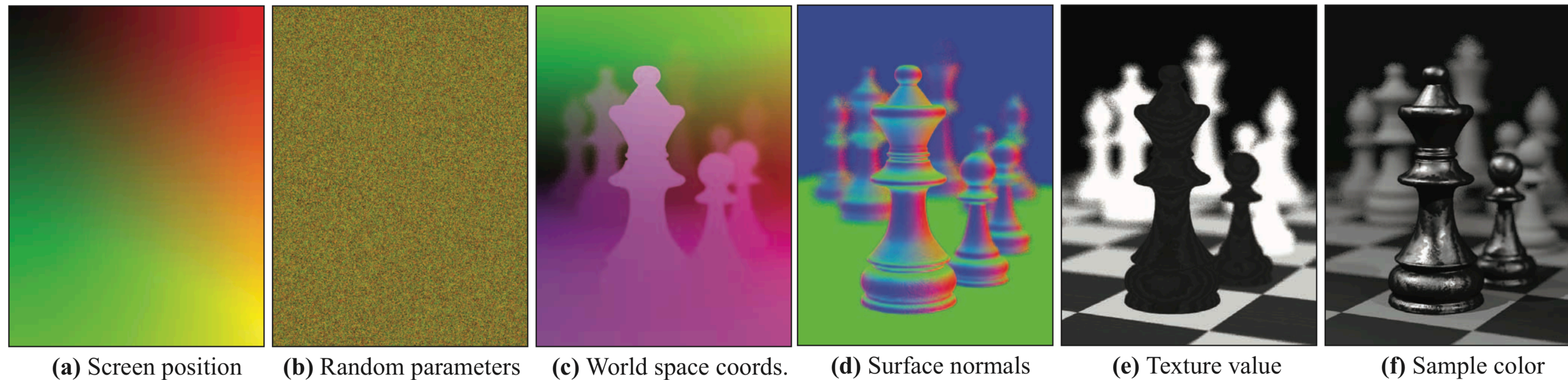
For cross Bilateral filters:

$$d_{i,j} = \exp \left[ - \frac{\|\bar{\mathbf{p}}_i - \bar{\mathbf{p}}_j\|^2}{2\alpha_i^2} \right] \times \exp \left[ - \frac{D(\bar{\mathbf{c}}_i, \bar{\mathbf{c}}_j)}{2\beta_i^2} \right] \times \prod_{k=1}^K \exp \left[ - \frac{D_k(\bar{\mathbf{f}}_{i,k}, \bar{\mathbf{f}}_{j,k})}{2\gamma_{k,i}^2} \right],$$

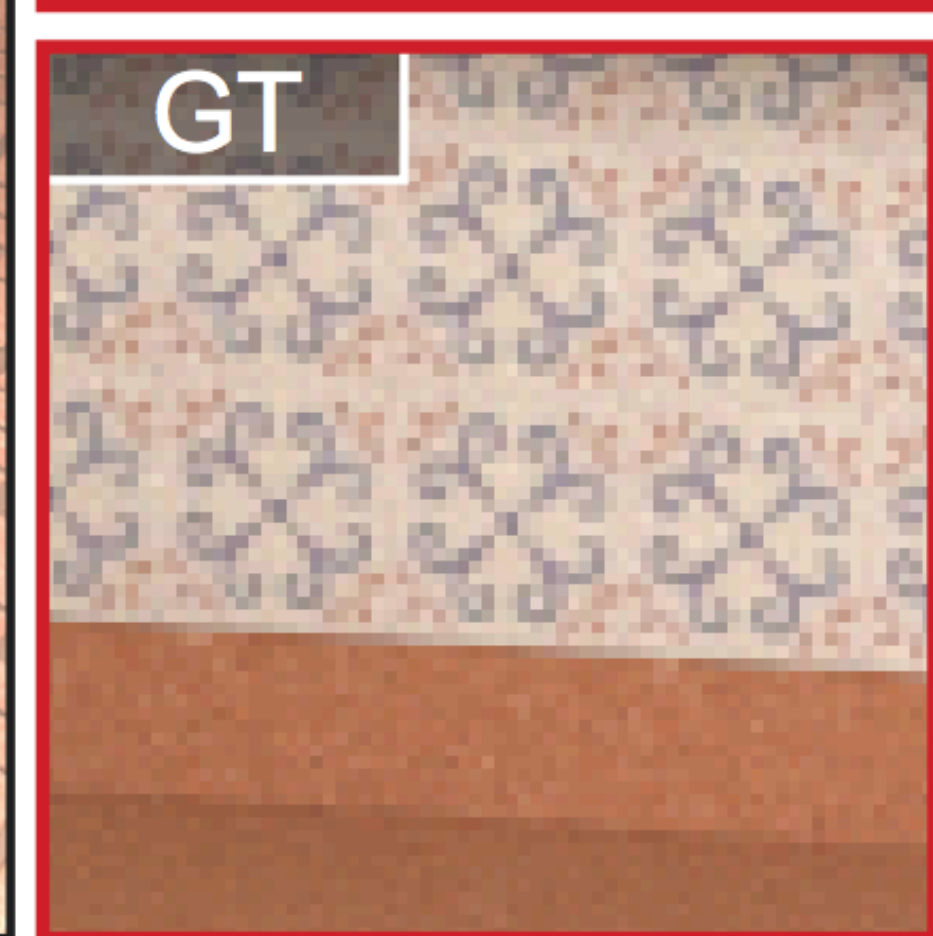
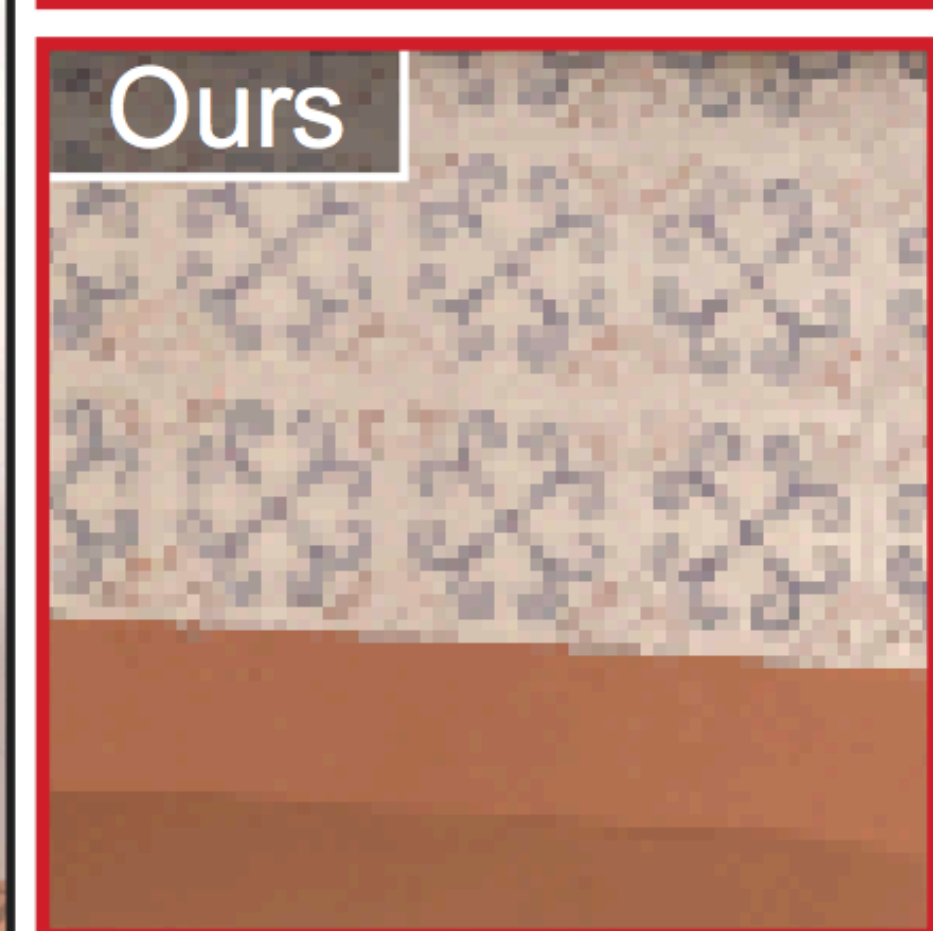
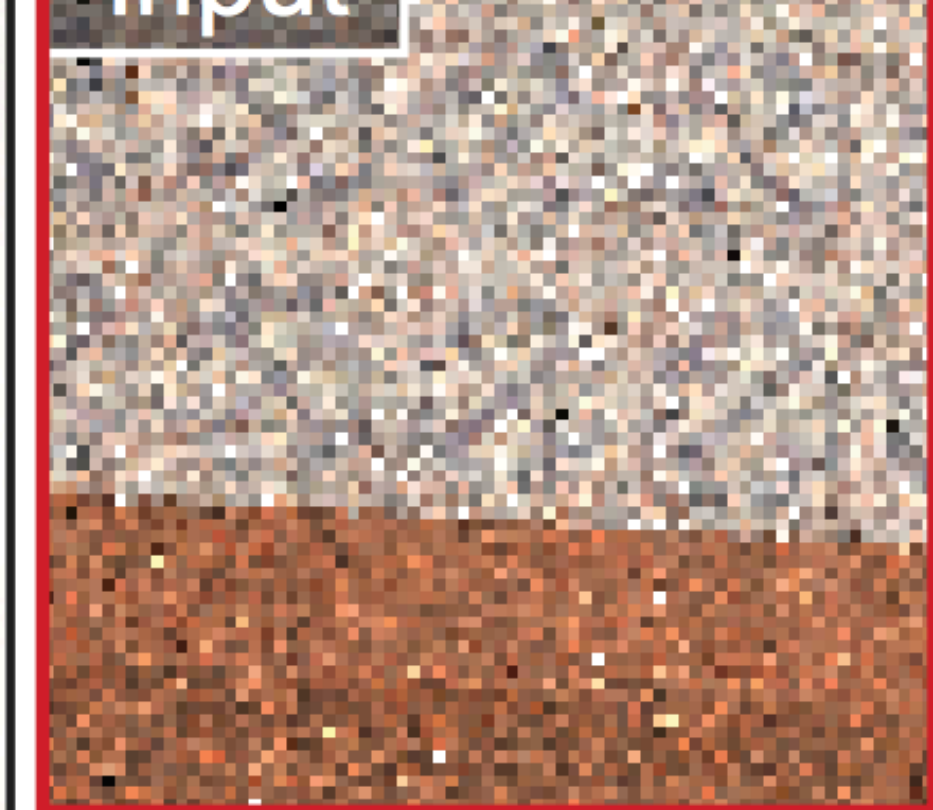
Pixel screen coordinates

Mean sample color value

Scene features







Our result with a cross-bilateral filter (4 spp)

# Overview on Convolutional Neural Networks (CNNs)

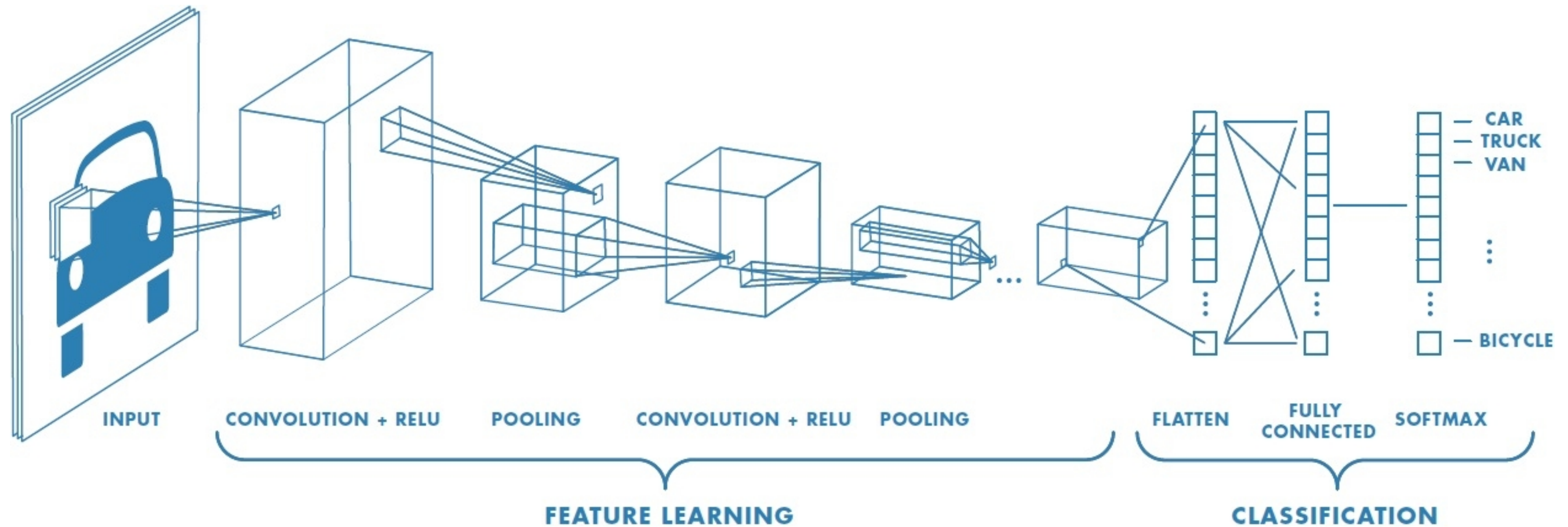
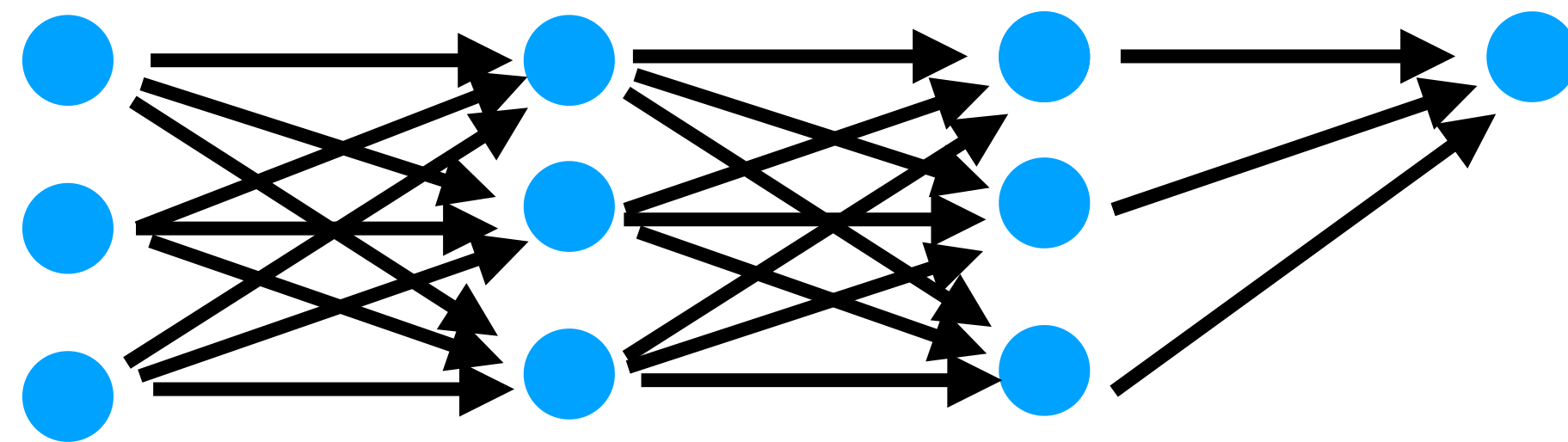


Image Courtesy: Mathworks (online tutorial)

# Multi-layer Perceptron vs. CNNs

Multi-layer perceptron

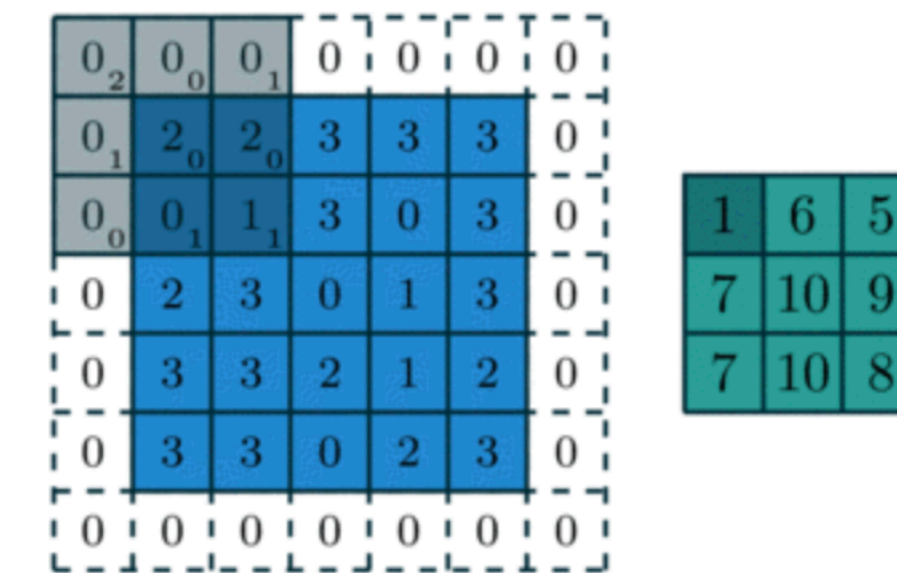


All nodes are fully connected in all layers

In theory, should be able to achieve good quality results in small number of layers.

Number of weights to be learnt are very high

CNNs

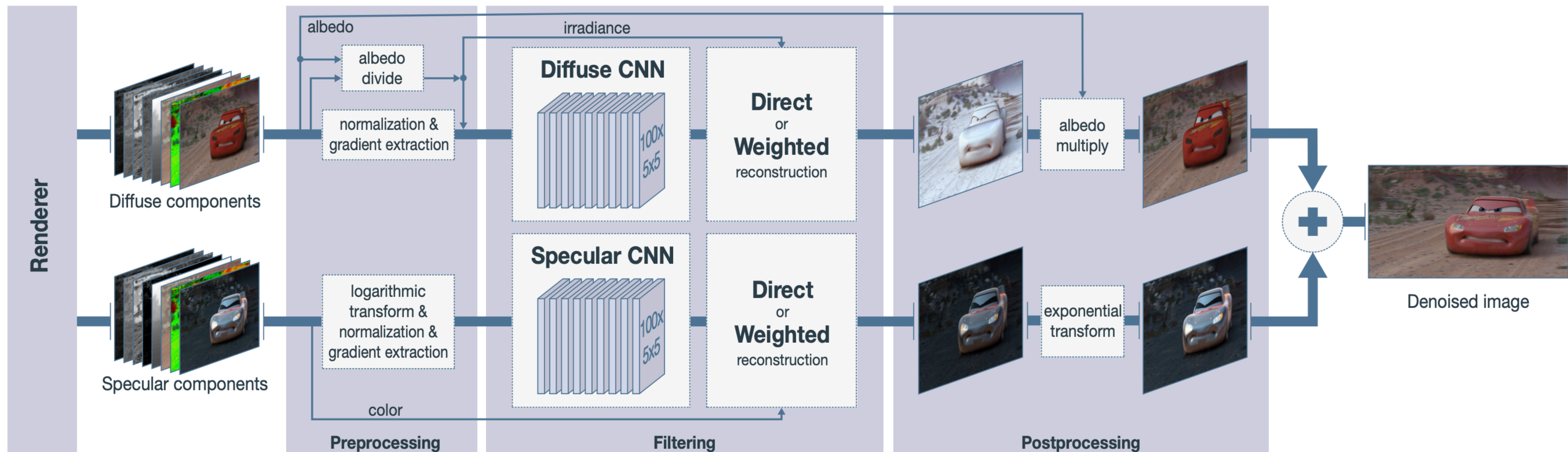


Weights are shared across layers

Requires significant number of layers to capture all the features (e.g. Deep CNNs)

Relatively small number of weights required

# Kernel-Predicting Networks for Denoising Monte-Carlo Renderings



# Recurrent AutoEncoder for Interactive Reconstruction

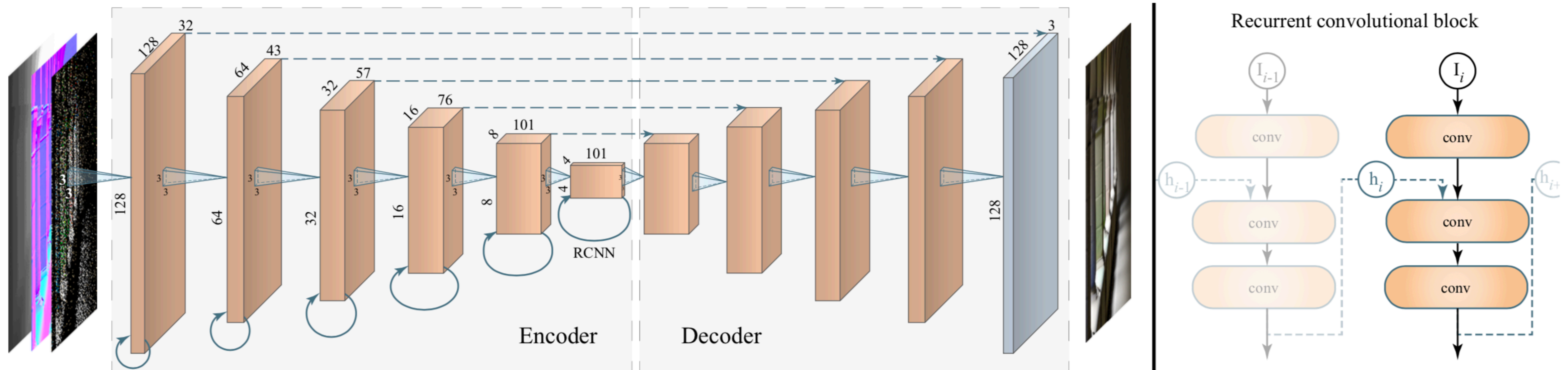
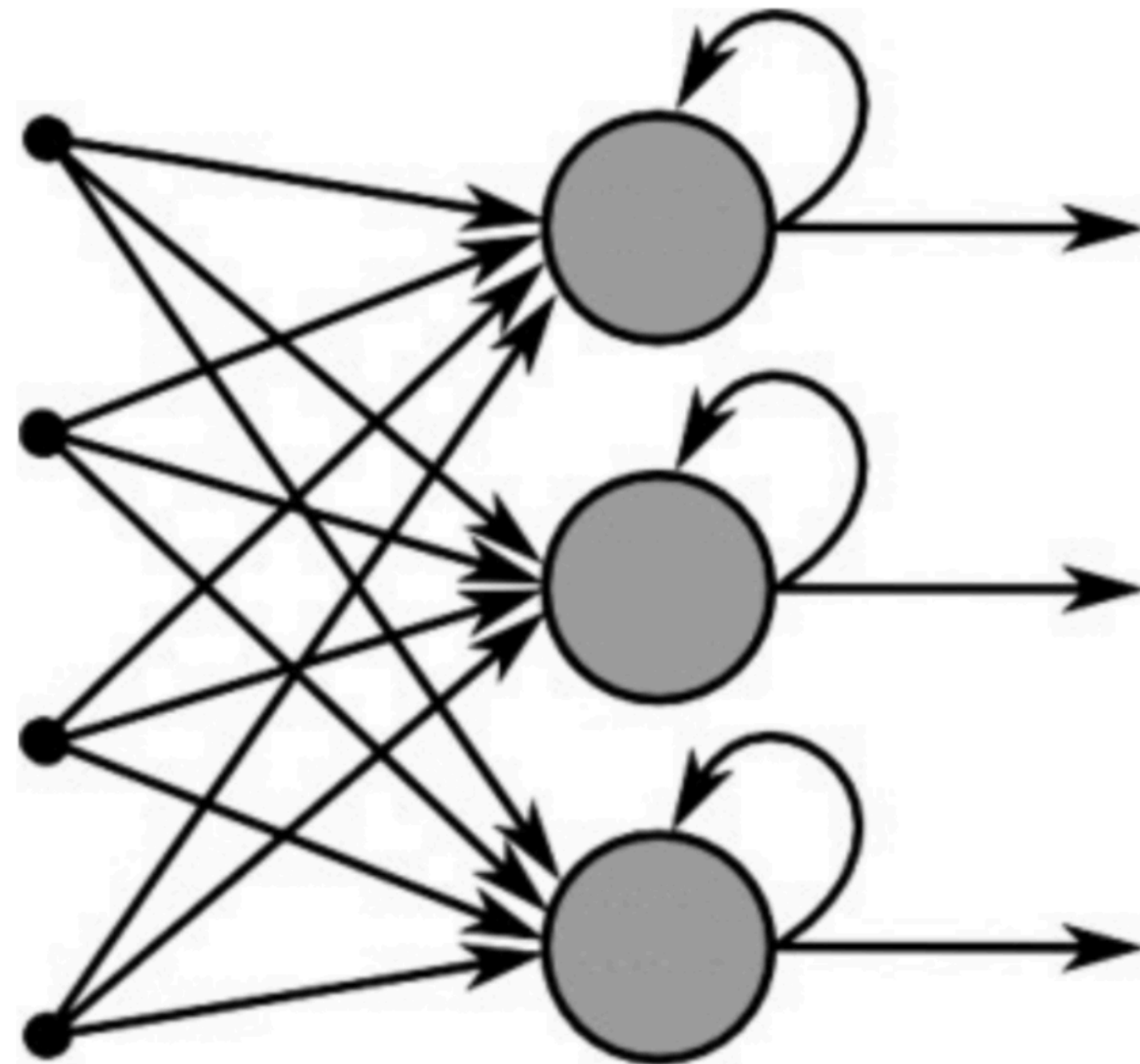


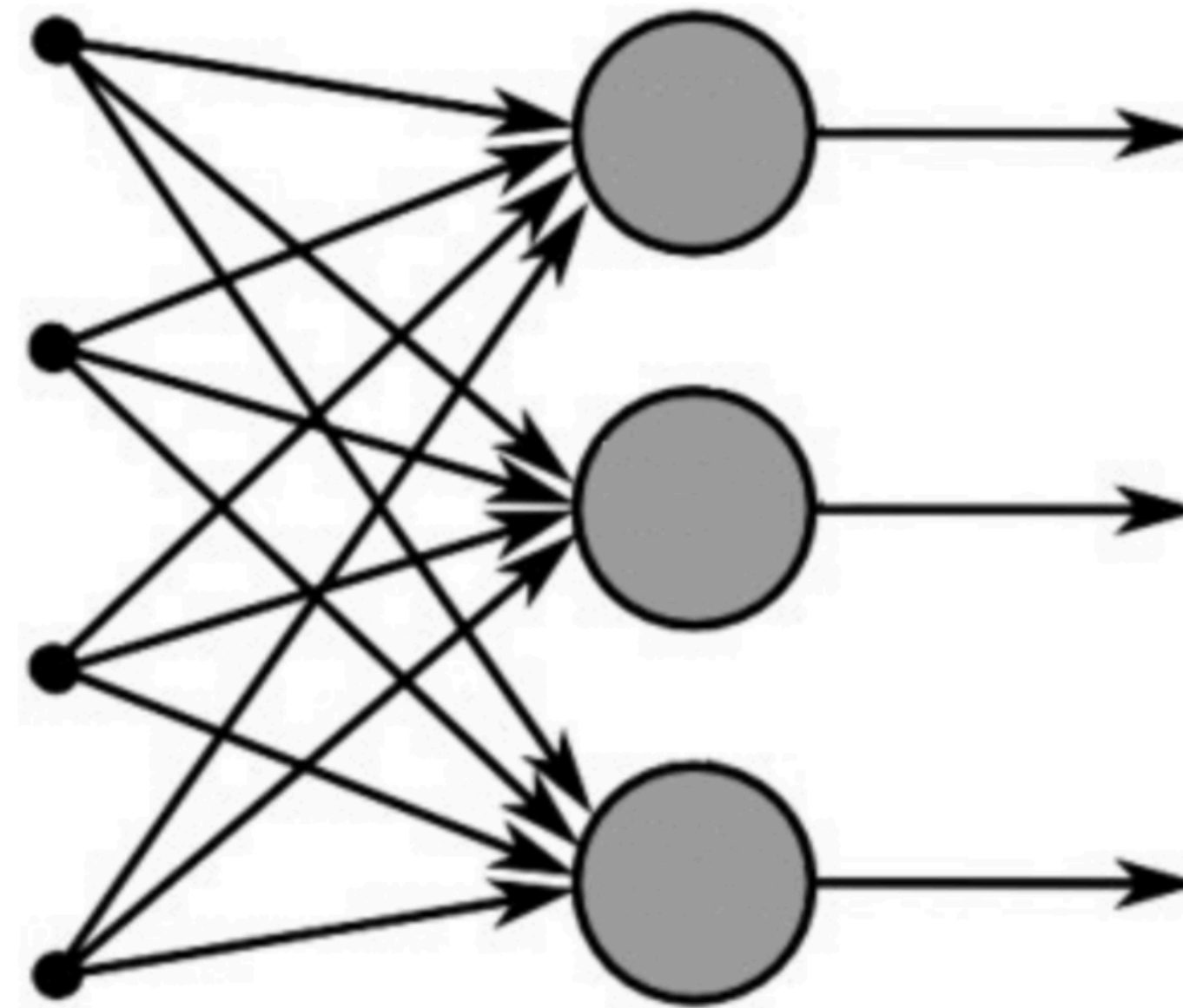
Fig. 2. Architecture of our recurrent autoencoder. The input is 7 scalar values per pixel (noisy RGB, normal vector, depth, roughness). Each encoder stage has a convolution and  $2 \times 2$  max pooling. A decoder stage applies a  $2 \times 2$  nearest neighbor upsampling, concatenates the per-pixel feature maps from a skip connection (the spatial resolutions agree), and applies two sets of convolution and pooling. All convolutions have a  $3 \times 3$ -pixel spatial support. On the right we visualize the internal structure of the recurrent RCNN connections.  $I$  is the new input and  $h$  refers to the hidden, recurrent state that persists between animation frames.

# Recurrent Neural Networks vs. Simple Feed-Forward NN

[Source link](#)



Recurrent Neural Network



Feed-Forward Neural Network

# Loss Functions

Spatial Loss to emphasize more the dark regions

$$L_s = \frac{1}{N} \sum_i^N |P_i - T_i|$$

Temporal loss

$$L_t = \frac{1}{N} \sum_i^N \left( \left| \frac{\partial P_i}{\partial t} - \frac{\partial T_i}{\partial t} \right| \right)$$

High frequency error norm loss for stable edges

$$L_g = \frac{1}{N} \sum_i^N |\nabla P_i - \nabla T_i|$$

Final Loss is a weighted averaged of above losses

$$L = w_s L_s + w_g L_g + w_t L_t$$

**Pixel-space  
Kernel Predicting  
Denoising**

**#Learnable  
Parameters?**

**Sample-based  
MC Denoising**

How to compute "learnable" parameters?



# How to compute "learnable" parameters?

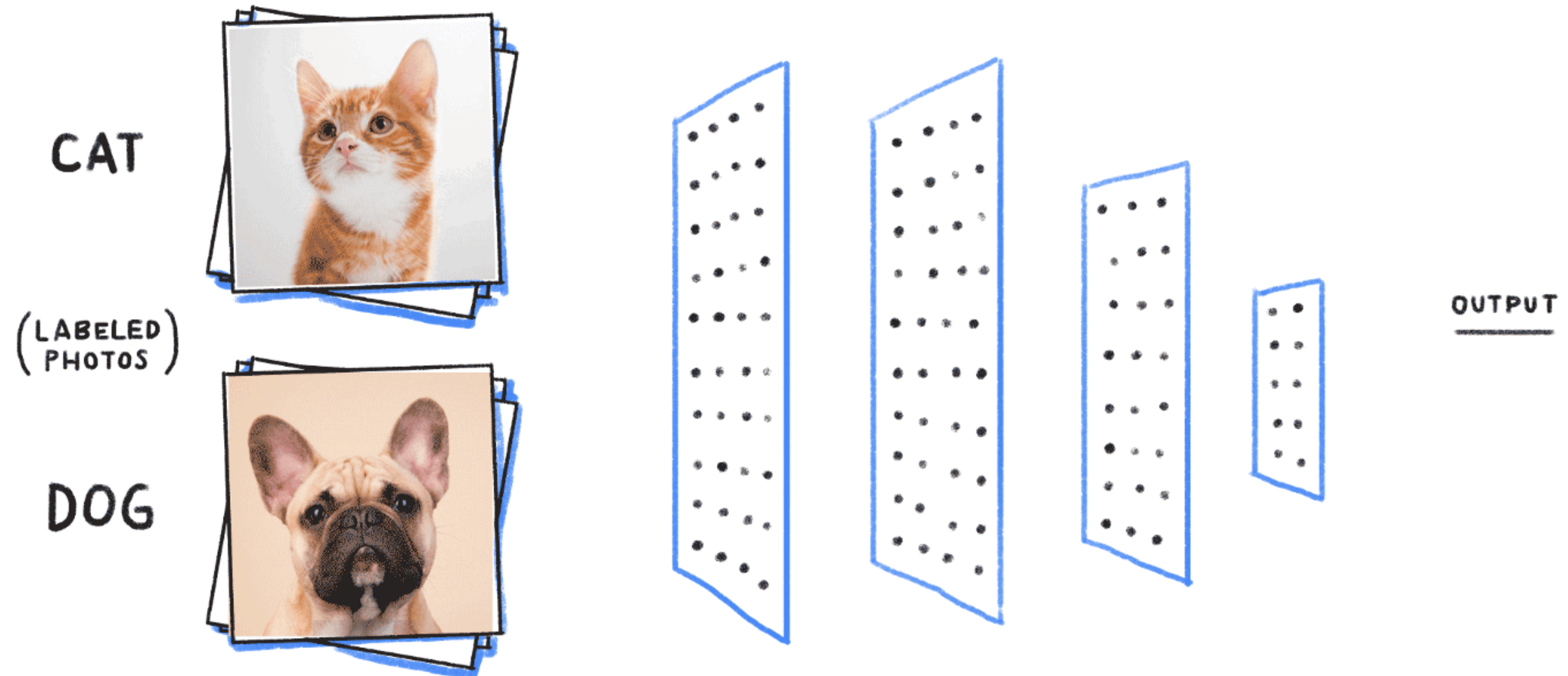


Image Source: Google

# How to compute "learnable" parameters?

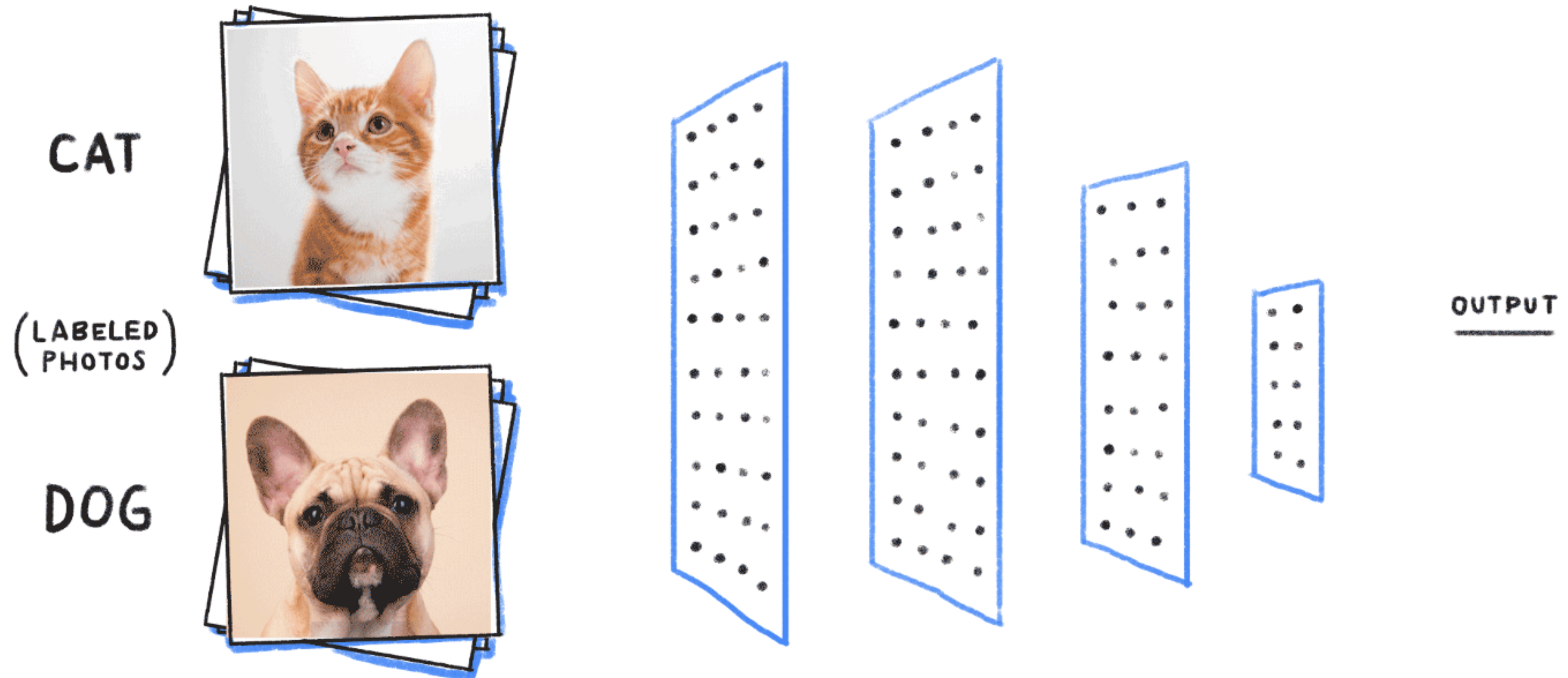


Image Source: Google

# Feed-Forward Neural Network

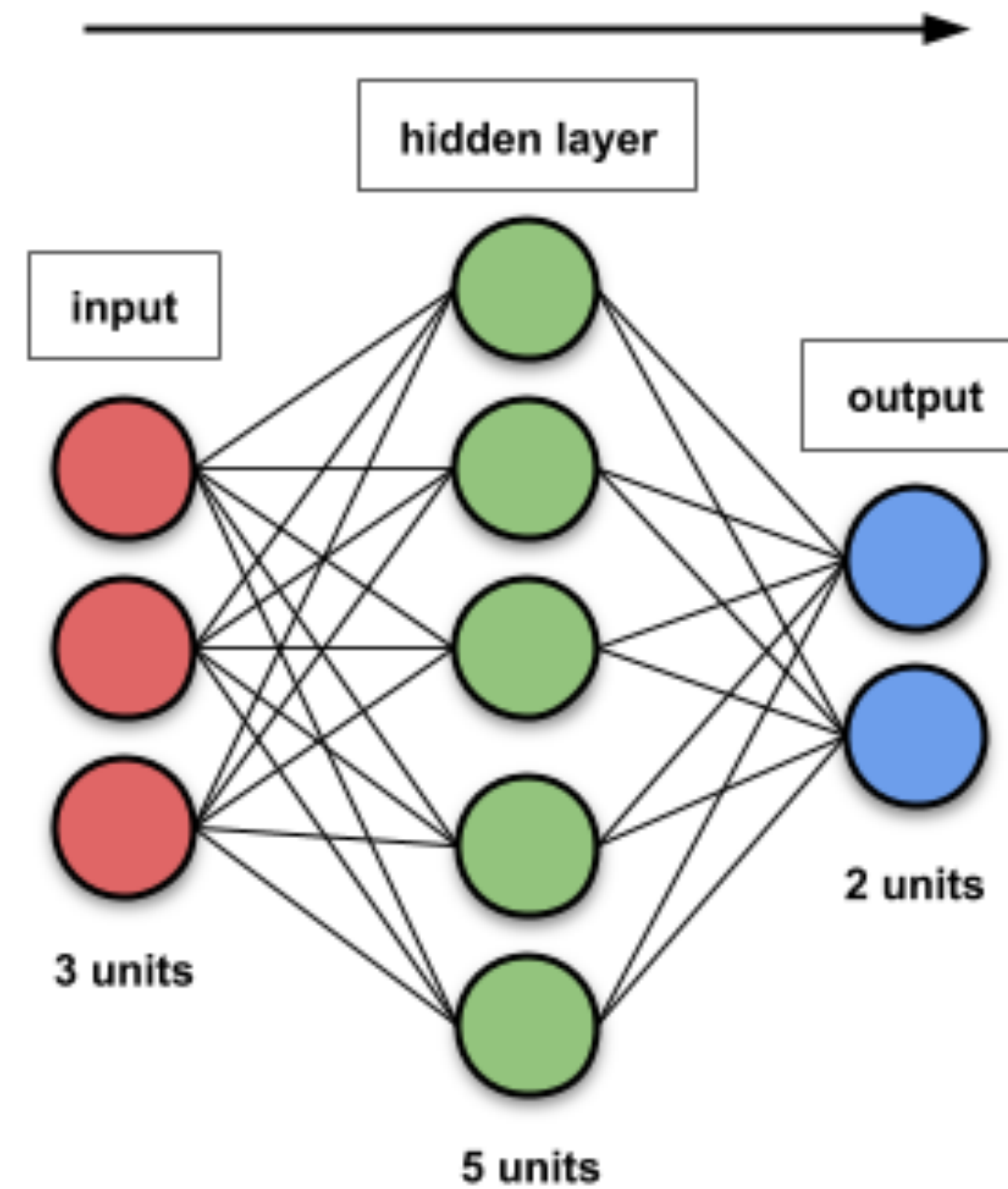
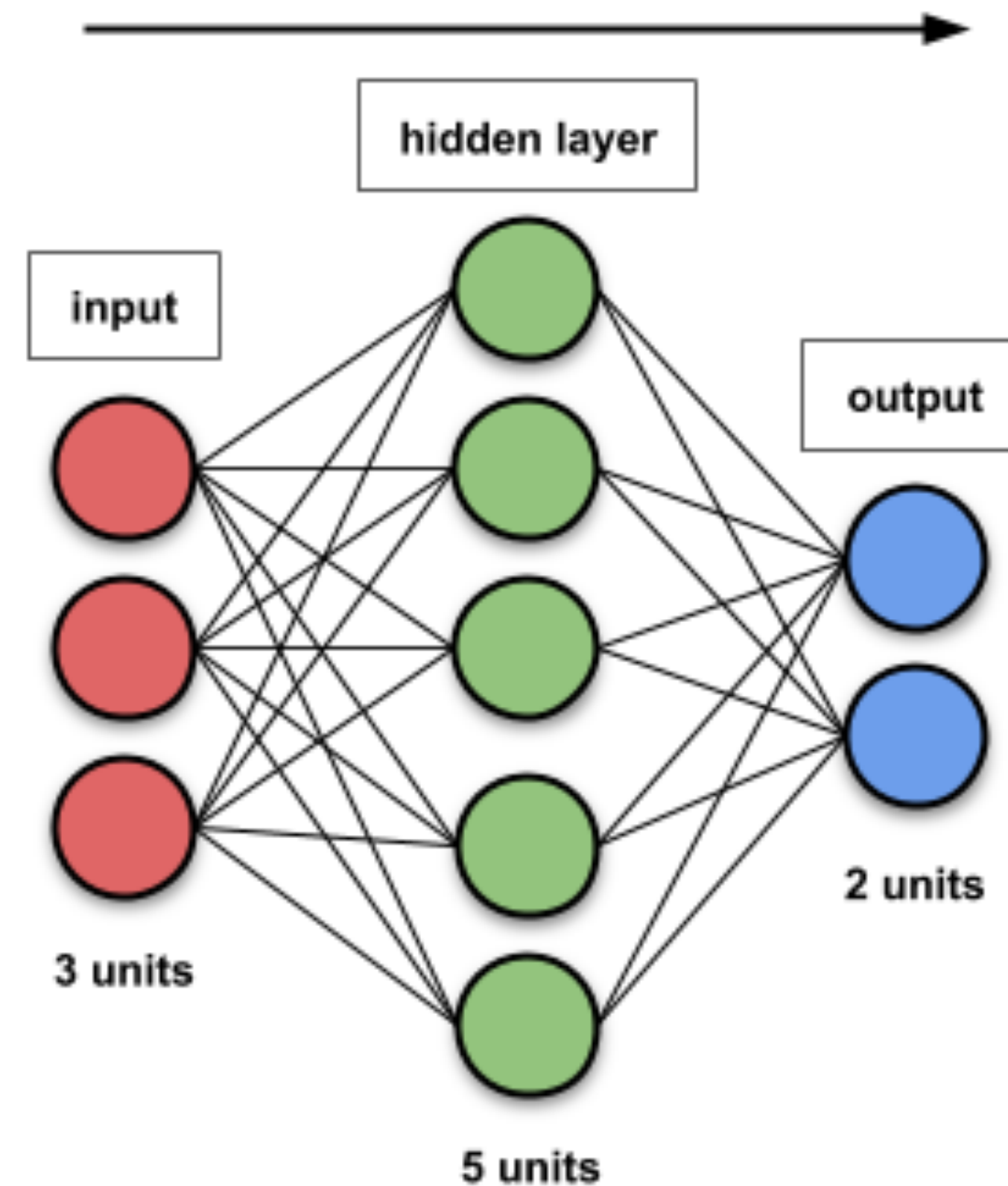


Image Source: towards-data-science

# Feed-Forward Neural Network



$$(3 \times 5) + (5 \times 2) + (5 + 2) = 17 \text{ parameters}$$

weights                  biases

Image Source: towards-data-science

# Feed-Forward Neural Network

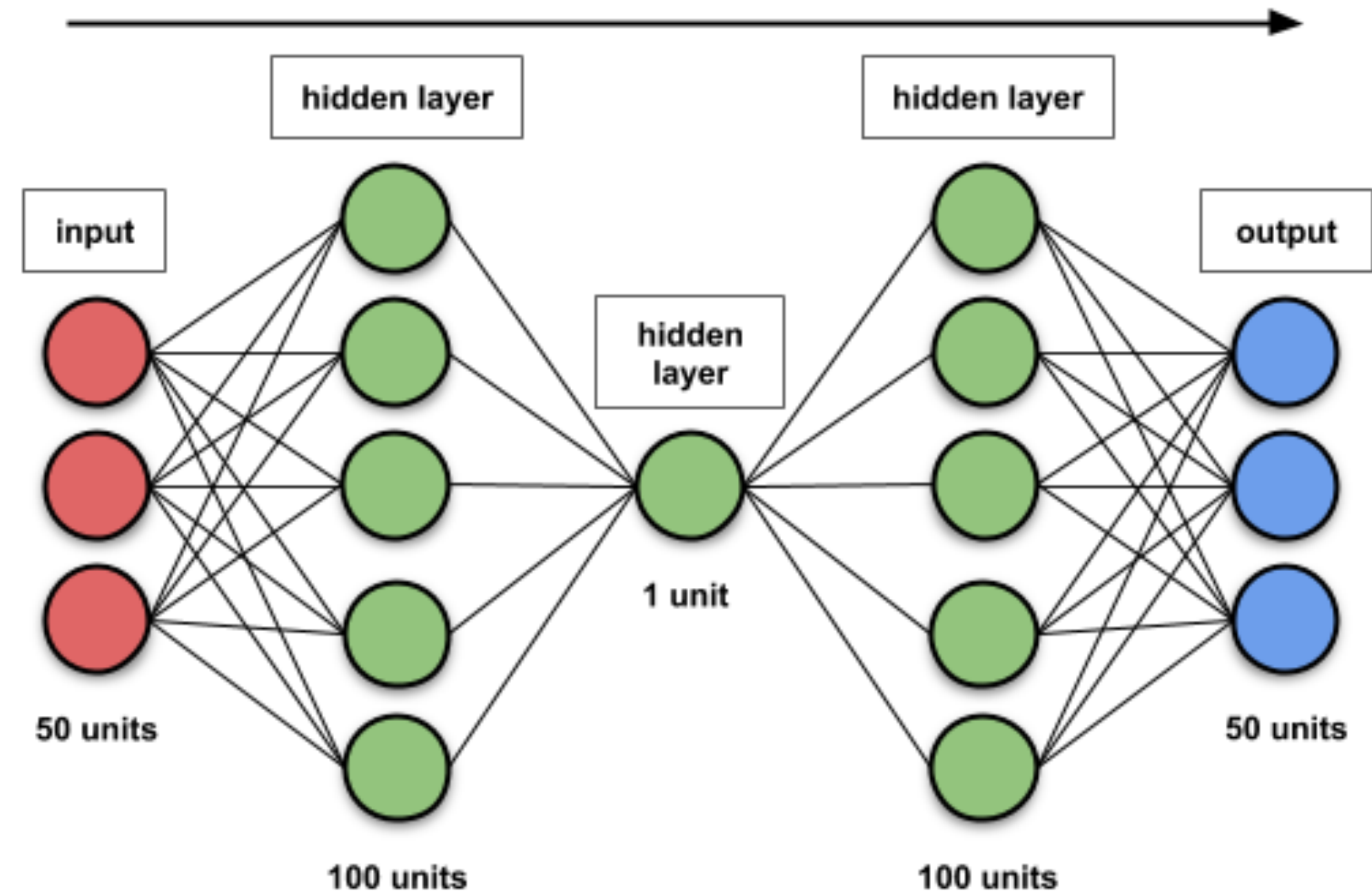


Image Source: towards-data-science

# Overview on Convolutional Neural Networks (CNNs)

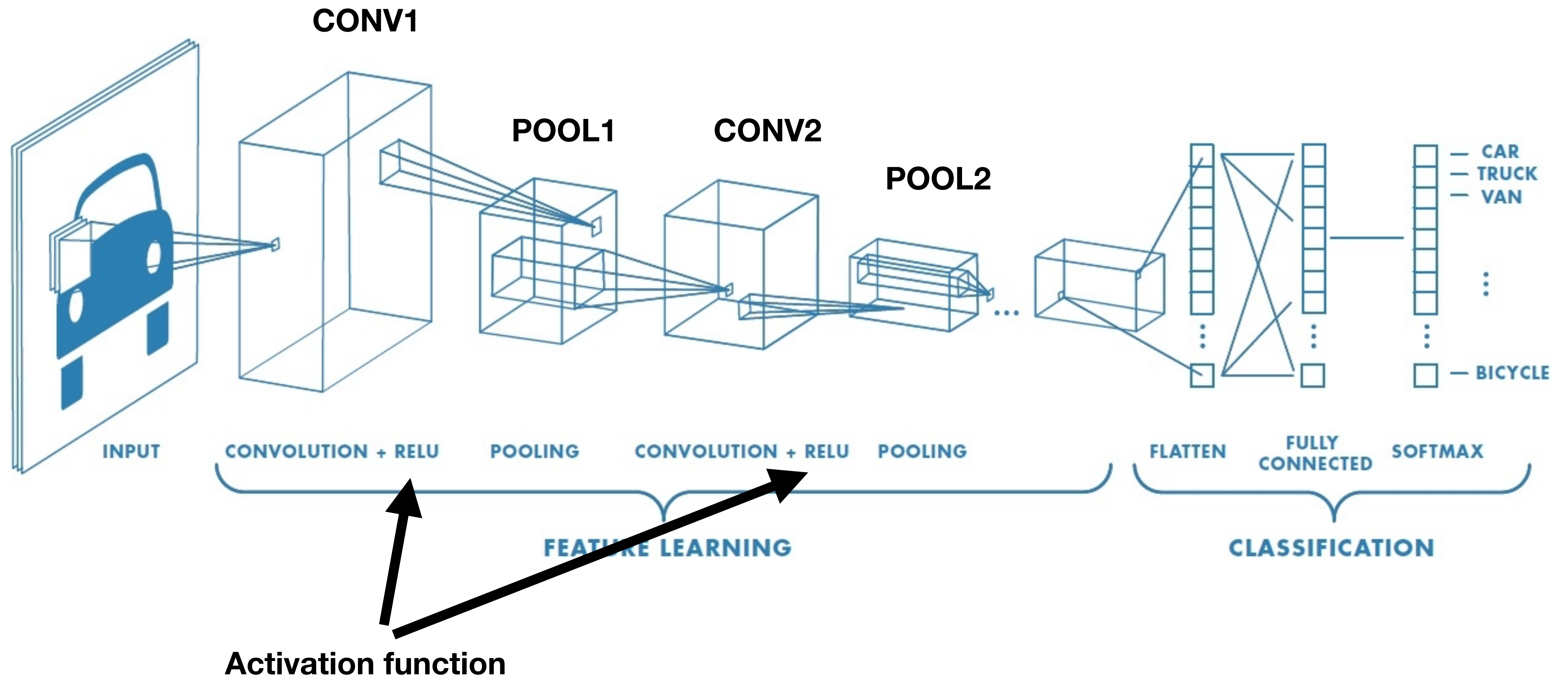
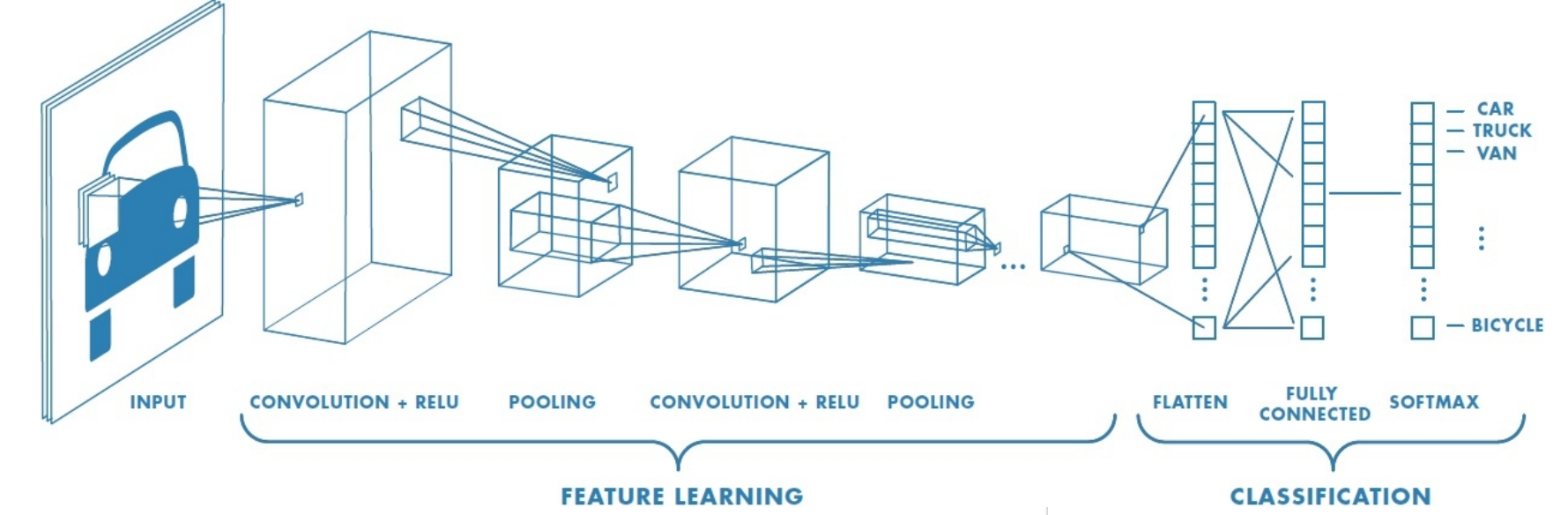


Image Courtesy: Mathworks (online tutorial)

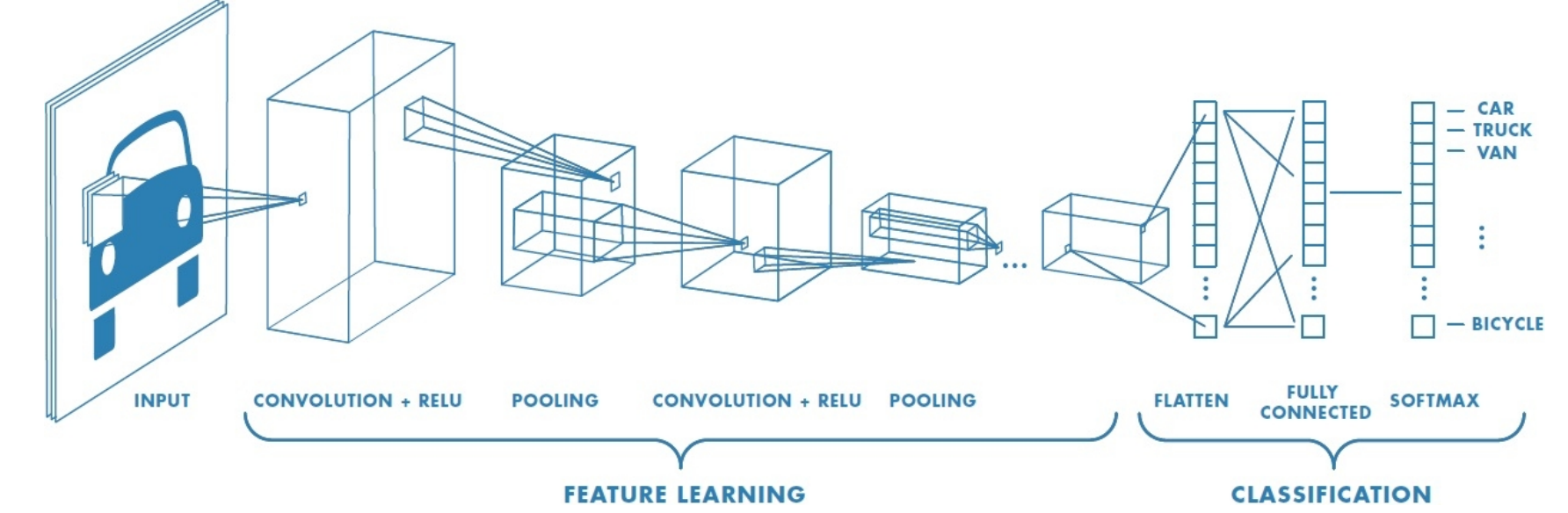
# Neural network example



	Activation shape	Activation Size	# parameters
Input:	(32,32,3)		
CONV1 (f=5, s=1)	(28,28,8)		
POOL1	(14,14,8)		
CONV2 (f=5, s=1)	(10,10,16)		
POOL2	(5,5,16)		
FC3	(120,1)		
FC4	(84,1)		
Softmax	(10,1)		

<https://www.coursera.org/learn/convolutional-neural-networks/lecture/uRYL1/cnn-example>

Andrew Ng



Activation size

# parameters

## Neural network example

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Input layer:

Conv1 layer:

Pool1 layer:

Conv2 layer:

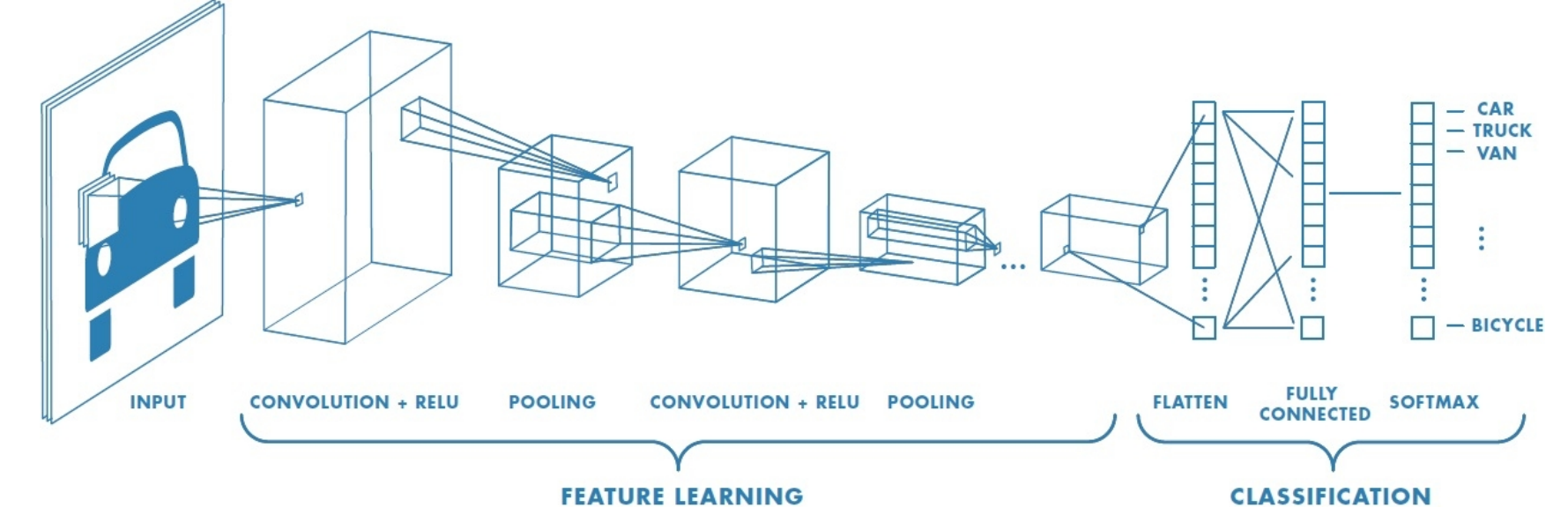
Pool2 layer:

FC3 layer:

FC4 layer:

Softmax layer:





## Neural network example

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Softmax	(10,1)		

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Activation size

# parameters

Input layer:  $32 \times 32 \times 3 = 3072$

Conv1 layer:

Pool1 layer:

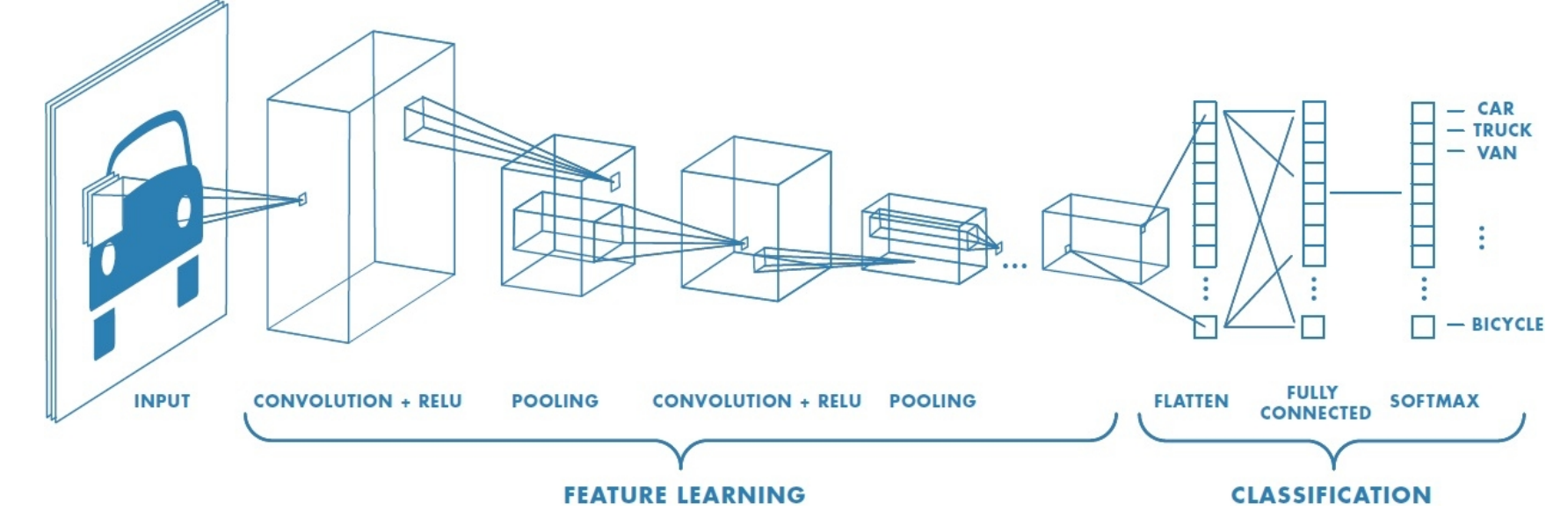
Conv2 layer:

Pool2 layer:

FC3 layer:

FC4 layer:

Softmax layer:



## Neural network example

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Input:	(32,32,3)		
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POOL2	(5,5,16)		
FC3	(120,1)		
FC4	(84,1)		
Softmax	(10,1)		

Andrew Ng

Activation size

# parameters

Input layer:  $32 \cdot 32 \cdot 3 = 3072$

Conv1 layer:  $28 \cdot 28 \cdot 8 = 6272$

Pool1 layer:  $14 \cdot 14 \cdot 8 = 1568$

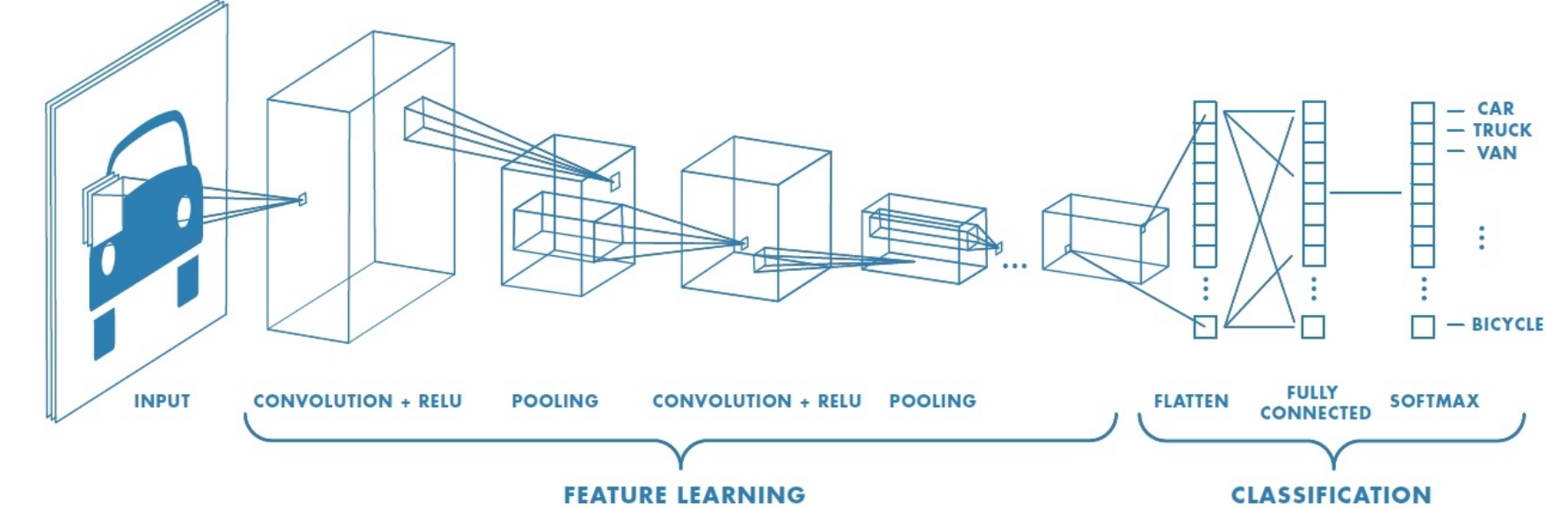
Conv2 layer:  $10 \cdot 10 \cdot 16 = 1600$

Pool2 layer:  $5 \cdot 5 \cdot 16 = 400$

FC3 layer:  $120 \cdot 1 = 120$

FC4 layer:  $84 \cdot 1 = 84$

Softmax layer:  $10 \cdot 1 = 10$

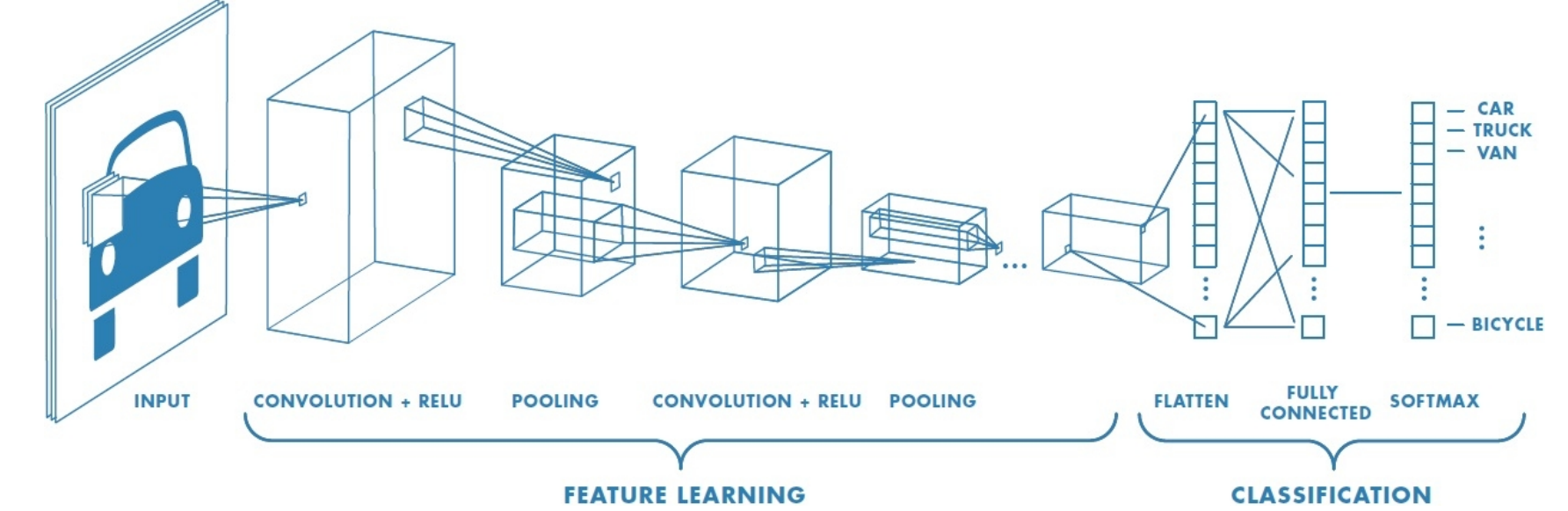


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FC3	(120,1)		
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Softmax	(10,1)		

Andrew Ng

	Activation size	# parameters
Input layer:	$32 \cdot 32 \cdot 3 = 3072$	0
Conv1 layer:	$28 \cdot 28 \cdot 8 = 6272$	
Pool1 layer:	$14 \cdot 14 \cdot 8 = 1568$	
Conv2 layer:	$10 \cdot 10 \cdot 16 = 1600$	
Pool2 layer:	$5 \cdot 5 \cdot 16 = 400$	
FC3 layer:	$120 \cdot 1 = 120$	
FC4 layer:	$84 \cdot 1 = 84$	
Softmax layer:	$10 \cdot 1 = 10$	

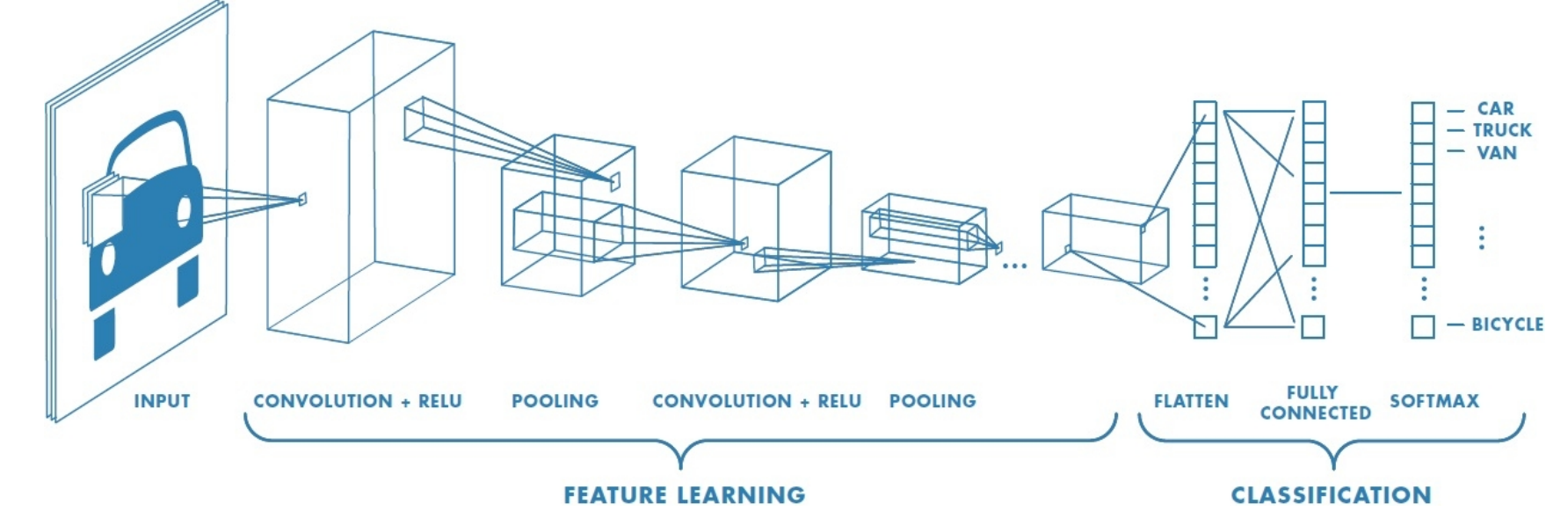


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Andrew Ng

	Activation size	# parameters
Input layer:	$32 \cdot 32 \cdot 3 = 3072$	0
Conv1 layer:	$28 \cdot 28 \cdot 8 = 6272$	$(fwidth \cdot fheight + 1) \cdot numfilters$
Pool1 layer:	$14 \cdot 14 \cdot 8 = 1568$	
Conv2 layer:	$10 \cdot 10 \cdot 16 = 1600$	
Pool2 layer:	$5 \cdot 5 \cdot 16 = 400$	
FC3 layer:	$120 \cdot 1 = 120$	
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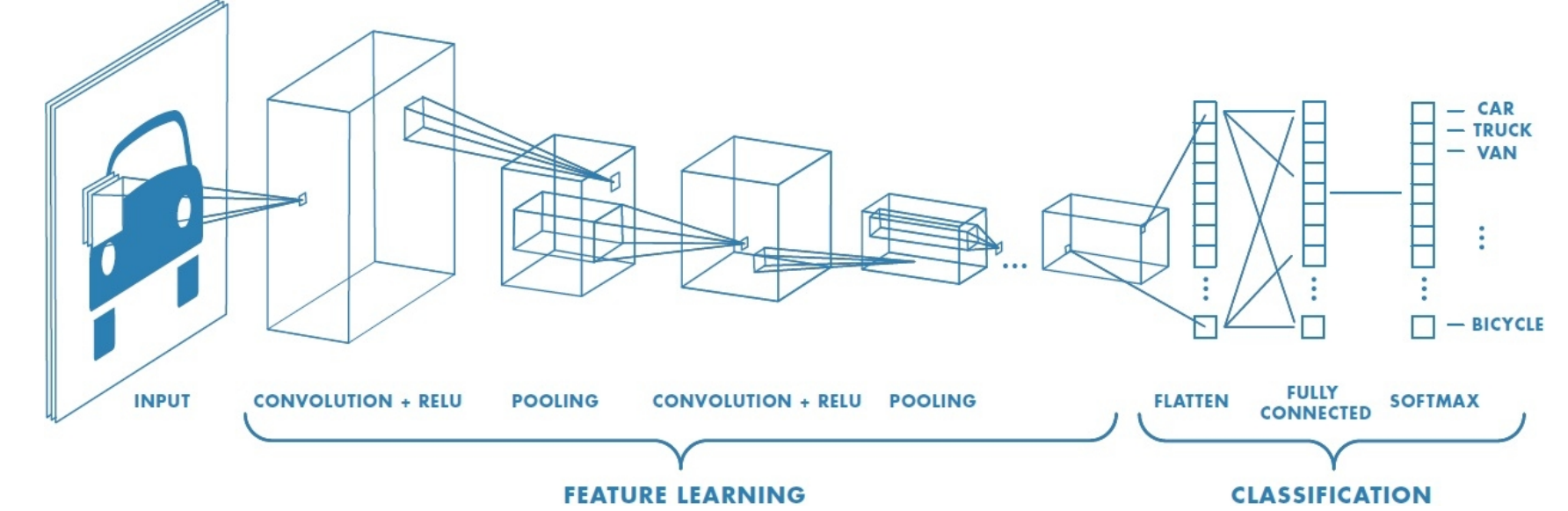


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FC3	(120,1)		
FC4	(84,1)		
Softmax	(10,1)		

Andrew Ng

	Activation size	# parameters
Input layer:	$32 \cdot 32 \cdot 3 = 3072$	0
Conv1 layer:	$28 \cdot 28 \cdot 8 = 6272$	$(5 \cdot 5 + 1) \cdot 8 = 208$
Pool1 layer:	$14 \cdot 14 \cdot 8 = 1568$	0
Conv2 layer:	$10 \cdot 10 \cdot 16 = 1600$	$(5 \cdot 5 + 1) \cdot 16 = 416$
Pool2 layer:	$5 \cdot 5 \cdot 16 = 400$	0
FC3 layer:	$120 \cdot 1 = 120$	$\text{currentLayer} \cdot \text{PrevLayer} + 1$
FC4 layer:	$84 \cdot 1 = 84$	
Softmax layer:	$10 \cdot 1 = 10$	

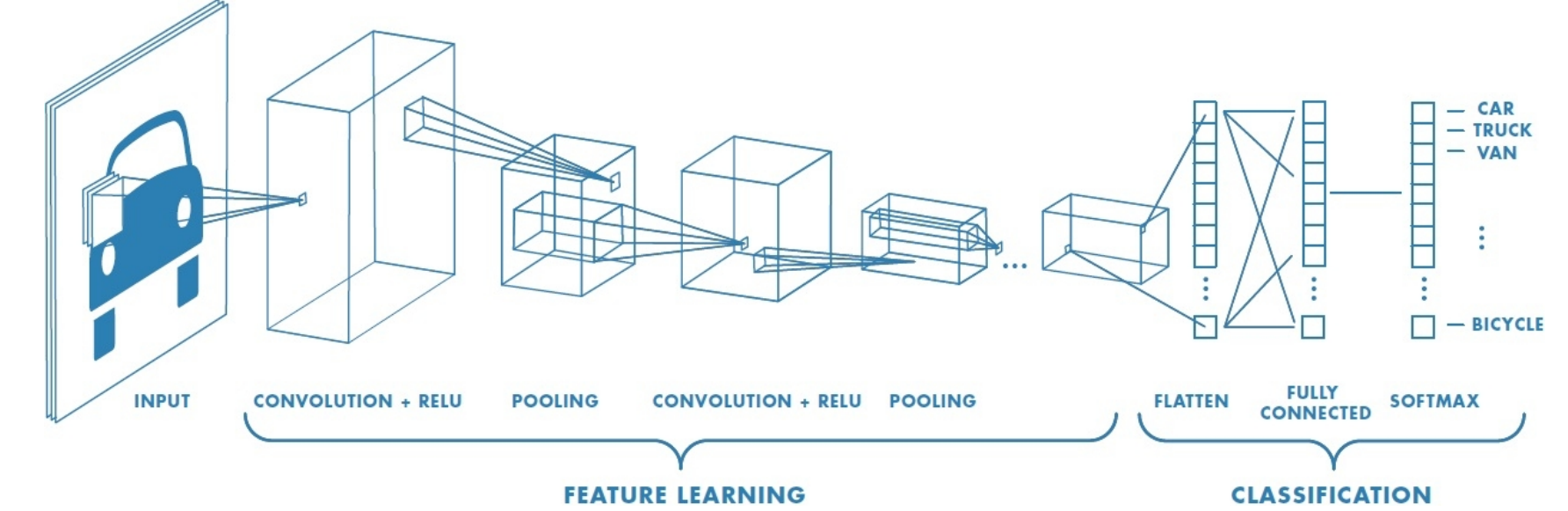


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Andrew Ng

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Pool2 layer:	$5 \cdot 5 \cdot 16 = 400$	0
FC3 layer:	$120 \cdot 1 = 120$	$\text{currentLayer} \cdot \text{PrevLayer} + 1$
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Andrew Ng

	Activation size	# parameters
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Pool1 layer:	$14 \cdot 14 \cdot 8 = 1568$	0
Conv2 layer:	$10 \cdot 10 \cdot 16 = 1600$	$(5 \cdot 5 + 1) \cdot 16 = 416$
Pool2 layer:	$5 \cdot 5 \cdot 16 = 400$	0
FC3 layer:	$120 \cdot 1 = 120$	$120 \cdot 400 + 1 = 48001$
FC4 layer:	$84 \cdot 1 = 84$	$120 \cdot 84 + 1 = 10081$
Softmax layer:	$10 \cdot 1 = 10$	$10 \cdot 84 + 1 = 841$

**Pixel-space  
Kernel Predicting  
Denoising**

**#Learnable  
Parameters?**

**Sample-based  
MC Denoising**

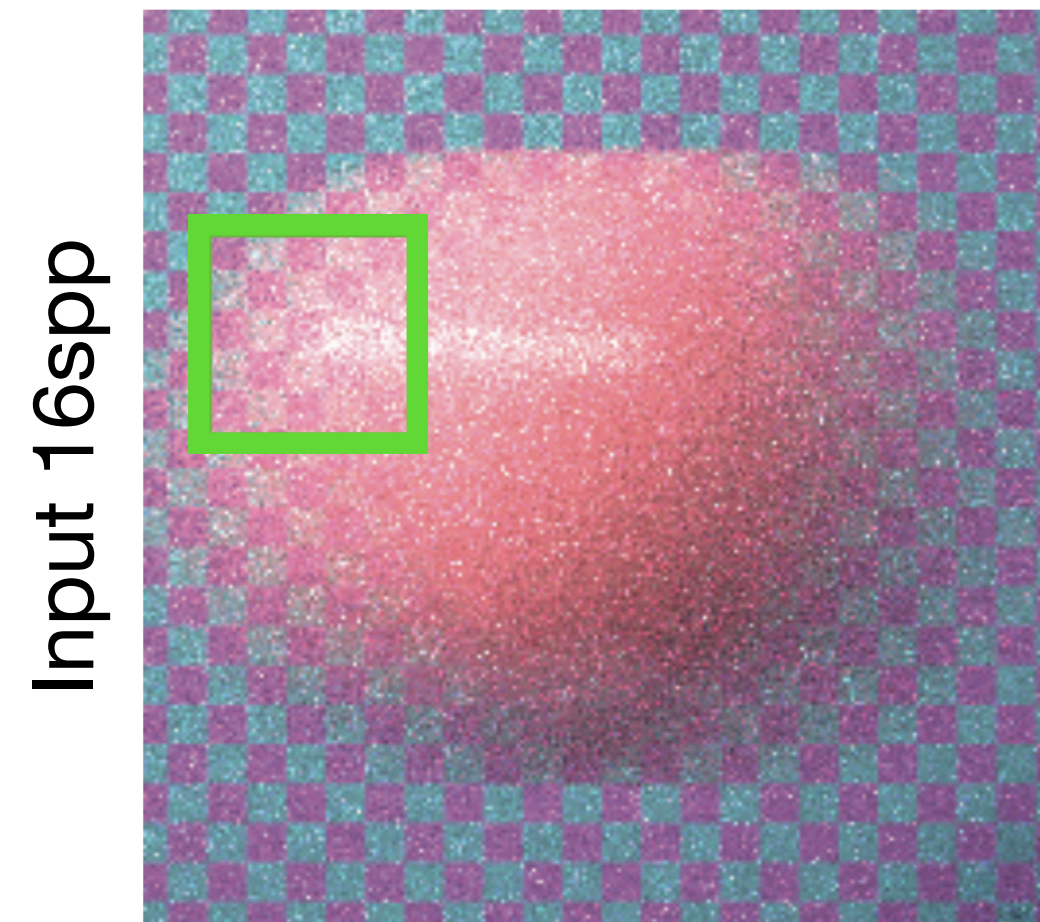
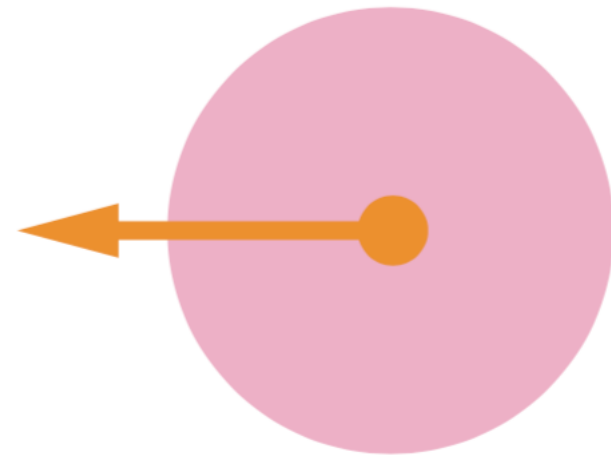


# Sample-based Denoising Network

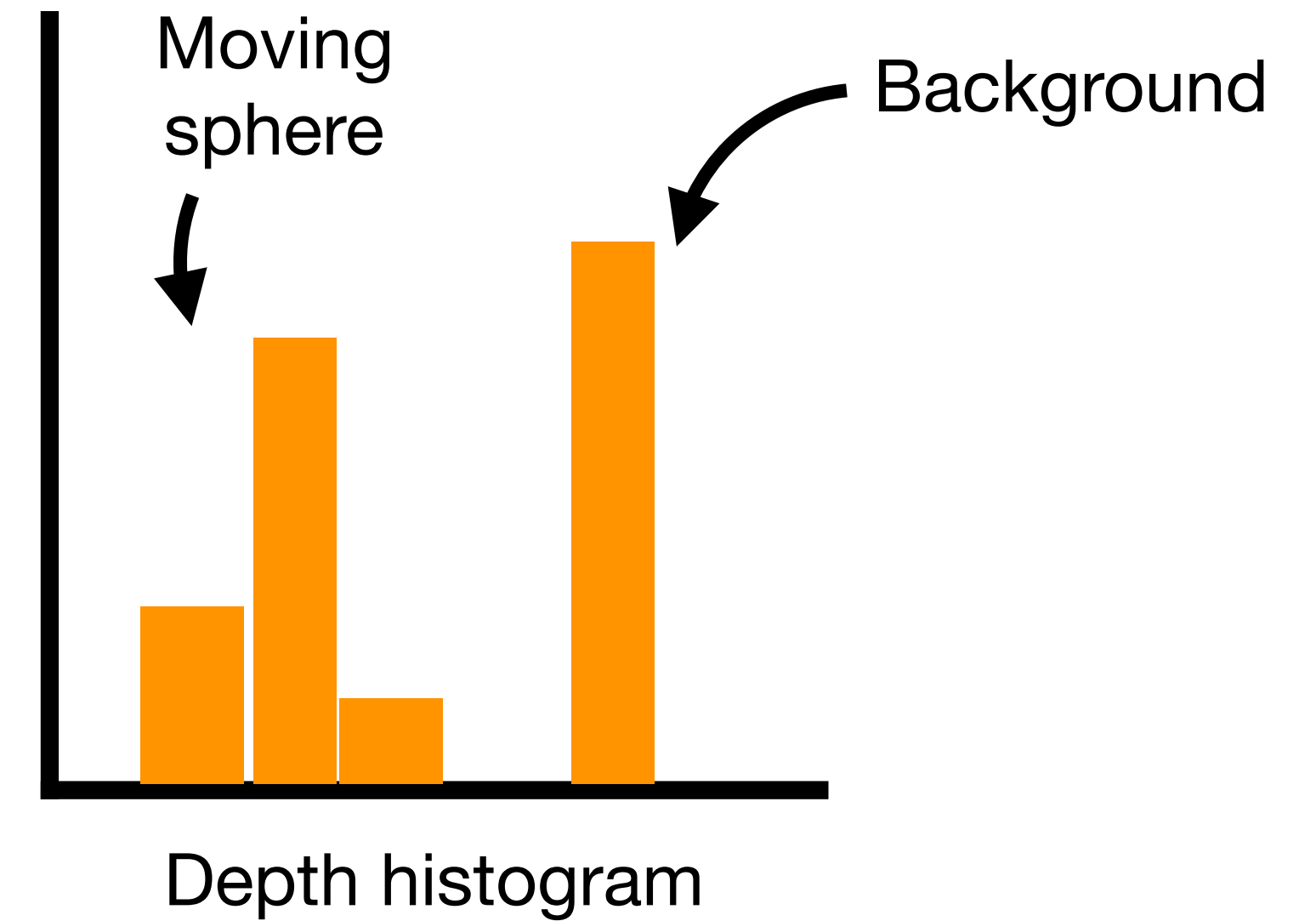
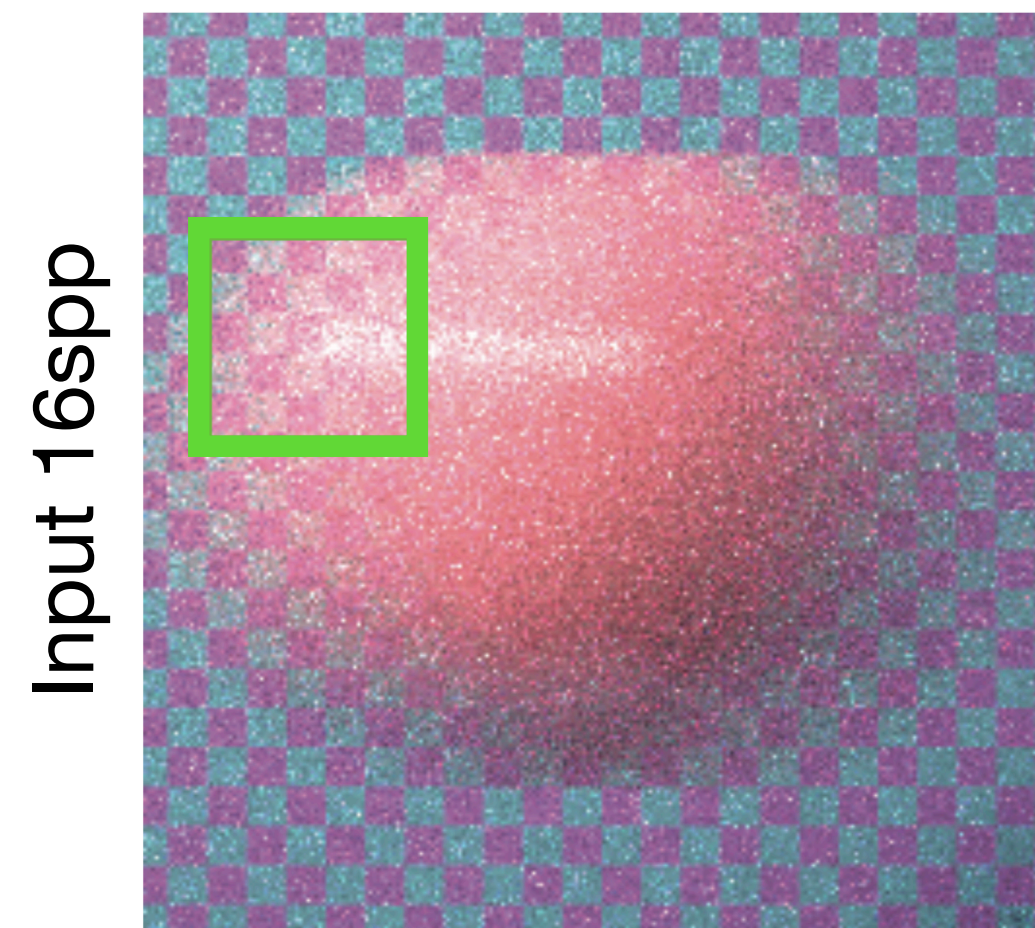
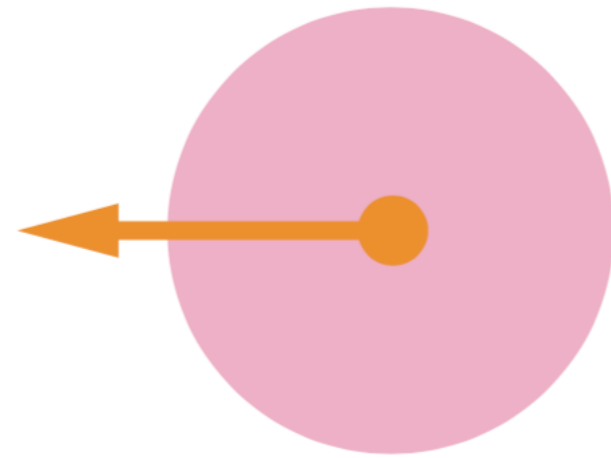
Michael Gharbi, Tzu-Mao Li, Miika Aittala, Jakko Lehtinen, Fredo Durand

SIGGRAPH 2019

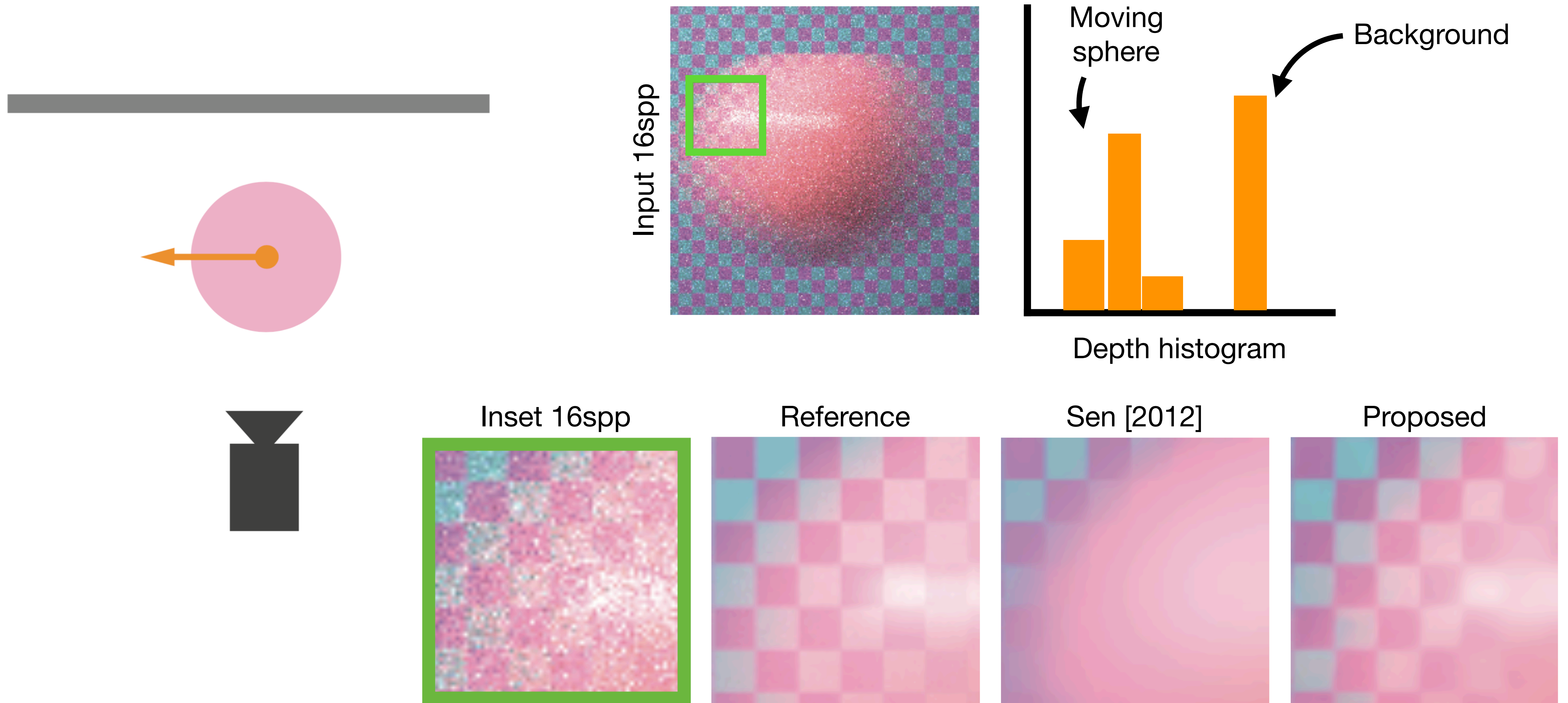
# Multimodal distribution of sample features



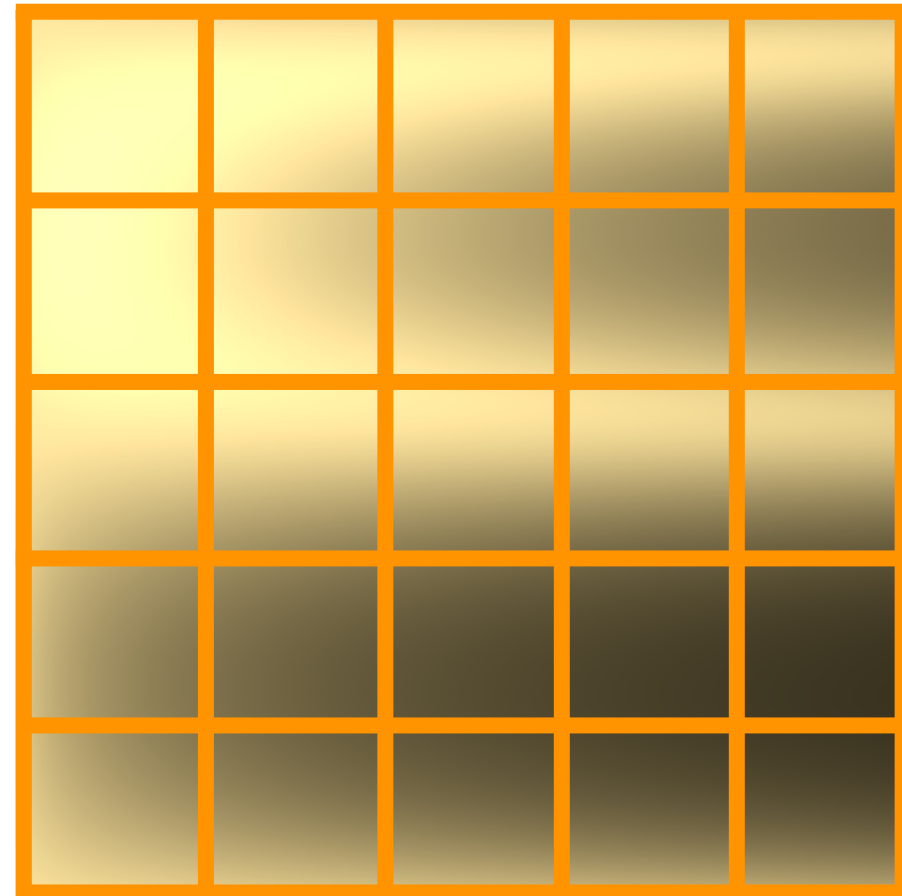
# Multimodal distribution of sample features



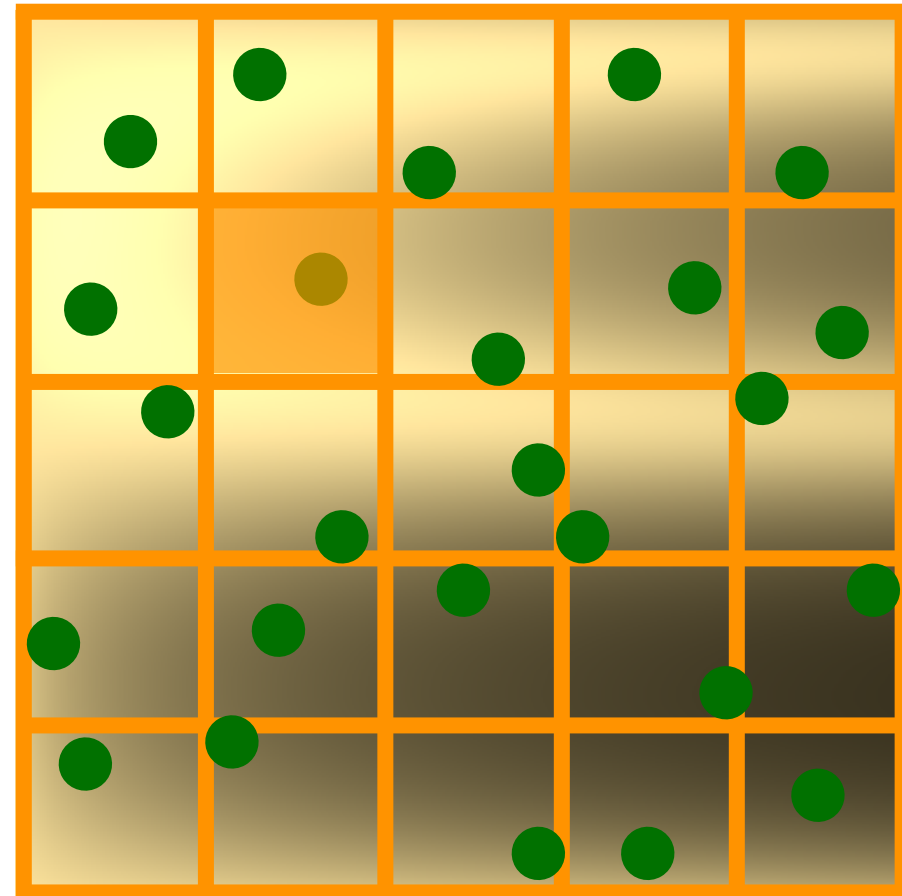
# Multimodal distribution of sample features



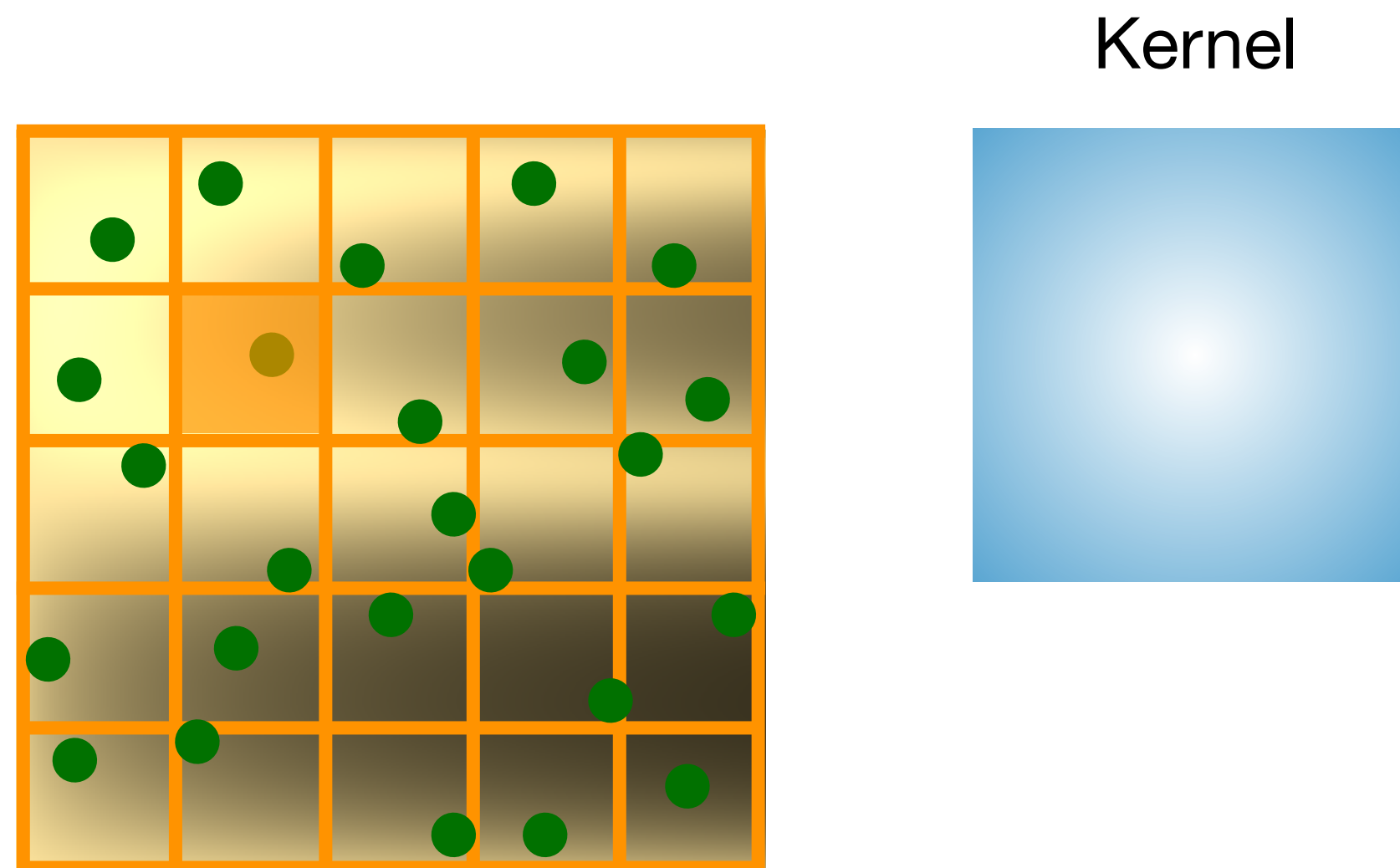
# Reconstruction: Kernel Gather



# Reconstruction: Kernel Gather

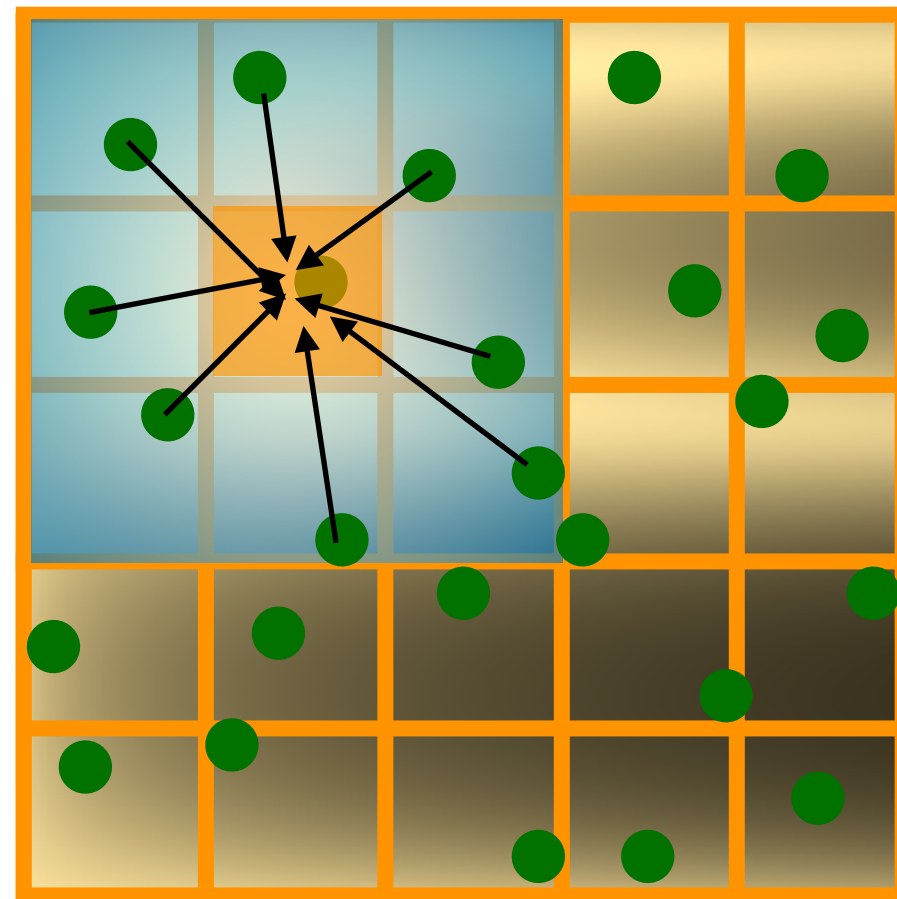


# Reconstruction: Kernel Gather



# Reconstruction: Kernel Gather

Kernel gather



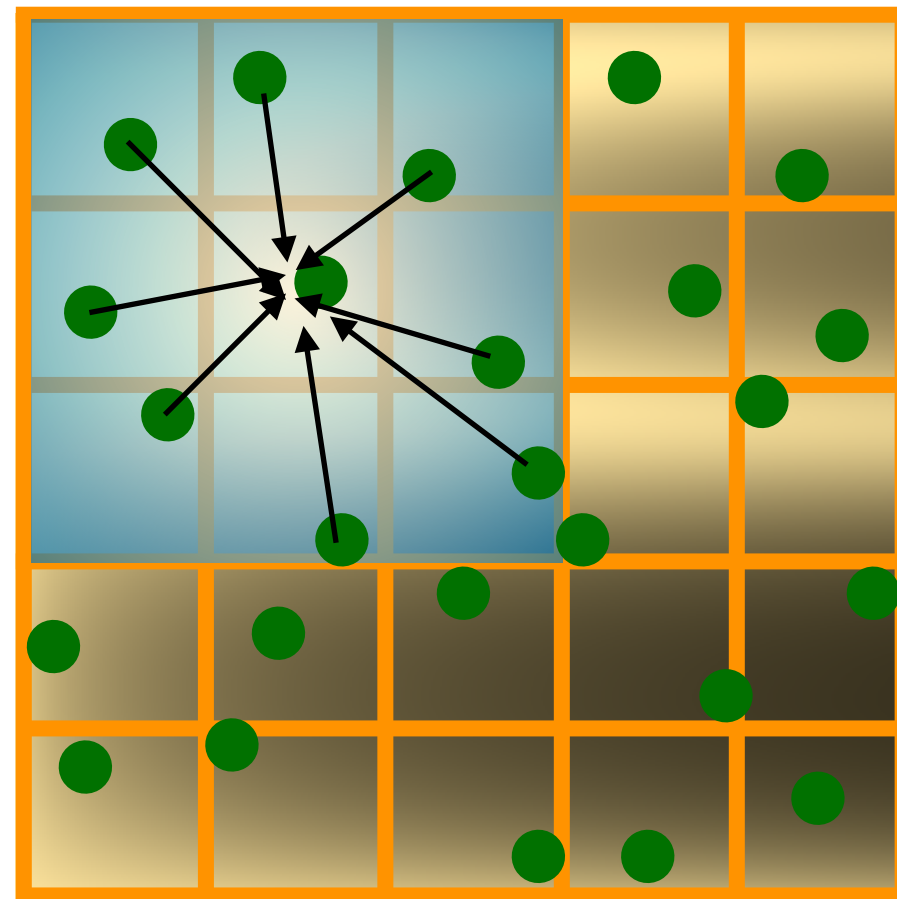
2D example

*How should nearby samples influence me?*



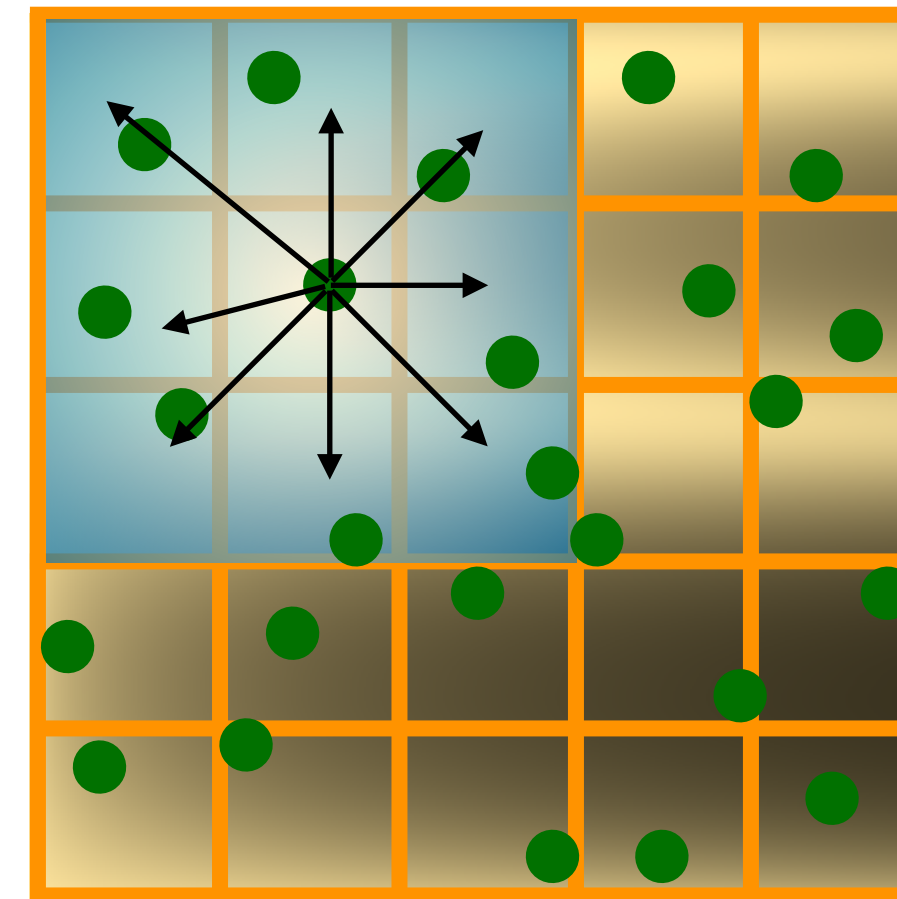
# Reconstruction: Kernel Splatting

Kernel gather



2D example

Kernel Splatting

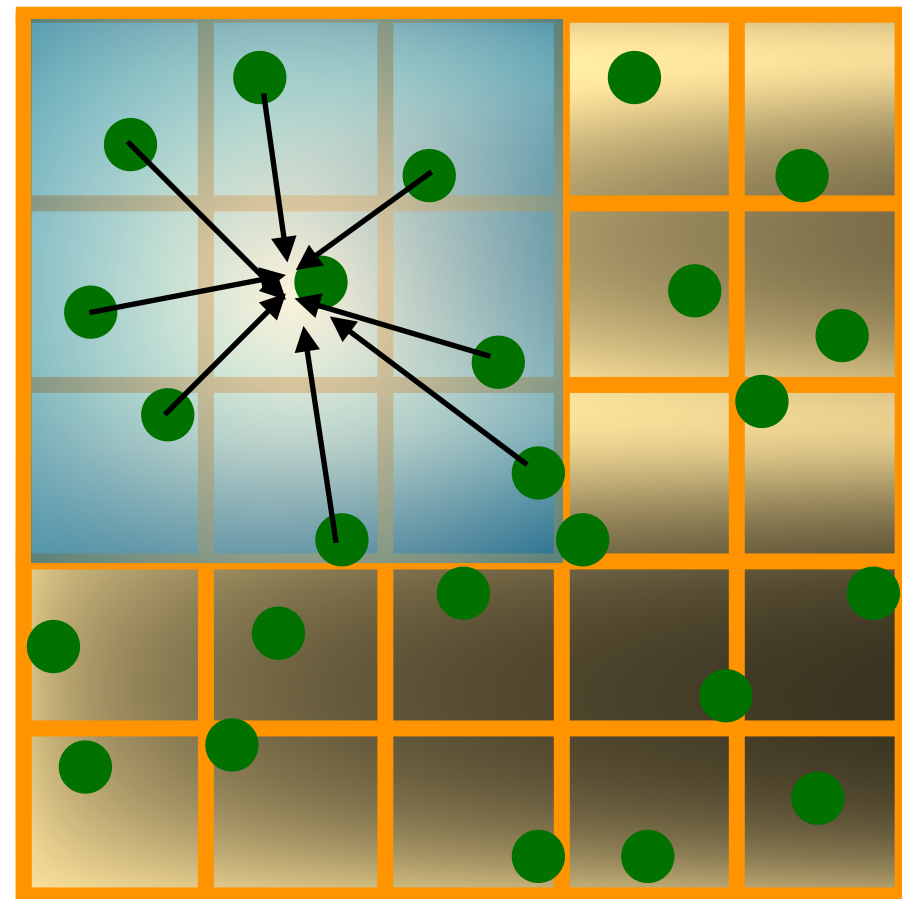


2D example

*How should nearby samples influence me?*

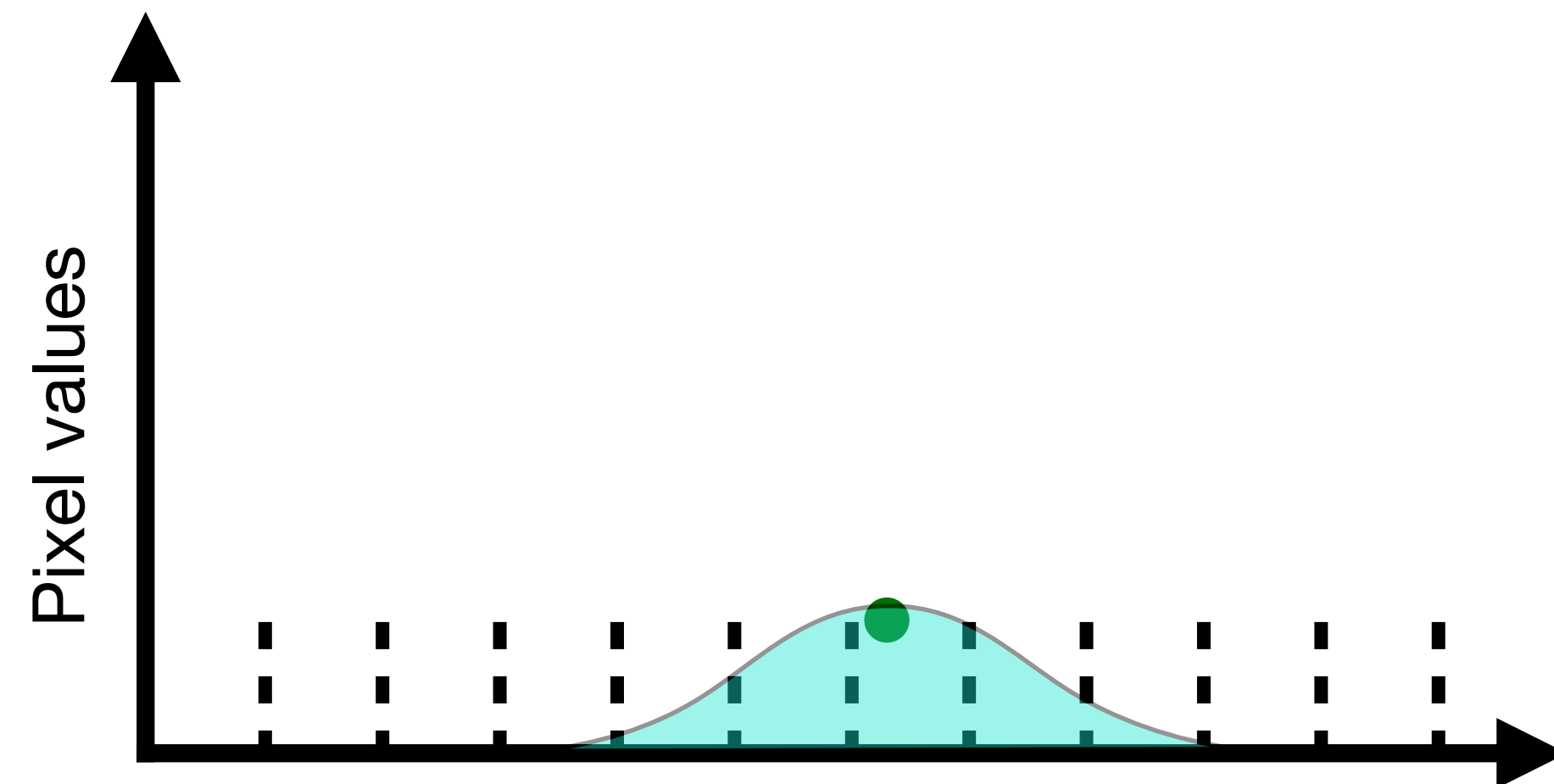
# Reconstruction: Kernel Splatting

Kernel gather



2D example

Kernel Splatting

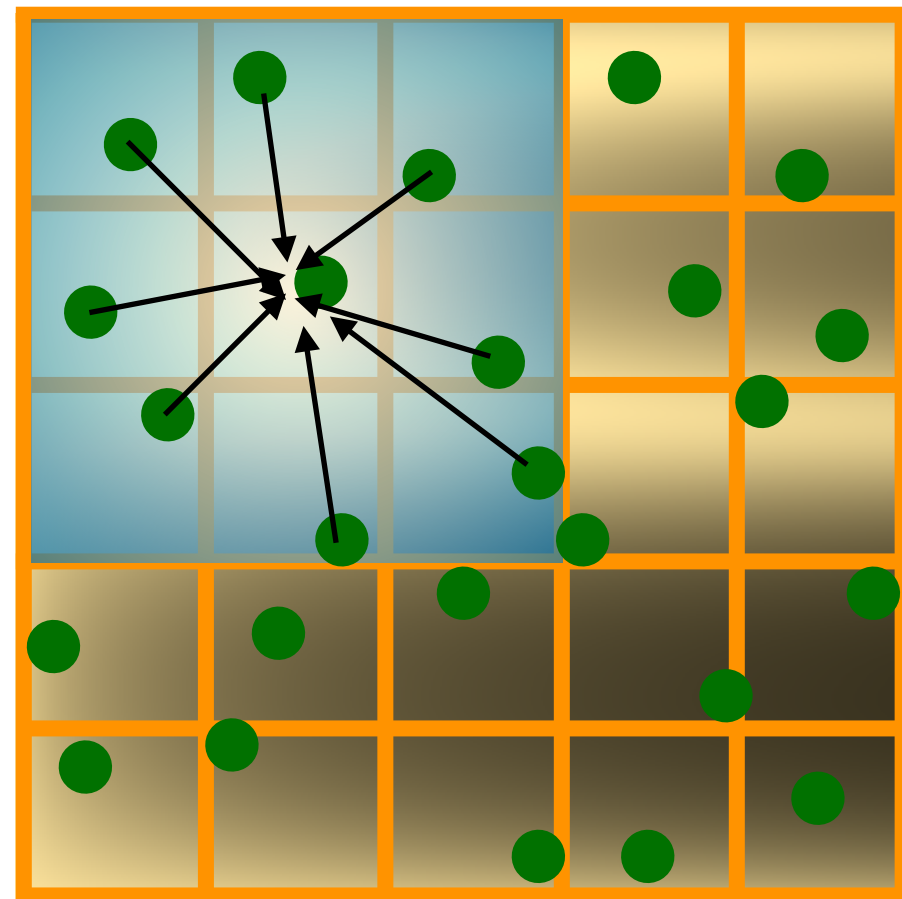


1D example

*How should nearby samples influence me?*

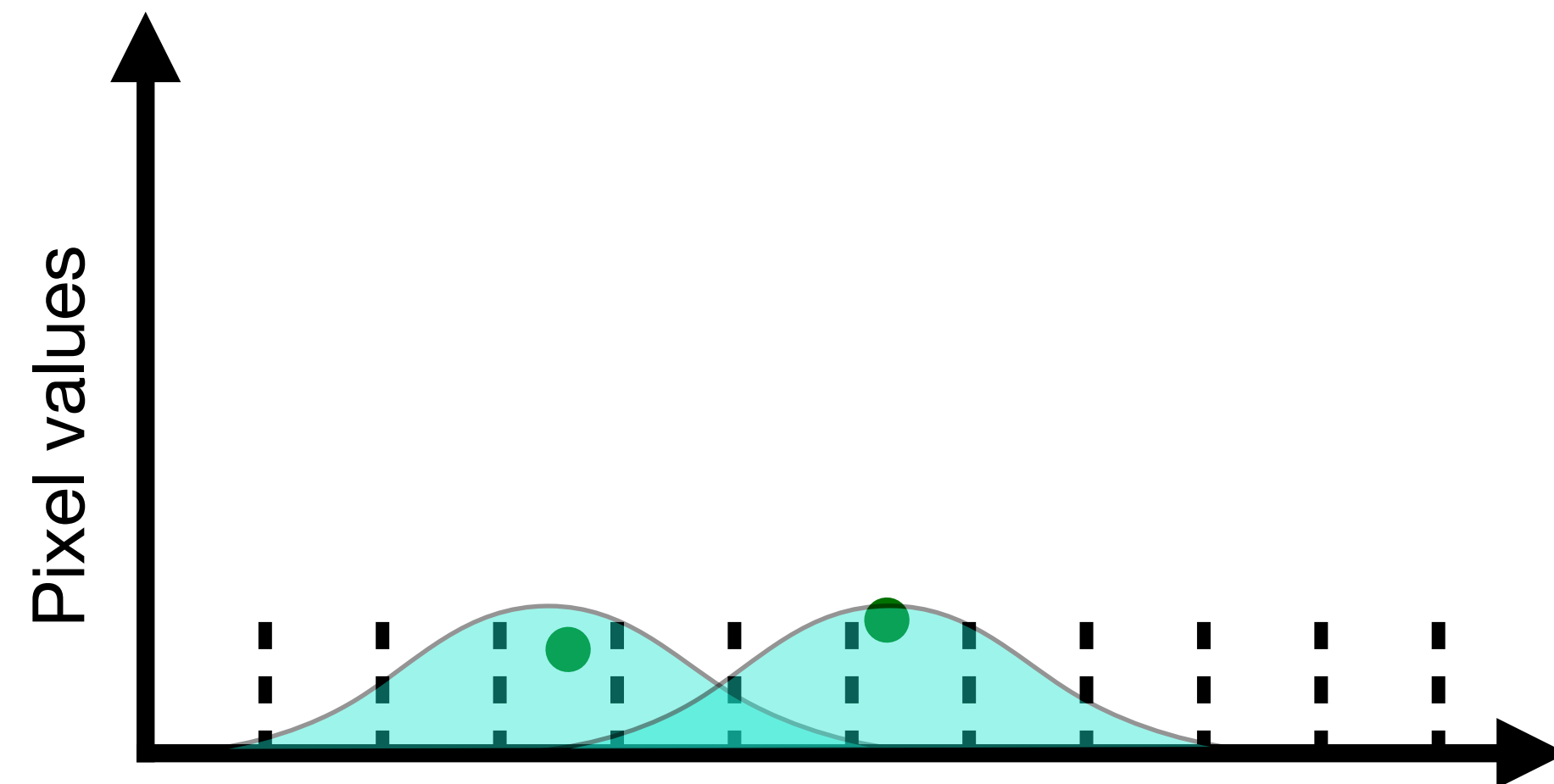
# Reconstruction: Kernel Splatting

Kernel gather



2D example

Kernel Splatting

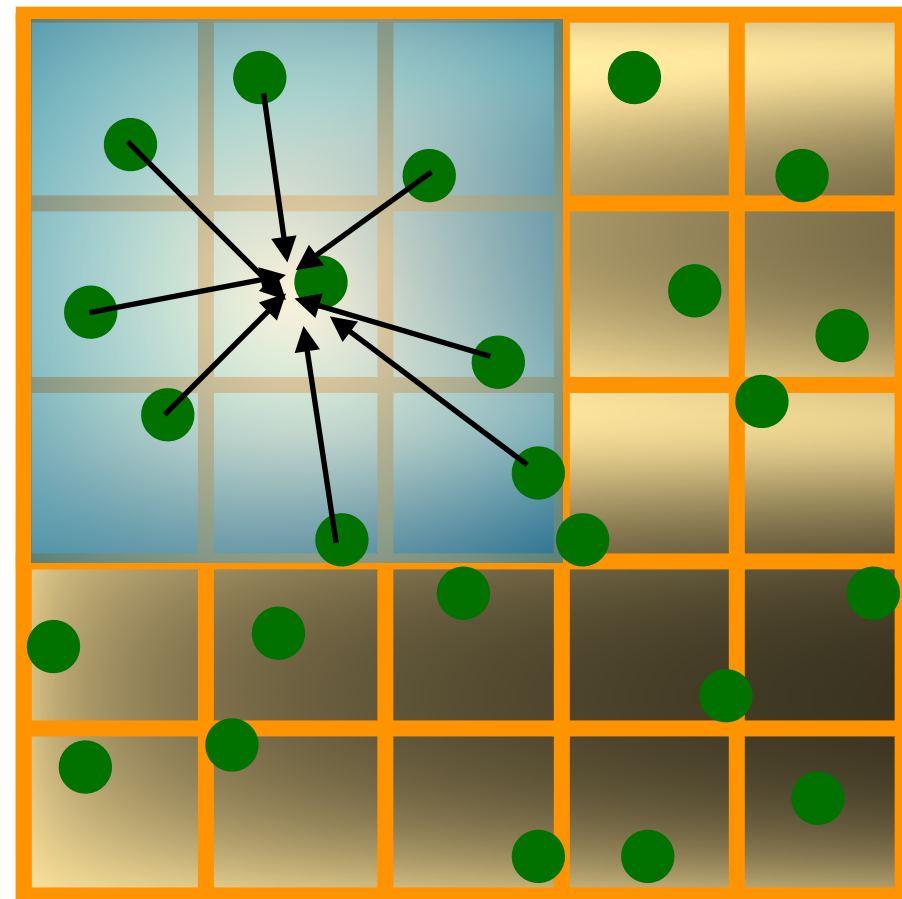


1D example

*How should nearby samples influence me?*

# Reconstruction: Kernel Splatting

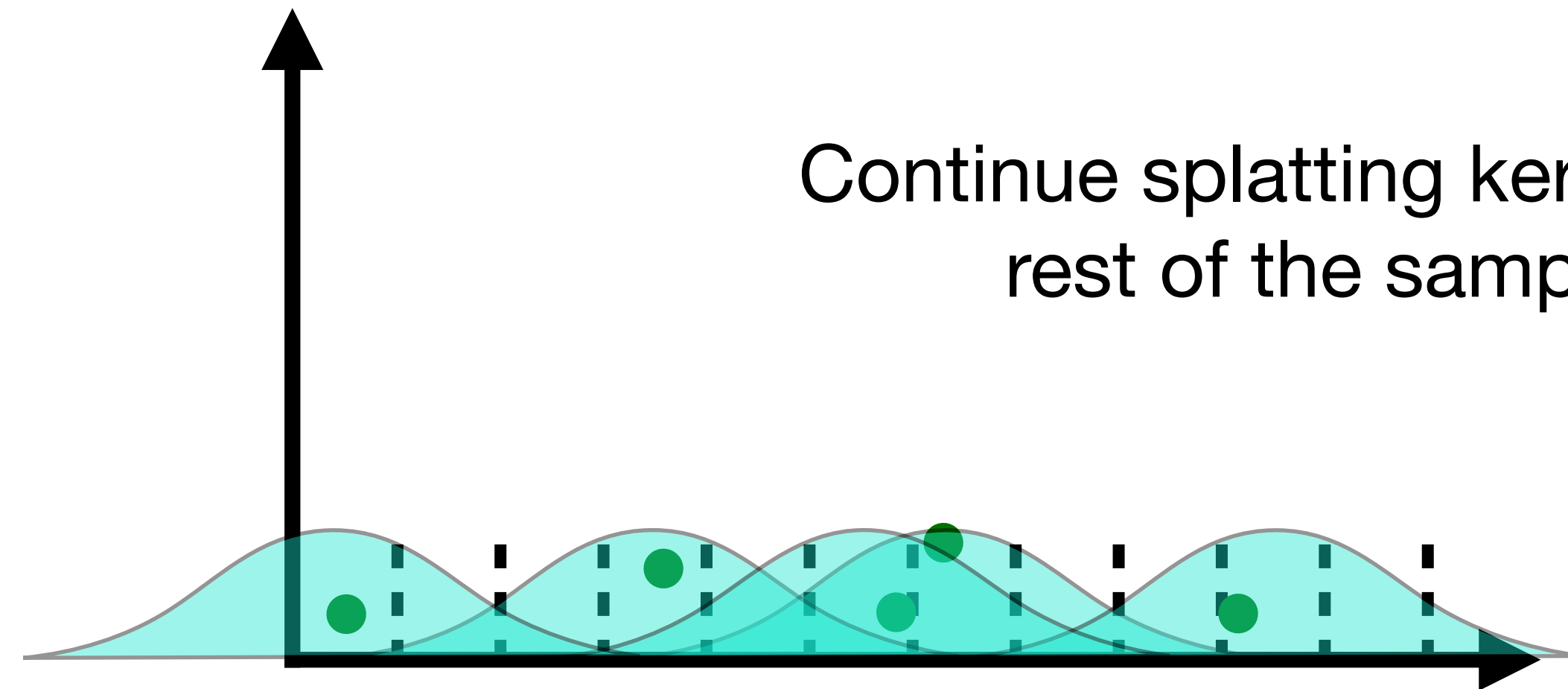
Kernel gather



2D example

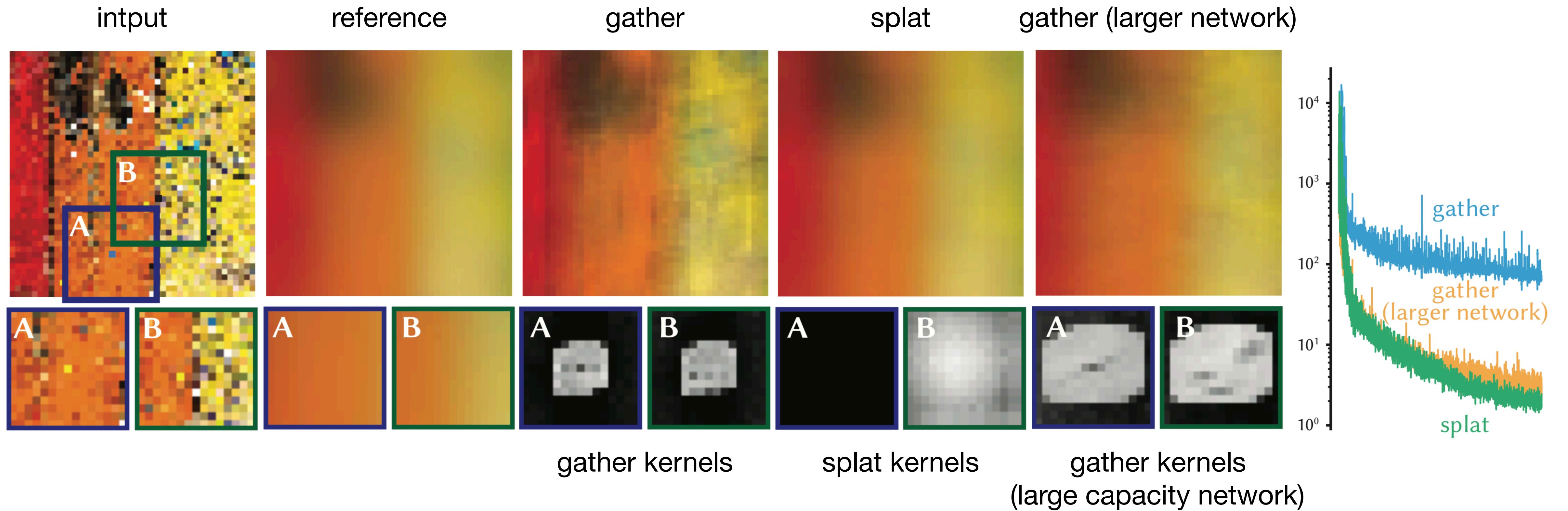
*How should nearby samples influence me?*

Kernel Splatting



*How do I contribute to nearby pixels,  
given all the samples around me?*

# Network: Kernel Gather vs Splatting



# Permutation Invariance

# Permutation Invariance

A model that produces the same output regardless of the order of elements in the input vector

# Permutation Invariance: Example



\*



=



# Permutation Invariance: Example



# Permutation Invariance: Example

Not Permutation Invariance



\*



=



\*



=

# Permutation Invariance: Example

Not Permutation Invariance



\*



=



\*



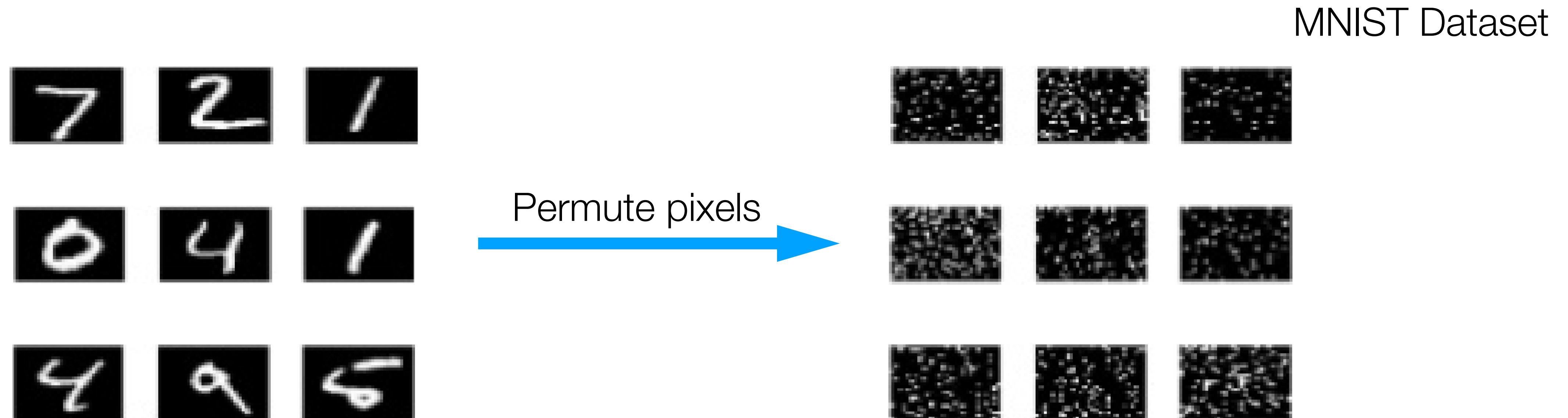
=



# Permutation Invariance: Architectures

- A standard feedforward neural net such as multilayer perceptron (MLP) is insensitive to order of elements in input vector - so it is inherently permutation insensitive
- However, both a Convnet and RNNs for instance make full use of input ordering - they are permutation sensitive.

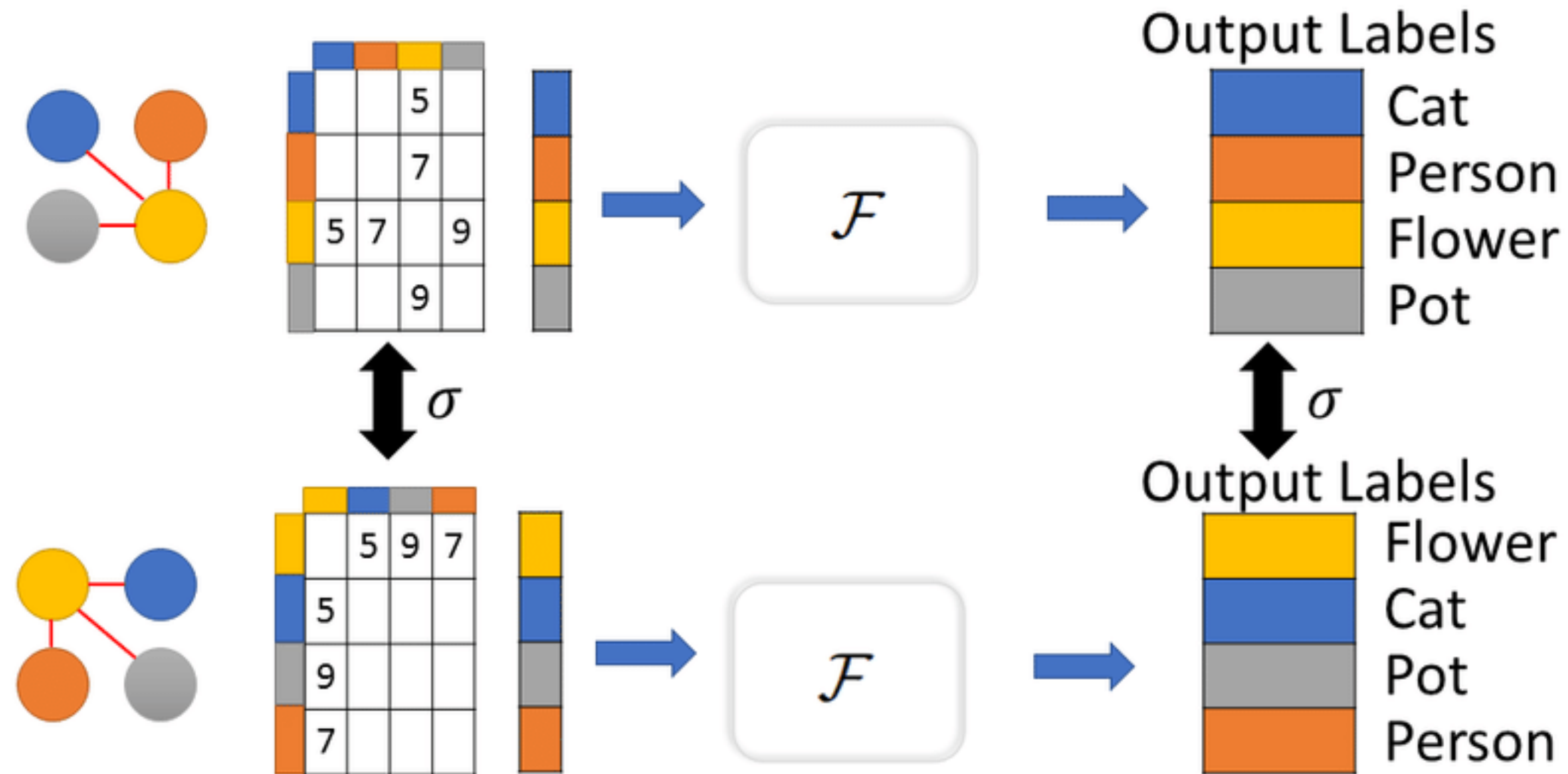
# Permutation Invariance: Example



Permuting pixels makes it difficult for humans to understand the images.

However, permutation invariant networks like MLP can detect digits irrespective of the order of pixels

# Permutation Invariance: Example

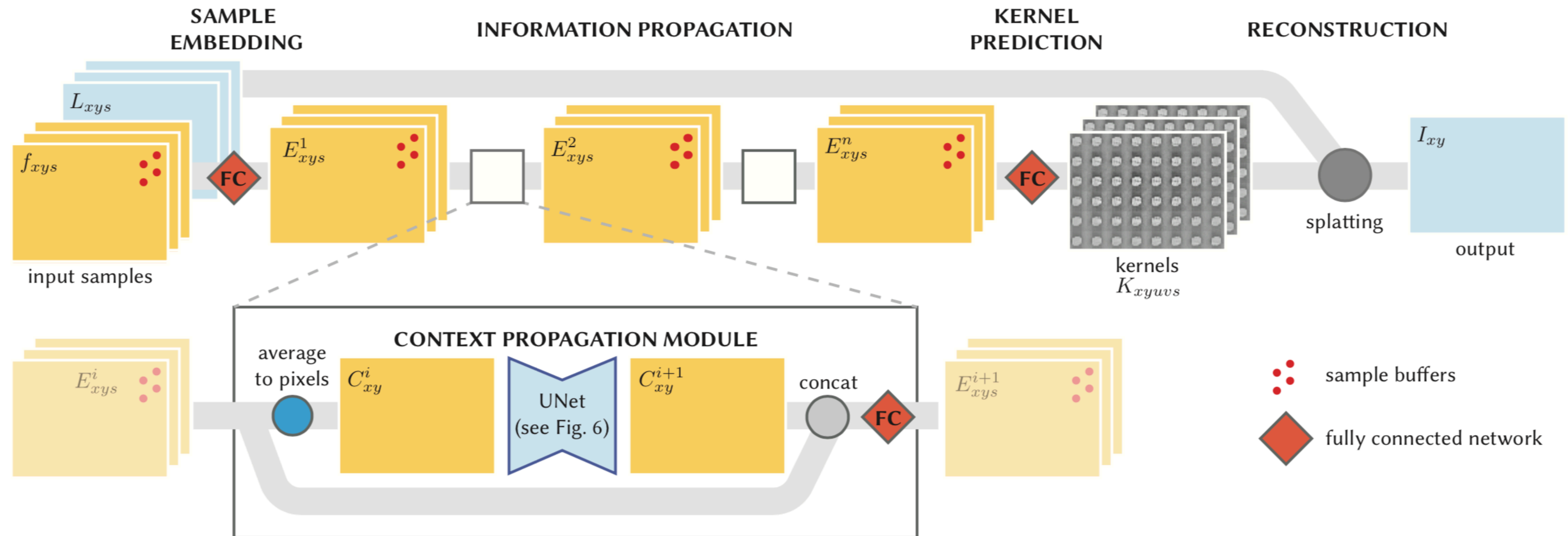


A graph labeling function  $\mathcal{F}$  is graph permutation invariant (GPI) if permuting the names of nodes maintains the output. Herzig et al.[2018]

# Permutation Invariance

- In MLPs, since each component is connected to each other, the order does not matter
- In structured convolutions, the order matters and therefore, it is not permutation invariant.

# Proposed Network Architecture





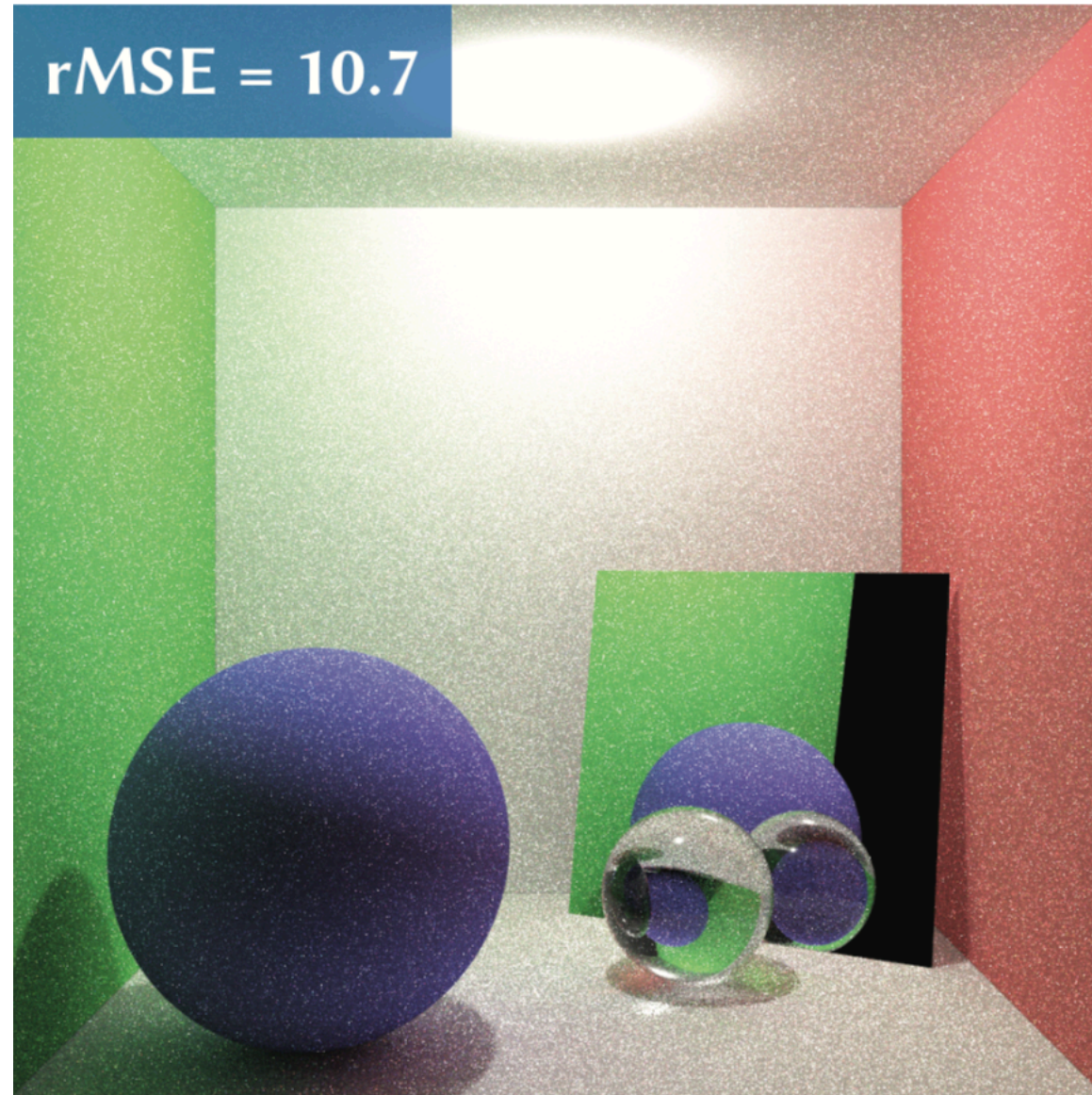
# Dataset and Training Procedure

Procedurally generated dataset: 300,000 renderings with 128x128 resolution

Also generated input buffer (4, 32 spp), but this time also maintained auxiliary features

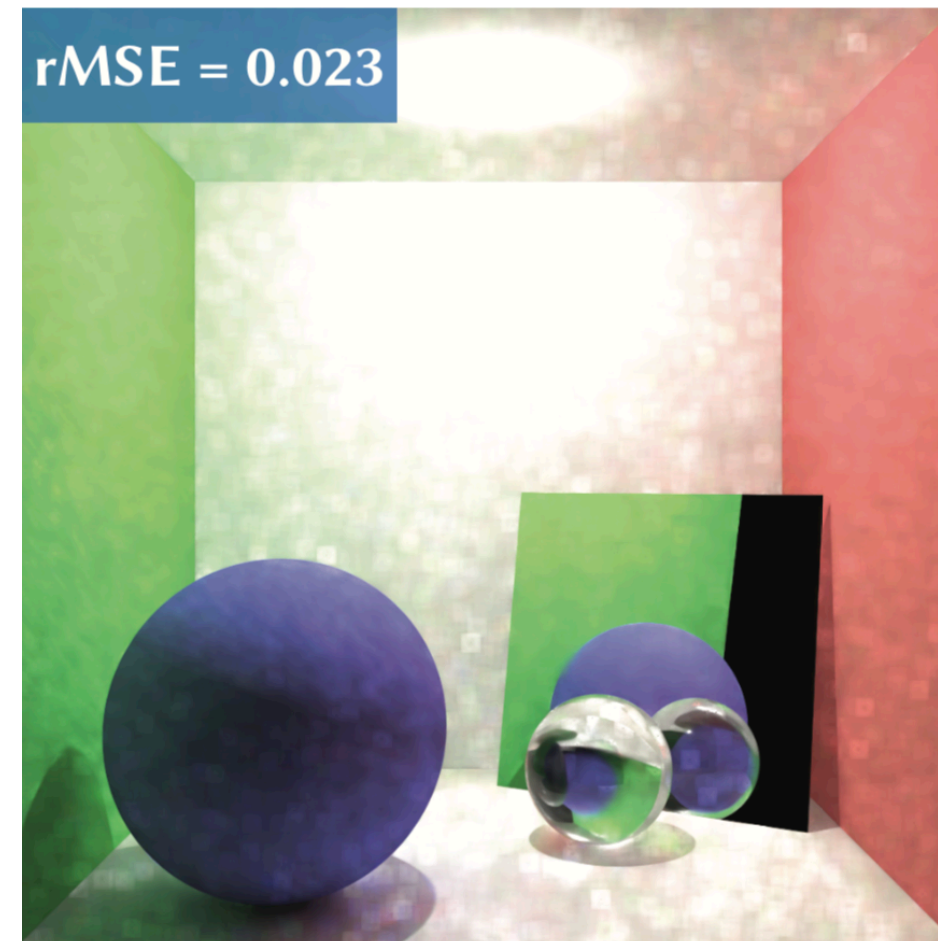
Reference was generated for 4096 samples

# Splat vs Gather

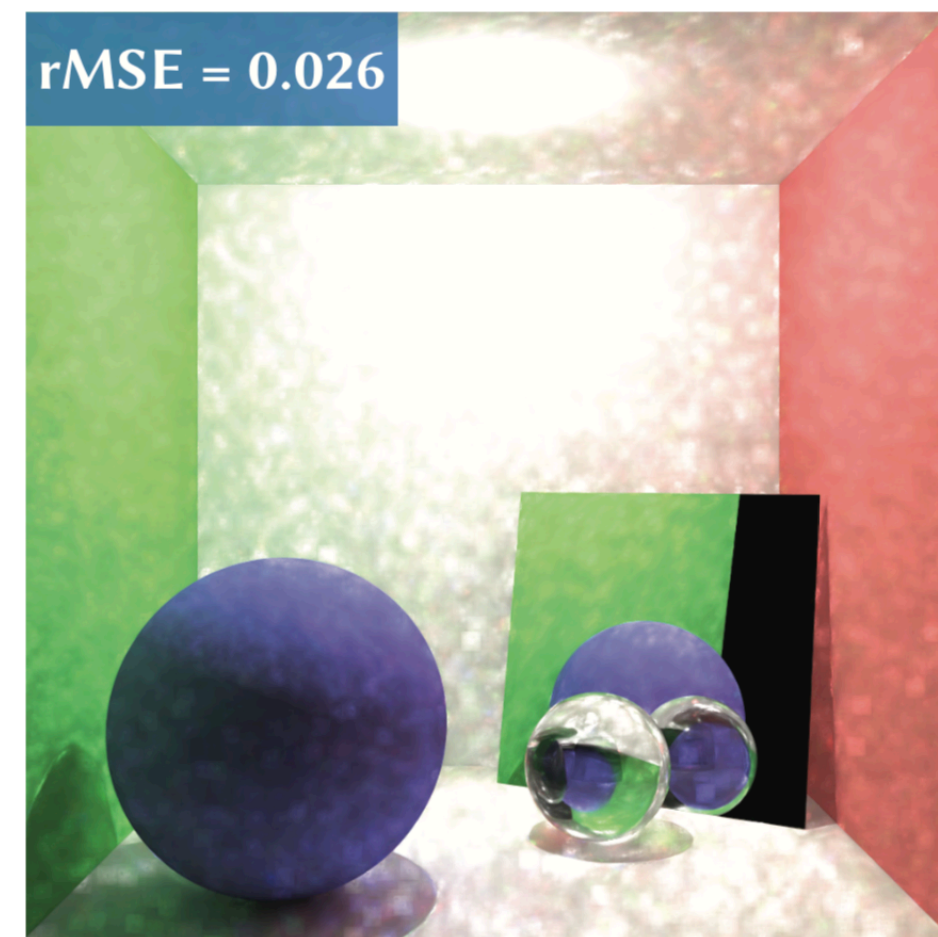


Input

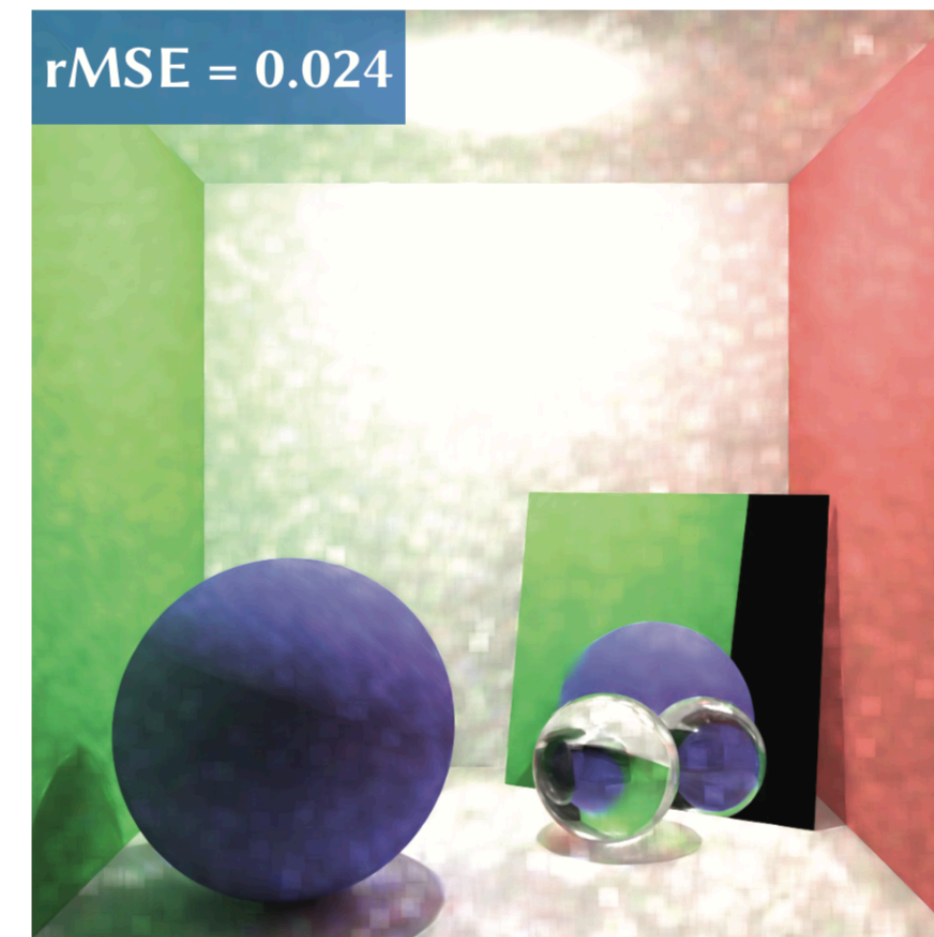
per sample gather



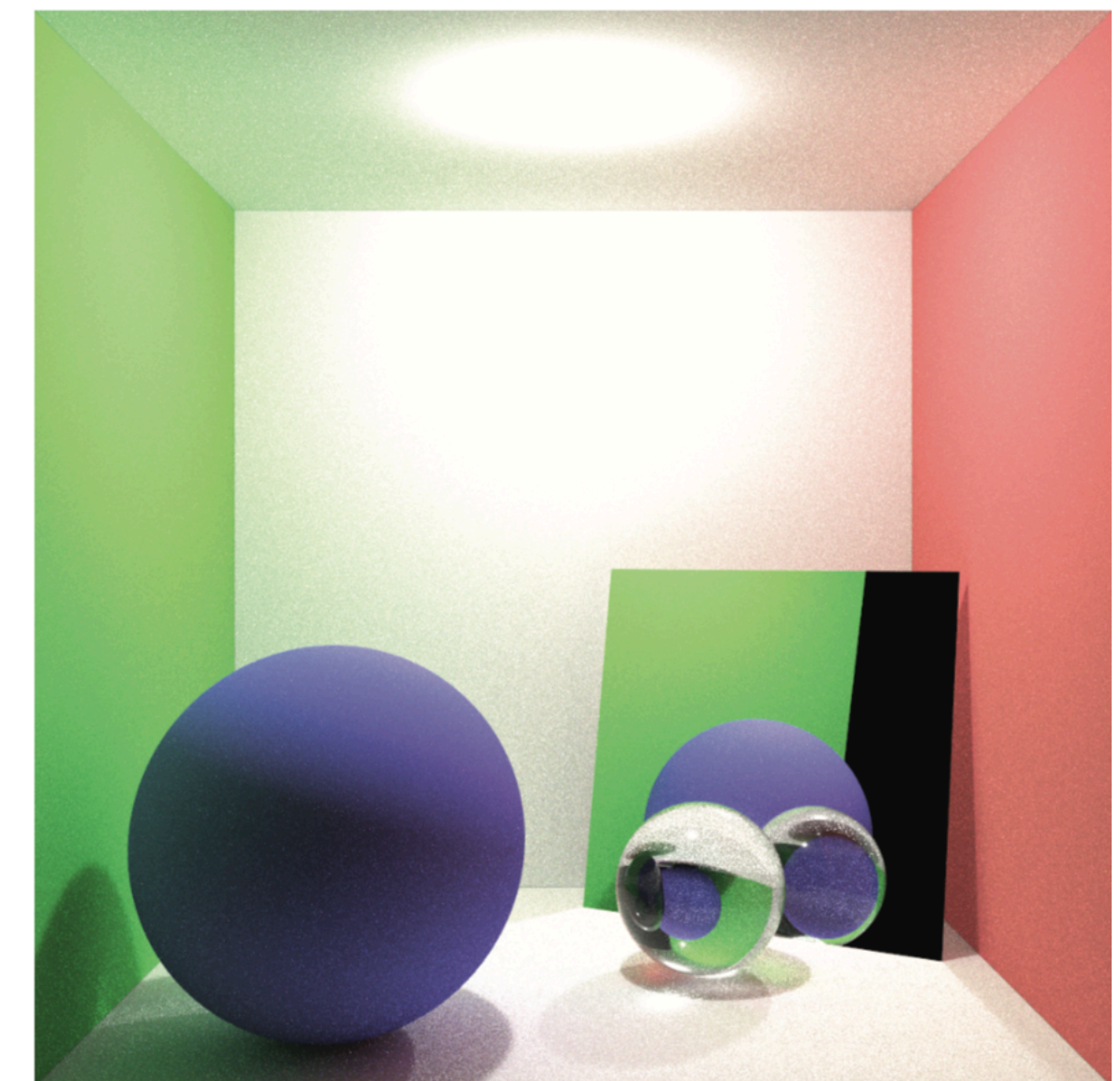
per pixel gather



per sample splat



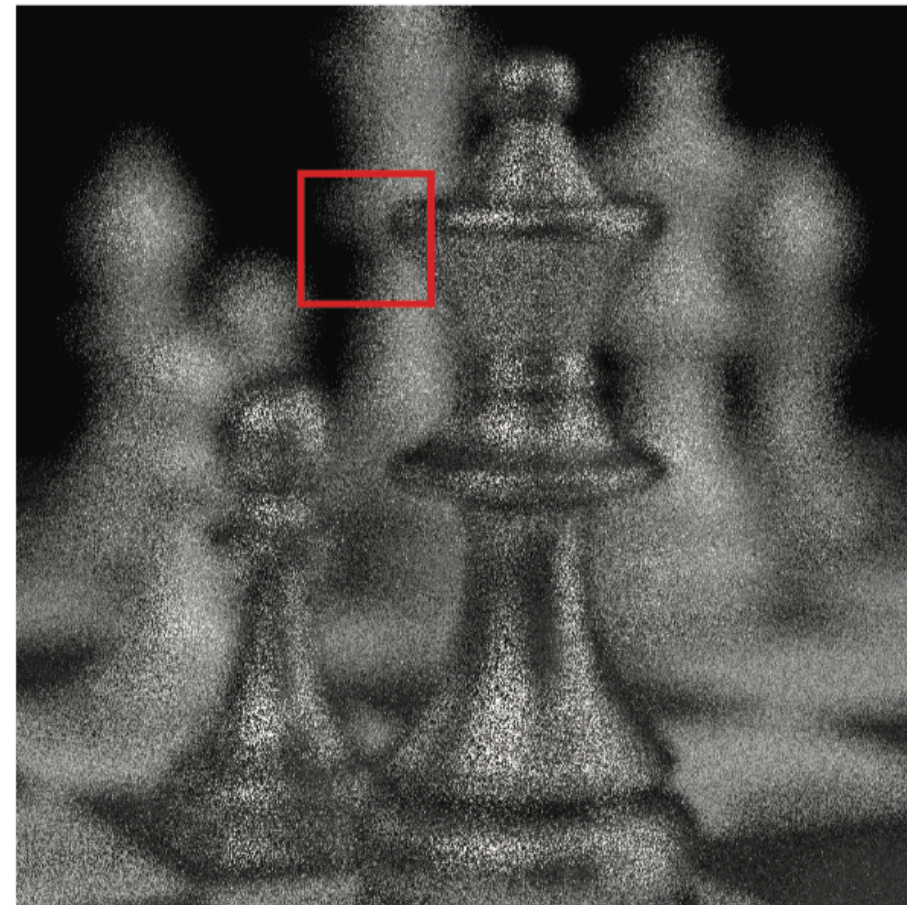
per pixel splat



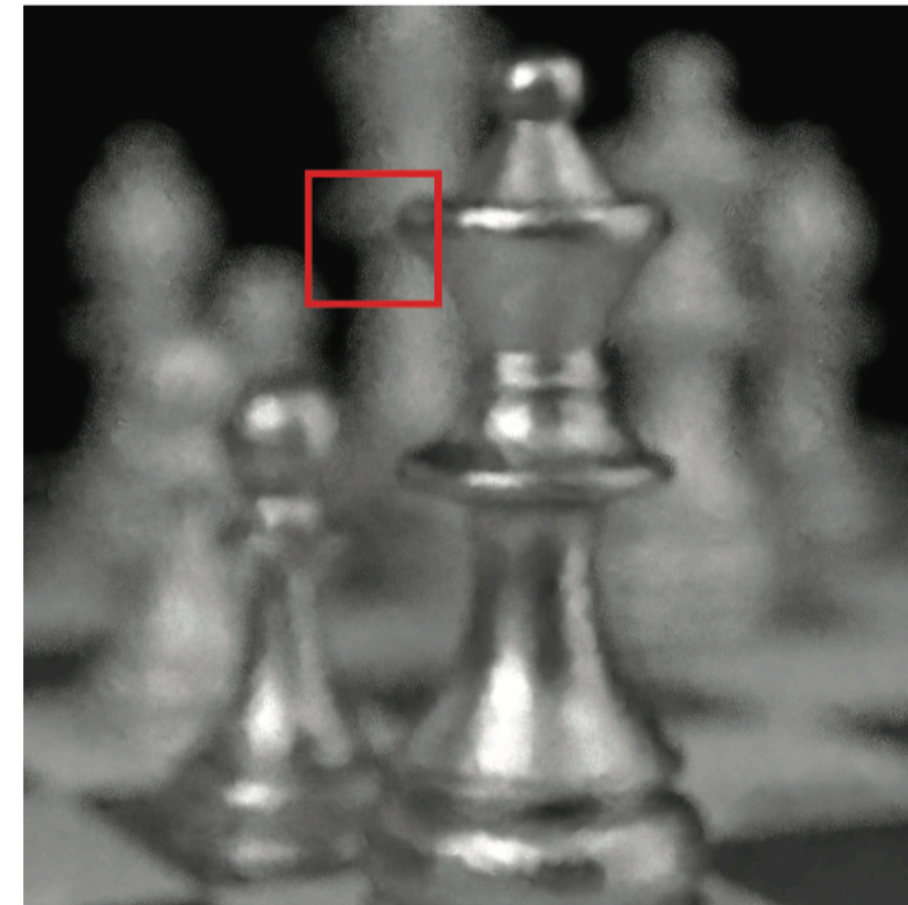
Reference

# Results

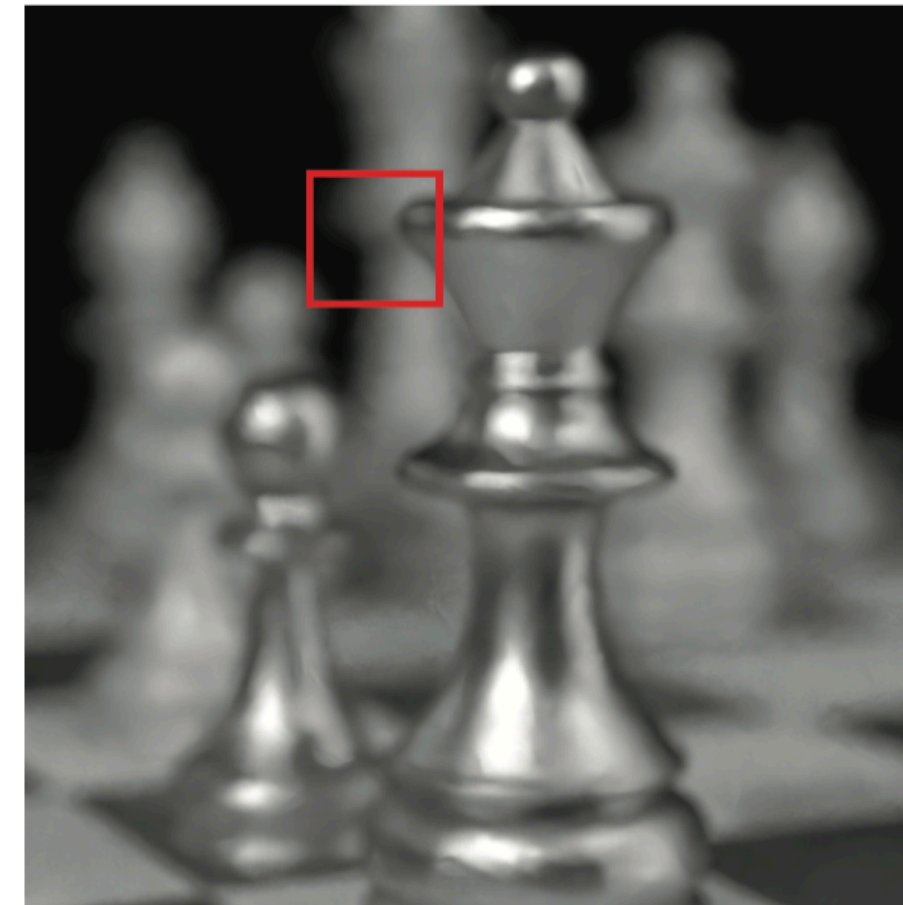
input 4spp



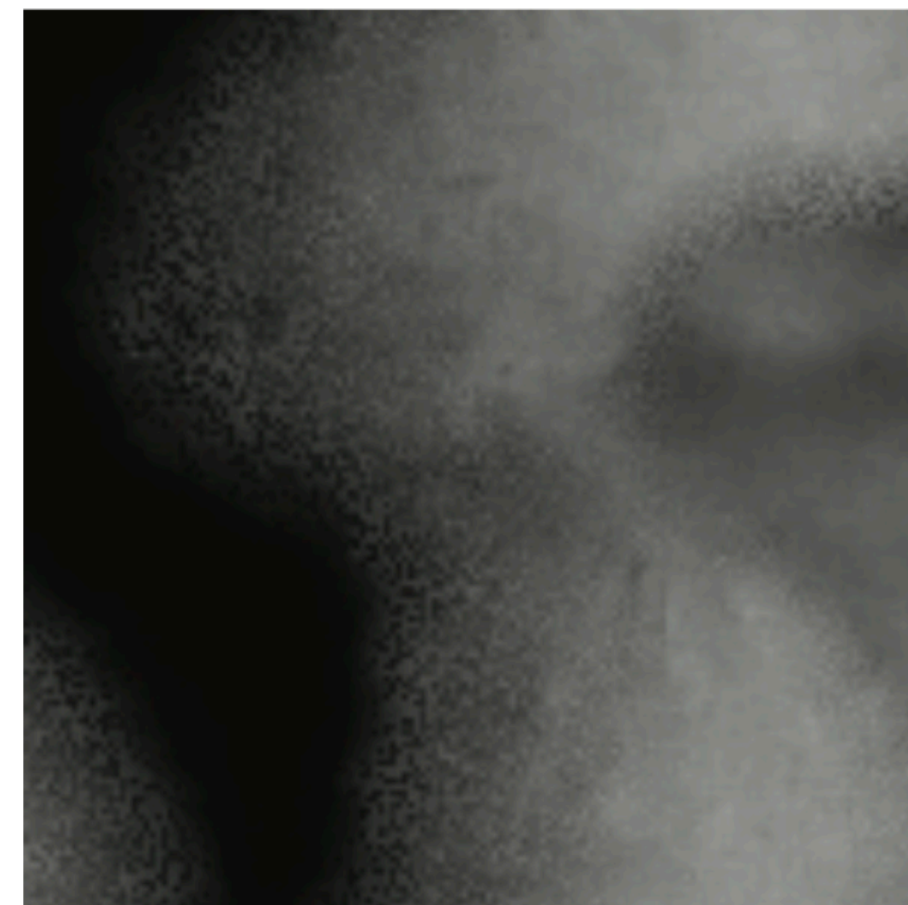
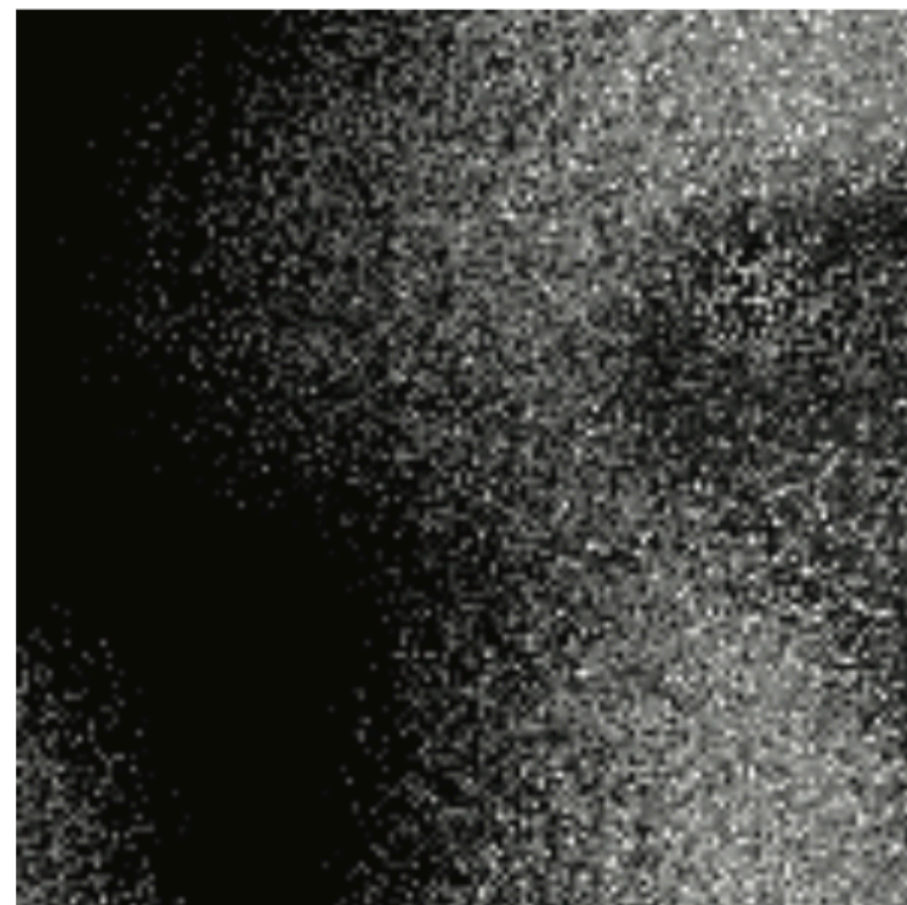
[Bako 2017]



ours



ref. 8192spp



# Network Architecture Comparisons

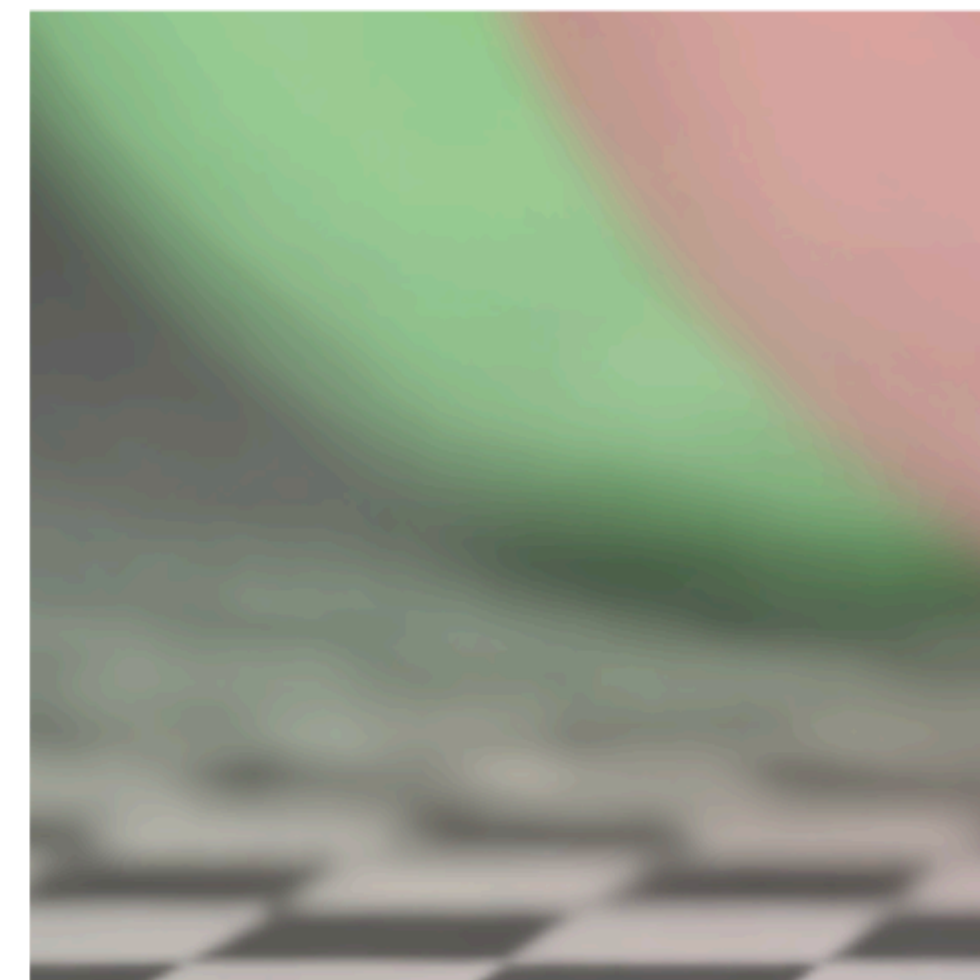
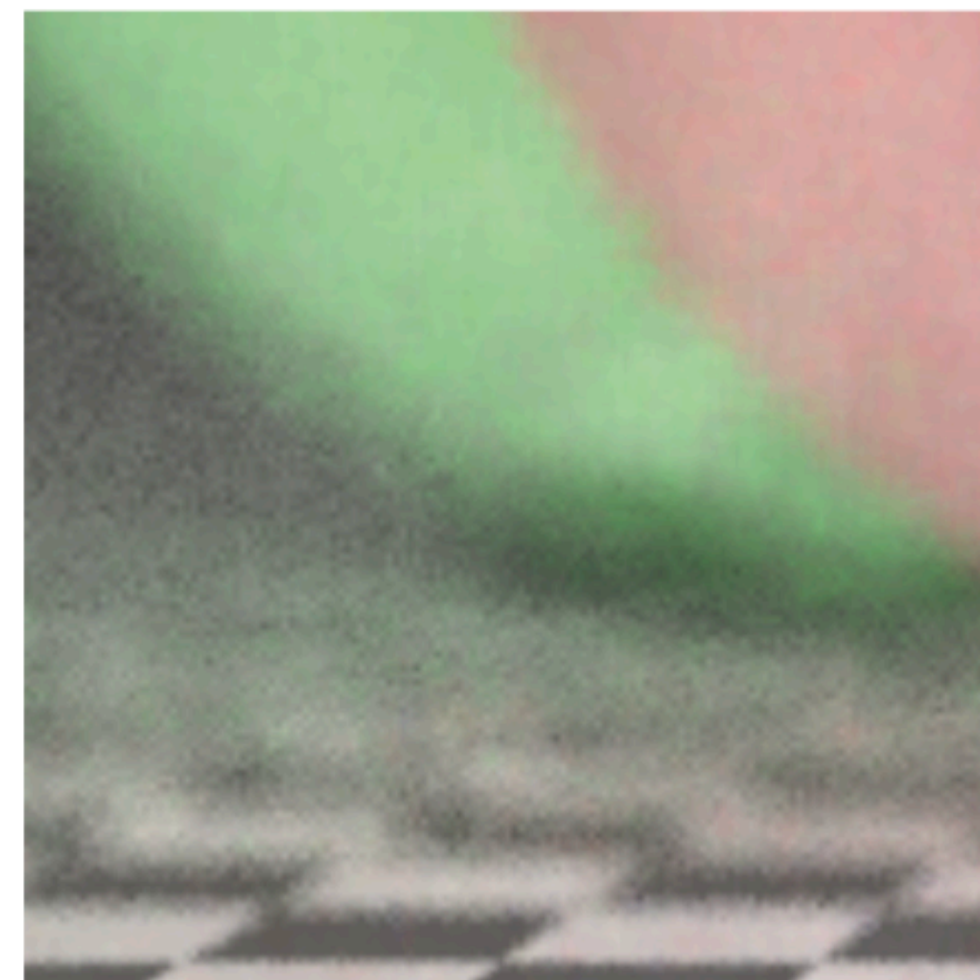
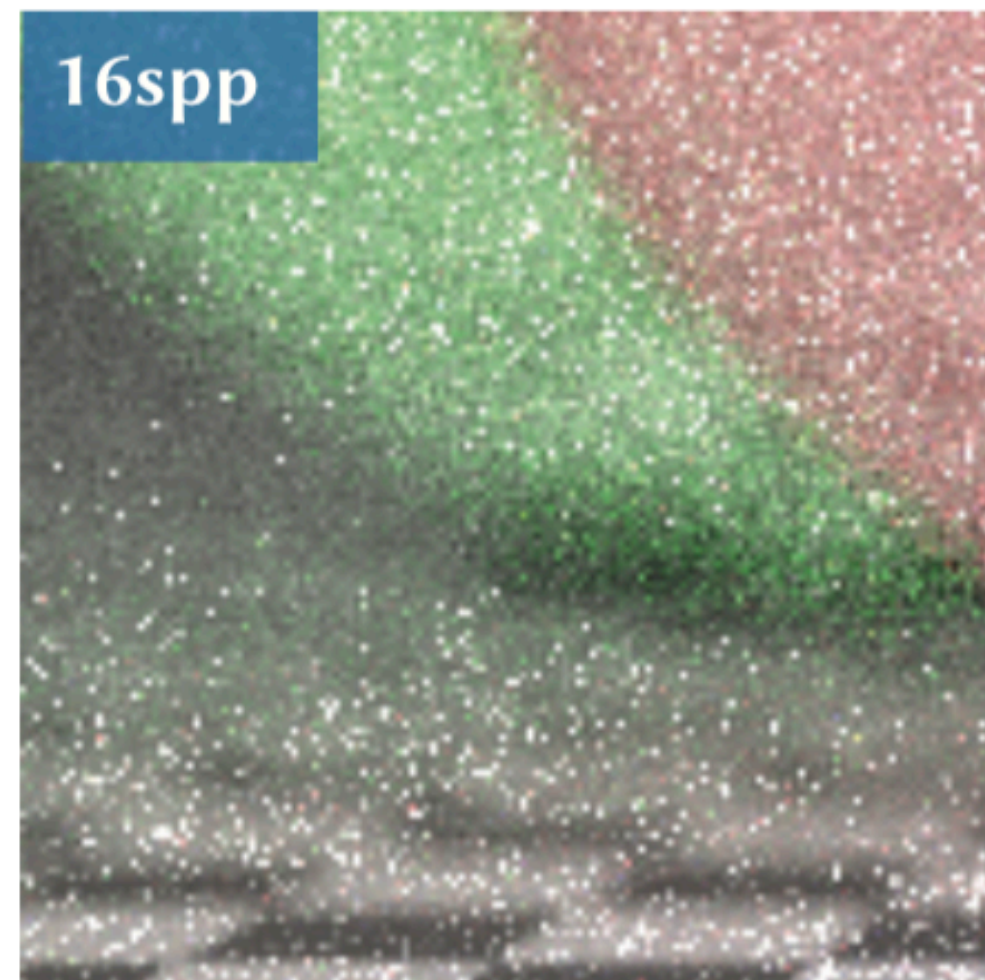
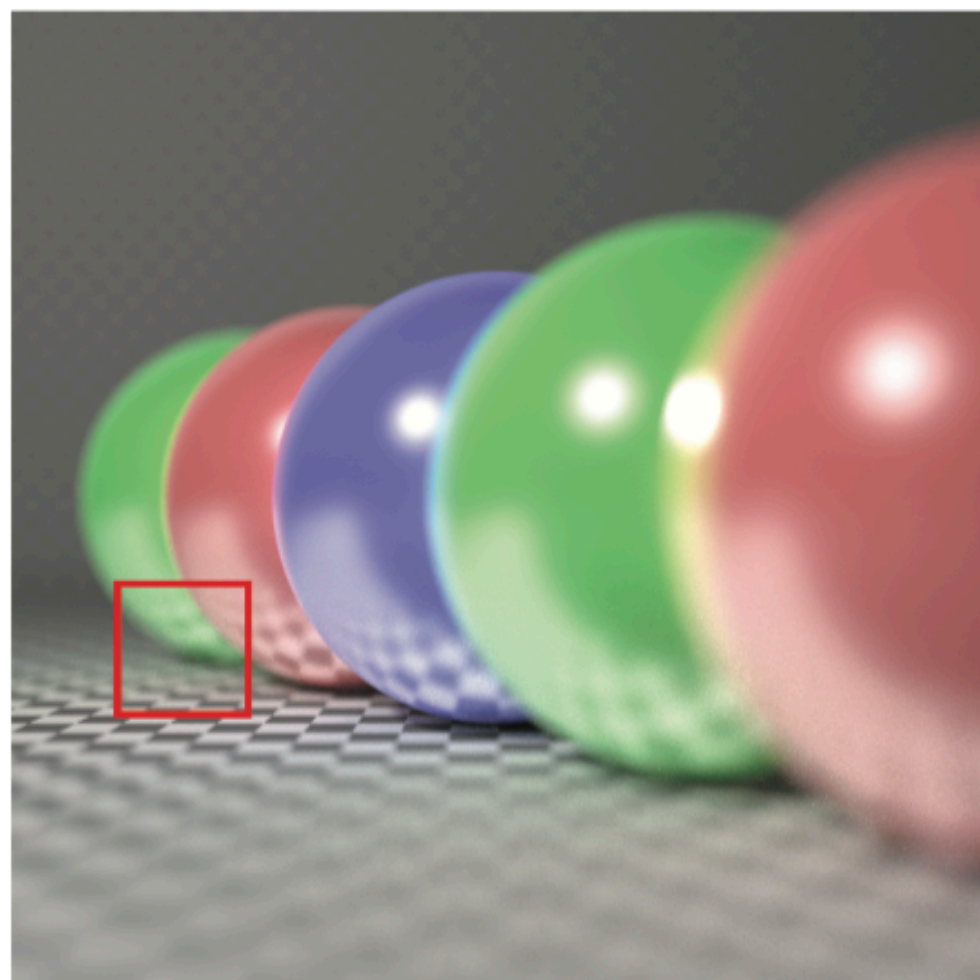
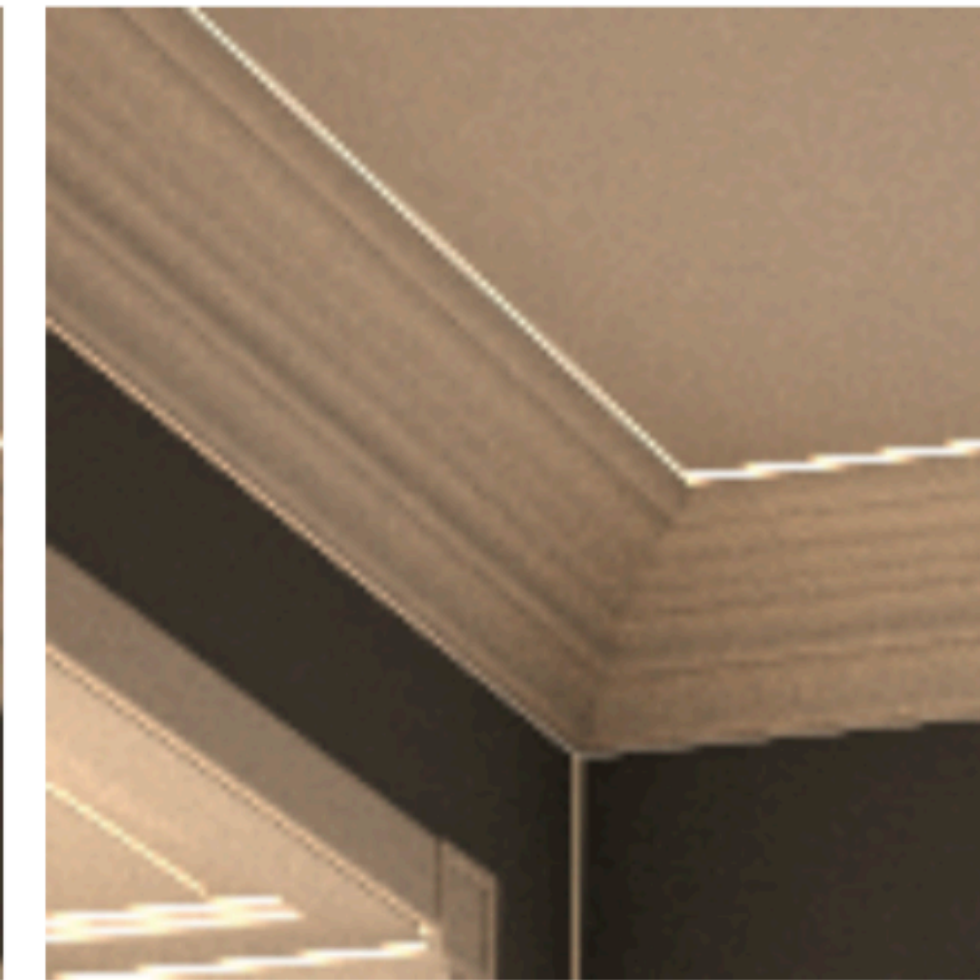
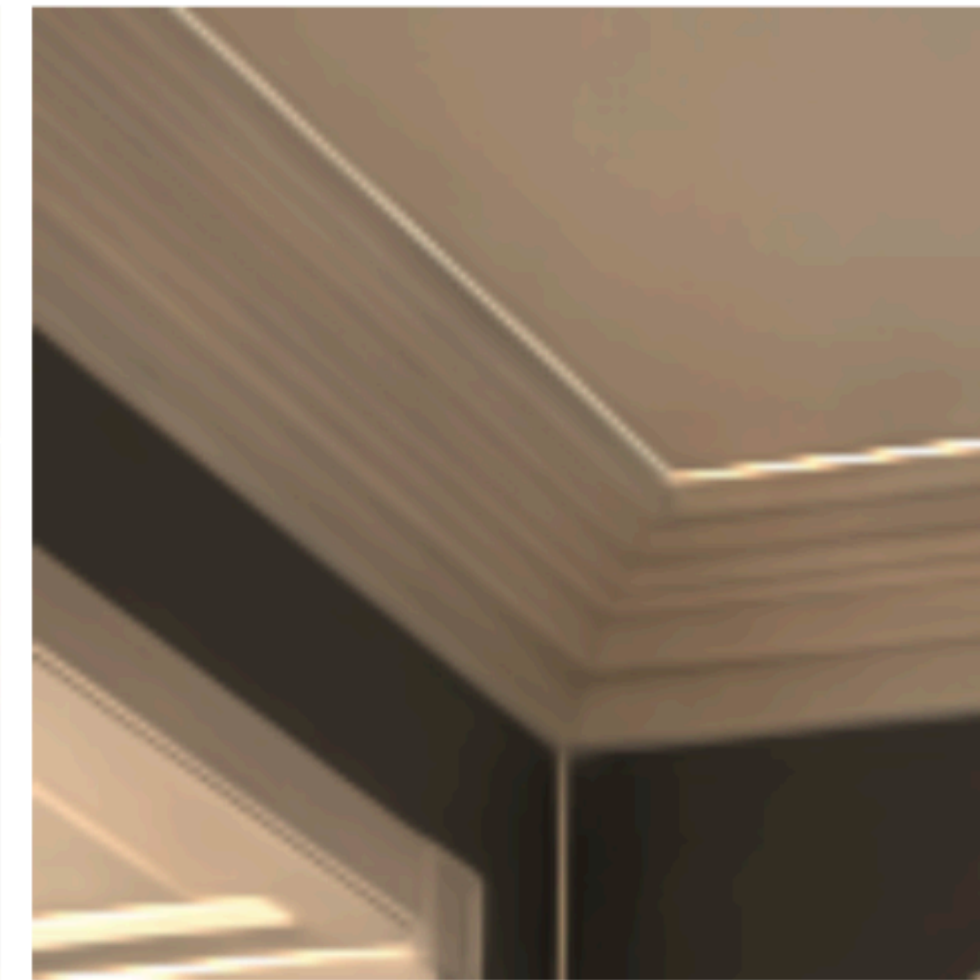
reference 8192spp

input

finetuned [Bako2017]

ours

reference 8192spp



# Final Exam

20.08.19 from 10:00 to 13:00 in HS 002

# References

A frequency analysis of light transport, Durand et al. SIGGRAPH 2005

Frequency Analysis and Sheared Reconstruction for Rendering Motion Blur, Egan et al. SIGGRAPH 2009

Temporal Light Field Reconstruction for Rendering Distribution Effects, Lehtinen et al. SIGGRAPH 2011

On Filtering the Noise from the Random Parameters in Monte Carlo Rendering, Sen and Darabi 2012

A Machine Learning Approach for Filtering Monte Carlo Noise, Kalantari et al. SIGGRAPH 2015

Interactive Reconstruction of Monte Carlo Image Sequences using a Recurrent Denoising Autoencoder, Chaitanya et al. SIGGRAPH 2017

Kernel-Predicting Convolutional Networks for Denoising Monte Carlo Renderings, Bako et al. SIGGRAPH 2017

Sample-based Monte Carlo Denoising using a Kernel-Splatting Network, Gharbi et al. SIGGRAPH 2019